

Jul. 5, 2023

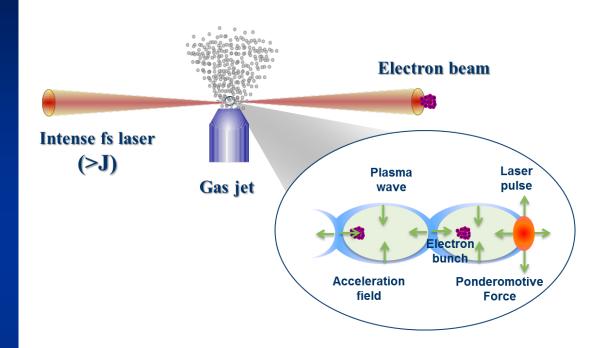


Overview: Strong field QED research

- A. Laser-driven electron acceleration
- **B. Nonlinear Compton scattering**



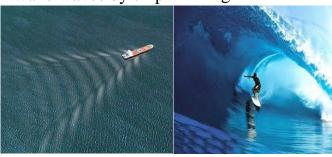
Laser Wakefield Electron Acceleration



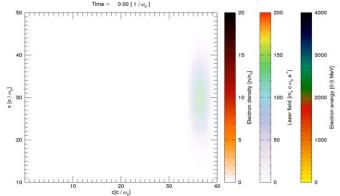
Electrons pushed out by ponderomotive force and pulled back by the Coulomb force of ions

- → Creation of an electron plasma wave
- → Acceleration of an injected electron bunch by the plasma wave

Wake waves by ship Surfing to the wave



LWFA (2D PIC)

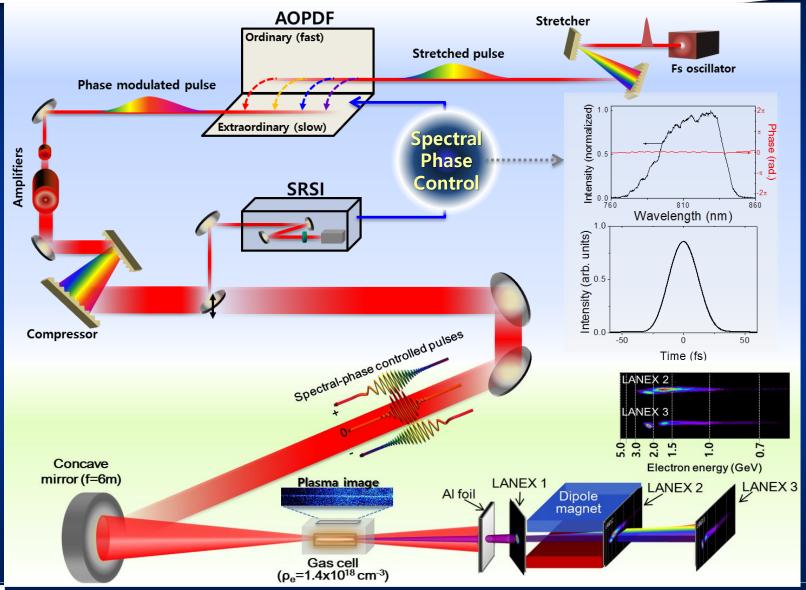


Huge acceleration field > 100 GeV/m





LWFA with structured PW laser pulses





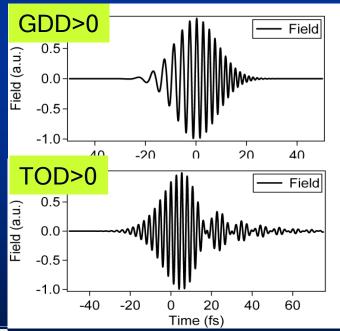


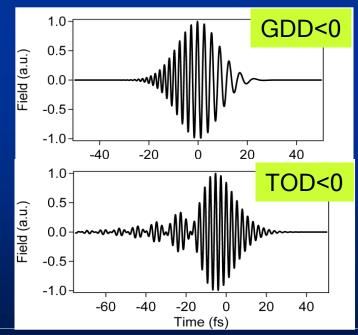
Coherent Control of Laser-Matter Interactions

spectral phase:

$$\varphi(\omega) = \varphi_0 + \varphi_1 \frac{\omega - \omega_0}{1!} + \varphi_2 \frac{(\omega - \omega_0)^2}{2!} + \varphi_3 \frac{(\omega - \omega_0)^3}{3!} + \dots$$

where
$$\left.\phi_2=\frac{d^2\varphi}{d\omega^2}\right|_{\omega=\omega_0}=$$
 group-delay dispersion (GDD) = linear chirp ,
$$\left.\phi_3=\frac{d^3\varphi}{d\omega^3}\right|_{\omega=\omega_0}=3^{\rm rd} \text{ -order spectral phase (TOD)}=\text{ quadratic chirp}$$



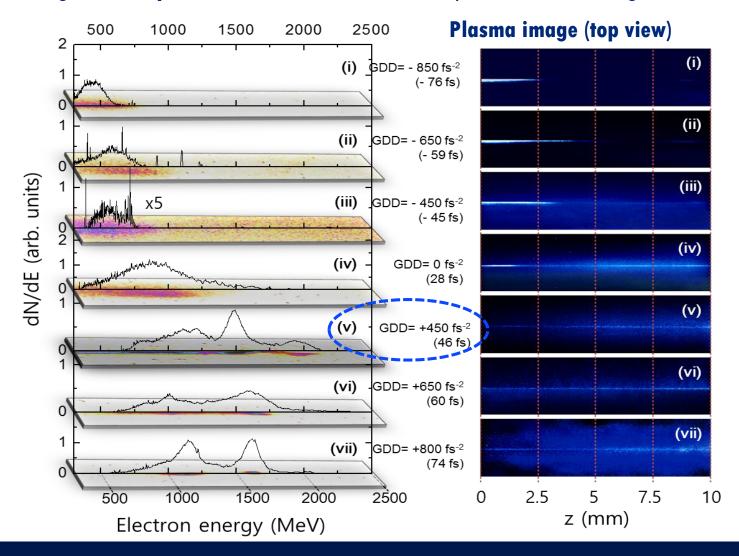






Control of spectral phase: GDD

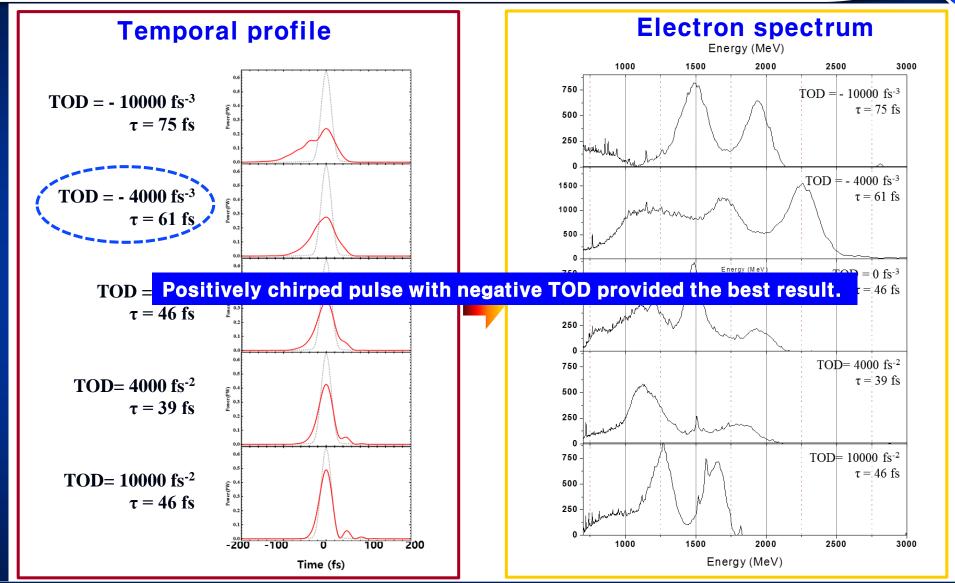
26 J on target, focal spot \sim 35 micron, Ne \sim 1.4x10¹⁸ /cc, 10 mm cell length







Control of spectral phase: GDD+TOD

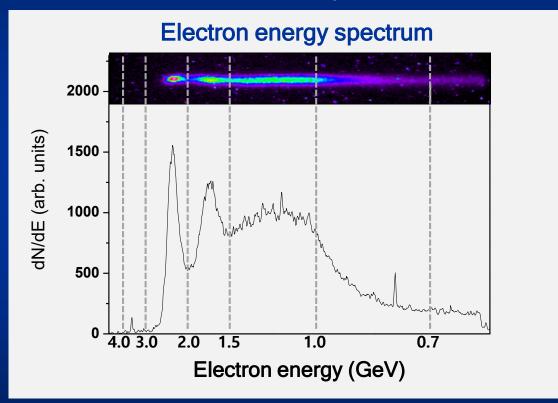




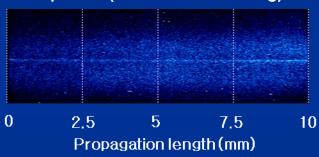


Electrons over 2 GeV from a 10-mm gas cell

Gas cell length = 10 mm Positively chirped 61 fs Intensity = $2x10^{19}$ W/cm² (a₀=3)



Top view (Thomson scattering)



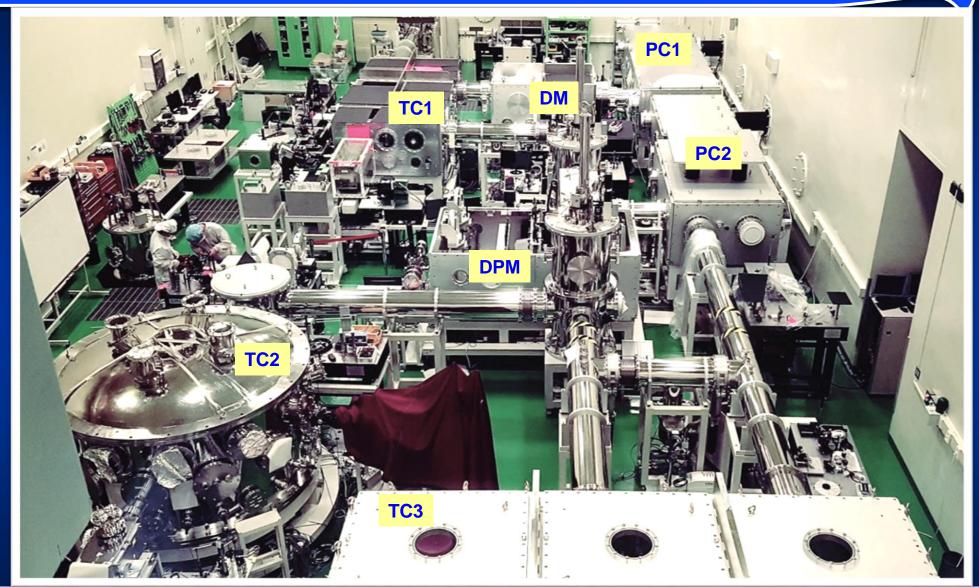
Smooth propagation over the whole medium length of 10 mm

E_e > 2 GeV after GDD and TOD control





PW Laser Experimental Area







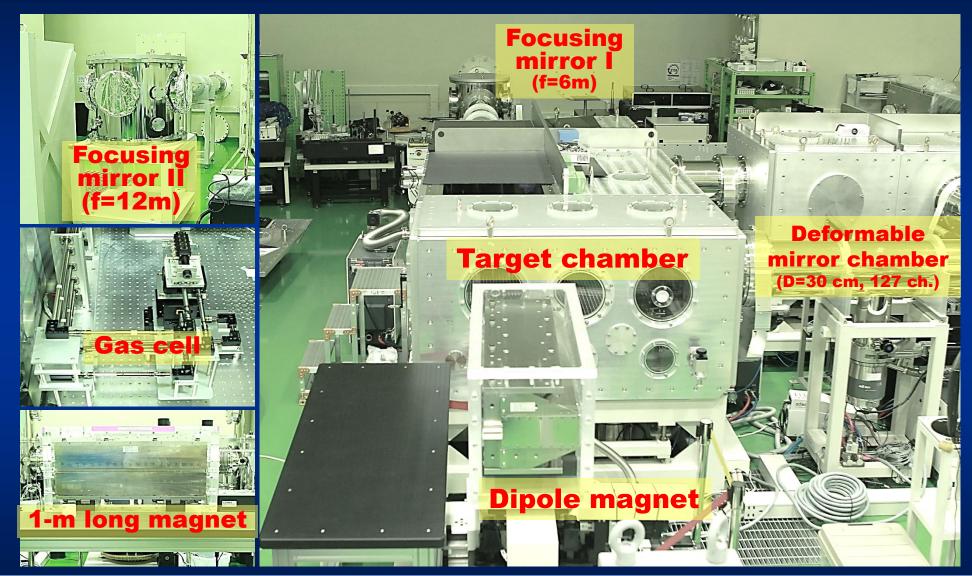
PW Laser Experimental Area (2018)







Target chamber for LWFA with 4 PW laser



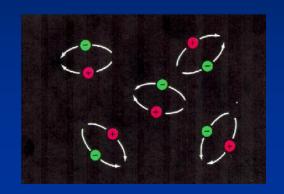




Pair production from vacuum

Vacuum fluctuations (quantum vacuum)

Creation and annihilation of electron-positron pairs occurs continually in quantum vacuum.



$$\delta E = mc^{2}$$

$$\rightarrow \delta t = \hbar/mc^{2}$$

$$\rightarrow \delta x = c\delta t = \hbar/mc = \overline{\lambda}_{C}$$



Schwinger field (E_S) for nonlinear optics in vacuum

Field-driven pair production over $\bar{\lambda}_{\mathcal{C}}$ in vacuum

$$eE_S\bar{\lambda}_C=m_ec^2$$
 where $\bar{\lambda}_C=\frac{\hbar}{m_ec}=3.9\times 10^{-11}$ cm

$$E_S = \frac{m_e^2 c^3}{e\hbar} = 1.3 \times 10^{16} \text{ V/cm}$$
: Schwinger limit

 $I_S = 2 \times 10^{29} \, \mathrm{W/cm^2}$: the corresponding laser intensity



Strong Field Quantum Electrodynamics (QED)

quantum electrodynamics (QED): relativistic quantum field theory of electrodynamics (quantum mechanics + special relativity)

QED: anomalous magnetic moment of electron Lamb shift of the energy levels of hydrogen (${}^2S_{1/2}$ and ${}^2P_{1/2}$)

$\chi_{\rm e}$: quantum nonlinearity parameter for strong-field QED

Field-driven pair production over $\bar{\lambda}_C$ with field $(F_{\mu\nu})$ and electron (p_{μ})

$$\chi_e = \frac{1}{m_e c^2} \frac{\bar{\lambda}_C}{c} \sqrt{\left(\frac{e}{m_e} F_{\mu\nu} p^{\nu}\right)^2} = \frac{E_{\text{proper}}}{E_S}$$

 $\Rightarrow 2\gamma E/E_{\rm S}$ for a counterpropagating relativistic electron

Pair production when $\chi_e \gtrsim 1$, For a rest electron, $I \sim I_S = 2 \times 10^{29} \, \text{W/cm}^2 \, \text{for} \, \chi_e = 1$ For a 2.5-GeV electron, $I \sim 10^{-8} I_S = 2 \times 10^{21} \, \text{W/cm}^2 \, \text{for} \, \chi_e = 1$

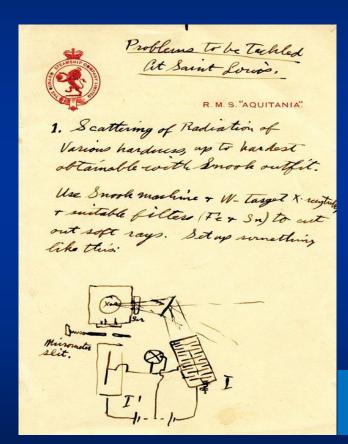


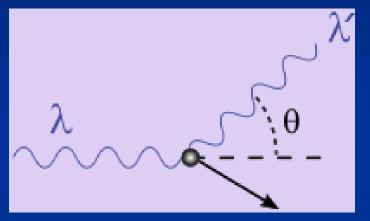


Compton scattering

Compton scattering:

the scattering of an x-ray or gamma-ray photon with an electron, resulting in a decrease in energy (increase in wavelength) of the photon





A. H. Compton, Phys. Rev. **21**, 483 (1923). (x-ray source: Mo K_a at 17 keV)

$$\lambda' - \lambda = \frac{h}{mc} (1 - \cos \theta),$$
or $E_{\gamma'} = \frac{E_{\gamma}}{1 + \frac{E_{\gamma}}{mc^2} (1 - \cos \theta)},$
with $E_{\gamma} = \frac{hc}{\lambda}$

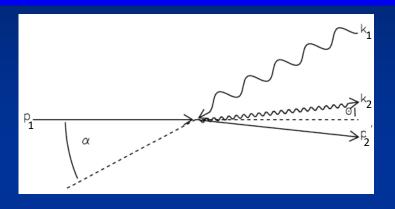
Problems to be tacked at Washington Univ in St. Louis (memorandum written in his return journey to US from Cambridge in 1920)



Compton scattering bet. an ultra-relativistic electron & a photon

Inverse Compton scattering (Compton back-scattering):

a high-energy charged particle transfers part of its energy to a photon, resulting in an increase in energy (decrease in wavelength) of the photon.



Energy – momentum conservation,
$$p_1^{\mu} + k_1^{\mu} = p_2^{\mu} + k_2^{\mu}$$
 (1)

$$p^{\mu} = (E/c, \vec{p}) = (\gamma mc, \gamma m\vec{v}); k^{\mu} = (\hbar \omega/c, \hbar \vec{k})$$

$$(p_{1}^{\mu} + k_{1}^{\mu})(p_{1\mu} + k_{1\mu}) = (p_{2}^{\mu} + k_{2}^{\mu})(p_{2\mu} + k_{2\mu}) \rightarrow p_{1}^{\mu} k_{1\mu} = p_{2}^{\mu} k_{2\mu}$$

$$p^{\mu}p_{\mu} = \gamma^{2}m^{2}c^{2} - \gamma^{2}m^{2}v^{2} = m^{2}c^{2}; k^{\mu}k_{\mu} = 0$$

$$k_{2\mu} \times (1), \quad k_{2\mu}(p_1^{\mu} + k_1^{\mu}) = k_{2\mu}(p_2^{\mu} + k_2^{\mu}) = k_{2\mu}p_2^{\mu} = p_1^{\mu}k_{1\mu}$$

$$A_{\mu}B^{\mu} = A_0B_0 - \vec{A} \cdot \vec{B}, \quad E_i = \hbar\omega_0 = \hbar c k_1; \ E_f = \hbar\omega_2 = \hbar c k_2$$

$$\gamma m E_f(1 - \beta \cos \theta) + \frac{1}{c^2} E_i E_f \{ 1 + \cos(\alpha - \theta) \} = \gamma m E_i (1 + \beta \cos \alpha)$$

Energy of scattered photon

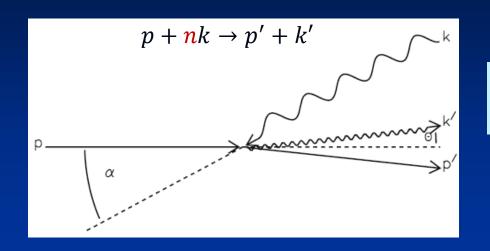
$$\Rightarrow E_f = \frac{\gamma mc^2 (1 + \beta \cos \alpha)}{\gamma mc^2 (1 - \beta \cos \theta) + E_i \{1 + \cos(\alpha - \theta)\}} E_i = \frac{1 + \beta \cos \alpha}{1 - \beta \cos \theta + \frac{E_i}{\gamma mc^2} \{1 + \cos(\alpha - \theta)\}} E_i$$

For for
$$\beta \approx 1$$
, $\theta \approx 0$, $E_f = \frac{1 + \cos \alpha}{1 - \beta + \frac{E_i}{\gamma mc^2} (1 + \cos \alpha)} E_i \longrightarrow E_f = 2\gamma^2 (1 + \cos \alpha) E_i$





Nonlinear Compton scattering in a strong EM field



Energy-momentum conservation under a background EM field

$$p^{\mu} + \frac{a_0^2 m^2 c^2}{4k_{\nu}p^{\nu}}k^{\mu} + nk^{\mu} = p'^{\mu} + \frac{a_0^2 m^2 c^2}{4k_{\nu}p'^{\nu}}k^{\mu} + k'^{\mu}$$

EM-field-dressed momentum

classical nonlinearity parameter:
$$a_0 = \frac{eE_0}{m\omega c} = \frac{eA_0}{mc^2}$$

Energy of the scattered photon

$$\varepsilon_{\gamma'} = \hbar \omega' = \hbar c k' = \frac{n \gamma^2 (1 + \beta \cos \alpha)}{\gamma^2 (1 - \beta \cos \theta) + \left[\frac{n \gamma \varepsilon_L}{m c^2} + \frac{a_0^2 / 4}{1 + \beta \cos \alpha} \right] [1 + \cos(\theta - \alpha)]} \varepsilon_L$$

$$(\varepsilon_L = \hbar \omega_0)$$

For
$$\beta \approx 1, \theta \approx 0$$
,
$$\varepsilon_{\gamma \prime} = \frac{2n\gamma^2(1+\cos\alpha)}{1+\frac{a_0^2}{2}+\frac{2n\gamma\varepsilon_L}{m_ec^2}(1+\cos\alpha)}\varepsilon_L$$

Bamber et al., PRD 60, 092004 (1999); Melissinos, Strong Field Laser Physics, 497 (2008)





Strong field QED: All-optical Compton scattering

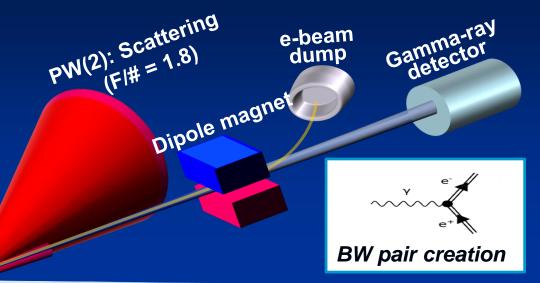
Linear Compton scattering

- $\blacktriangleright \omega'_{\text{max}} \approx 4 \gamma^2 \omega_0$
 - 100 MeV with 2 GeV e-beam
 - 2.5 GeV with 10 GeV e-beam

Nonlinear Compton scattering

 $\blacktriangleright \omega'_{\text{max}} \approx 4 \text{ n } \gamma^2 \omega_0 / (1 + a_0^2 / 2)$

He gas cell

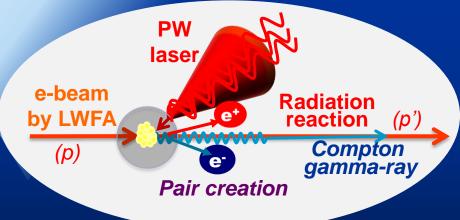




Parameters that control NLQED processes:

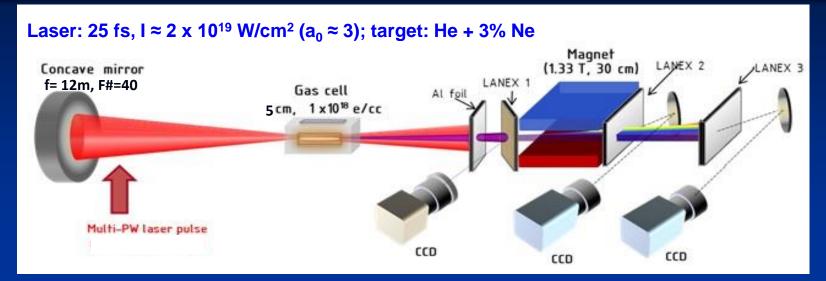
$$\chi_e = 2\gamma E/E_S \approx 0.3 \frac{\mathcal{E}}{GeV} \sqrt{\frac{I}{10^{21} \text{W/cm}^2}}$$

$$\chi_{\gamma} \approx \frac{\hbar \omega}{m_e c^2} \frac{E}{E_s}$$

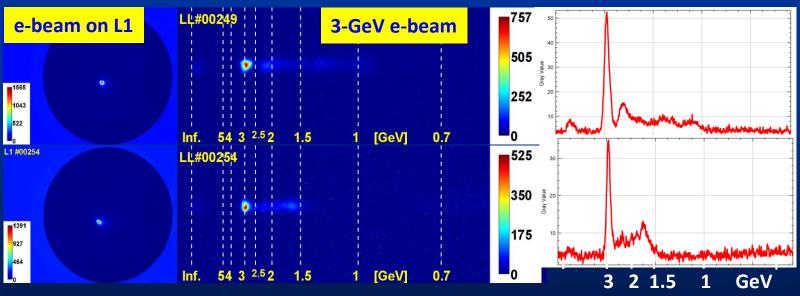




Generation of Multi-GeV Electron Beams



- linear pol. @800 nm, 25 fs
- Gas cell with He +3%Ne
- Focusing with f=12m (f/# = 43)

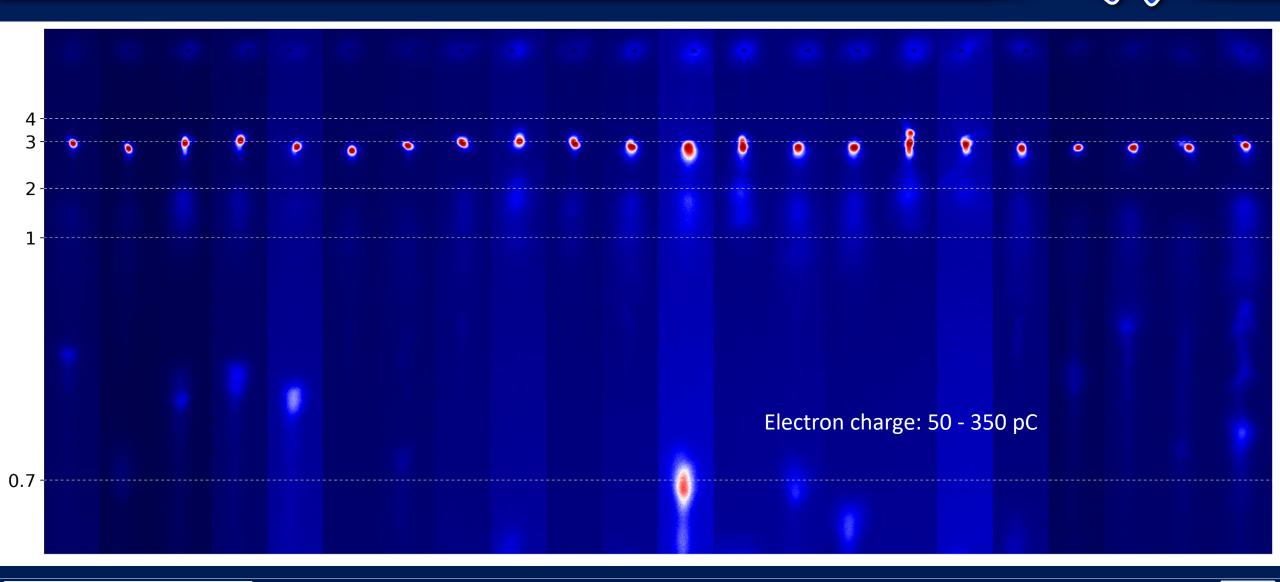


Low divergence ~ 1mrad Low Energy Spread <2% 100-200 shots per day Charge: up to 350 pC Energy: up to 3.5 GeV





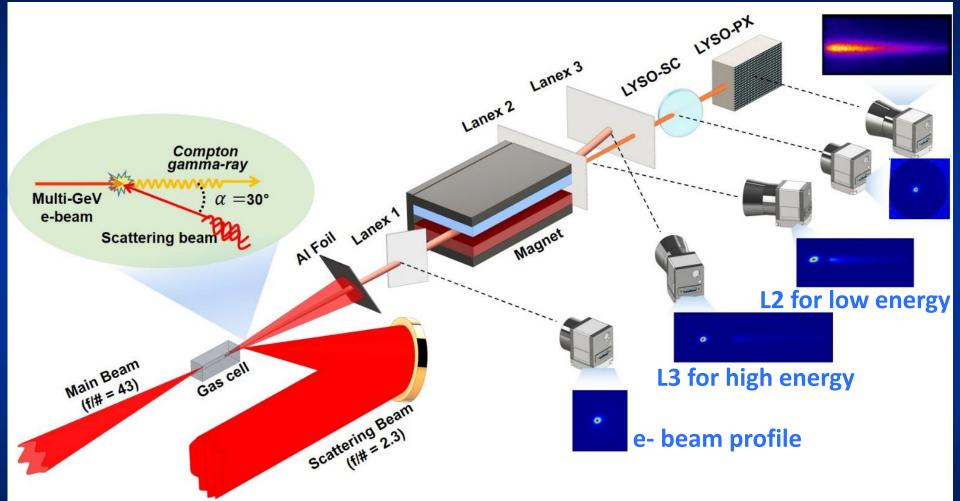
Reproducible monochromatic electron beam







All Optical Nonlinear Compton Scattering Experiment



Pixelated LYSO for γ-ray energy spectrum

Single crystal LYSO for γ-ray beam profile

Main Beam

- 25 fs
- $I = 3x10^{19} \text{ W/cm}^2$
- Spot size: 45 μm

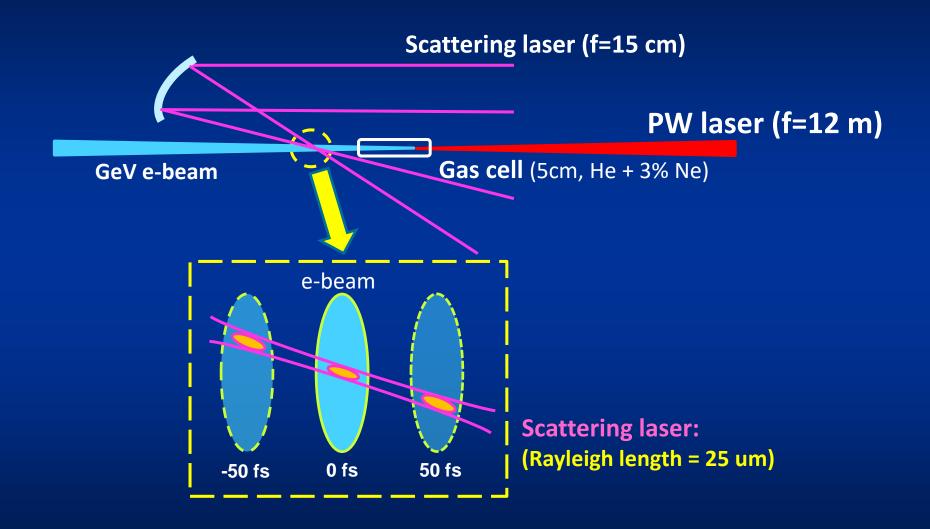
Scattering Beam

- 25 fs
- $I = 4x10^{20} \text{ W/cm}^2$
- Spot size: 2.5 μm
- $a_0 = 14$





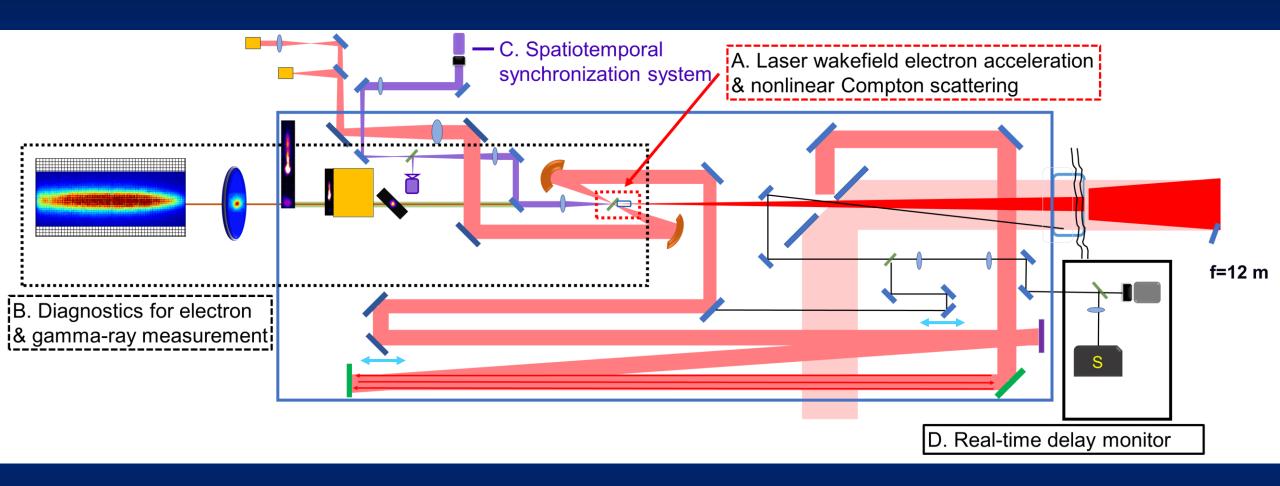
Geometry for nonlinear Compton scattering







Experimental Setup for Nonlinear Compton Scattering

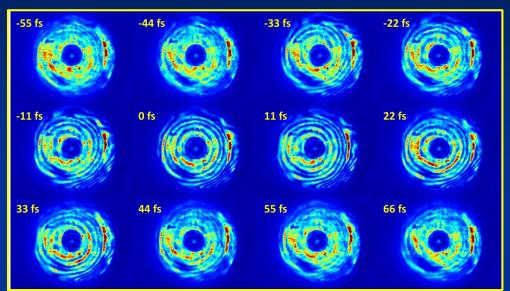


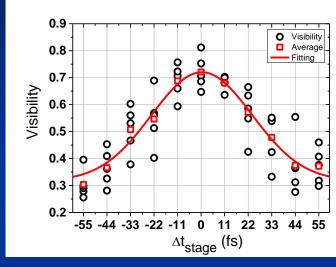


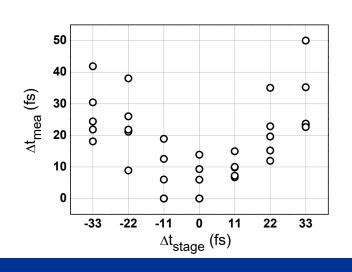


Temporal synchronization for Compton scattering

Spatial interferogram in the setup 1







- The visibility of interference varied with the time delay.
- The zero time delay was set where the visibility is the highest.

*** visibility,**
$$\eta' = \frac{I_{max} - I_{min}}{I_{max} + I_{min}}$$

$$\eta' = 0.40 \times \exp\left(-\frac{\Delta t^2}{2 \times 23.5^2}\right) + 0.32$$

$$|\Delta t_{mea}| = 2 \times 23.5^2 \times \ln \frac{0.40}{(\eta' - 0.32)} (fs)$$

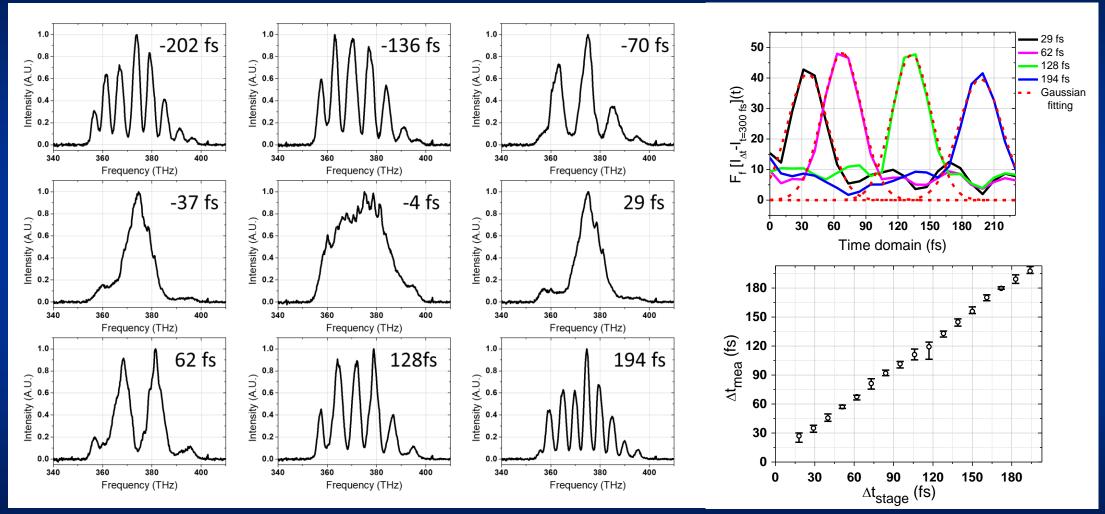
accuracy of time delay $\left(\frac{\sum_{i=1}^{n}(\Delta t_{mea}-\Delta t_{stage})_{i}^{2}}{n}\right)$: 11 fs





Temporal synchronization for Compton scattering (2)

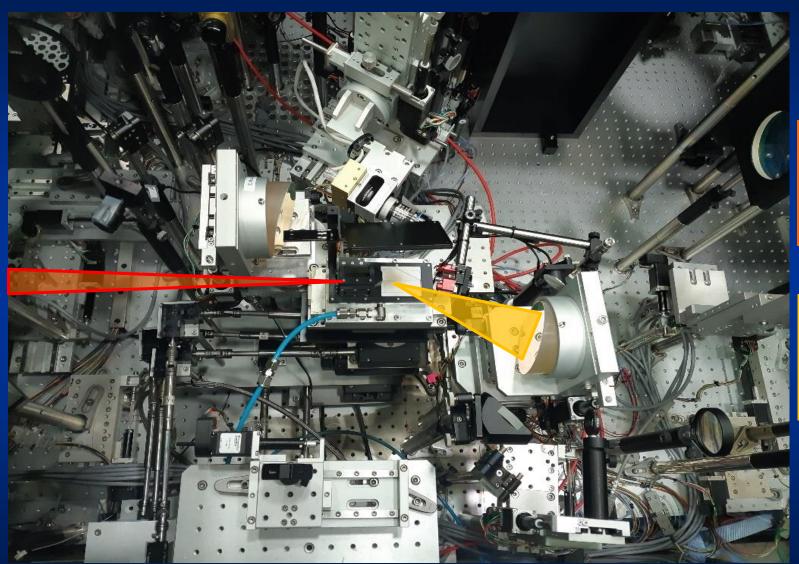
Real-time delay monitoring with a spectral interferometer in the setup 2



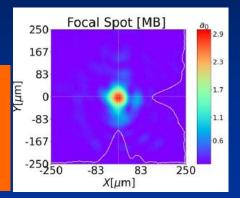




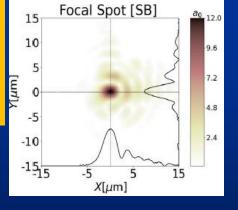
Experimental Chamber of Compton Scattering



Main beam τ = 25 fs I= 3×10^{19} W/cm² W₀ = 45 μ m



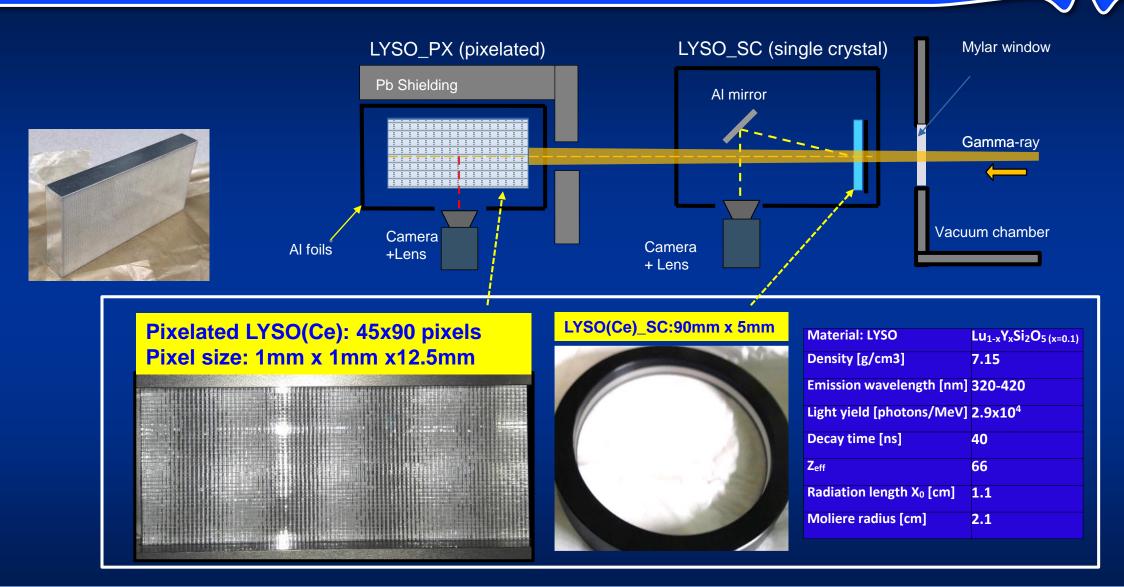
Scattering beam τ = 25 fs I= 4×10^{20} W/cm² W₀ = 2.5 μ m







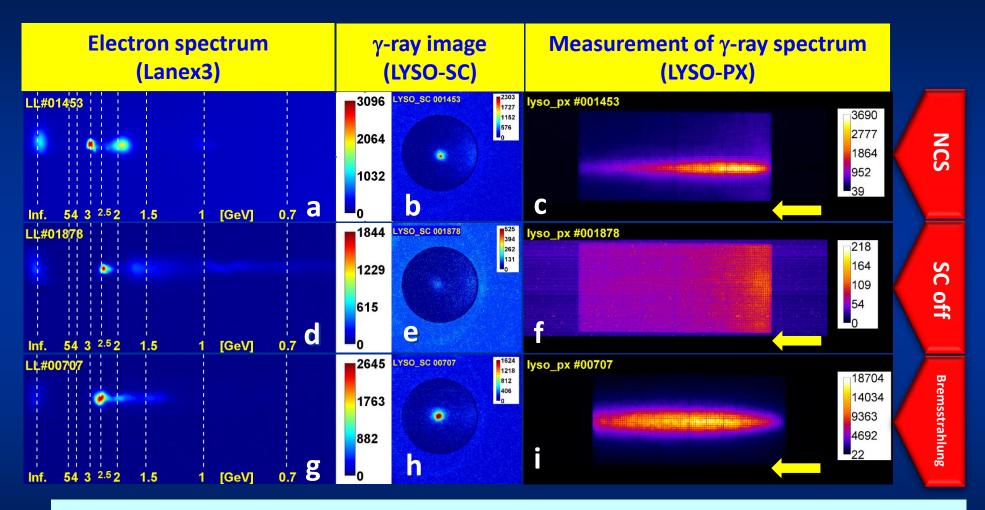
Diagnostics of Gamma-ray beam







Demonstration of nonlinear Compton scattering



Clear measurement of Compton scattering signal!





Reconstruction methods

Two methods were applied to reconstruct the gamma-ray spectra.

Simultaneous Iterative Reconstruction **Technique (SIRT)**

NO Functional form assumed for the spectrum, Originally for pair spectrometer, adapted for LYSO

$$g_j^{(k+1)} = g_j^{(k)} + \alpha \frac{\sum_{i} S_{ij} \times \left(\frac{r_i - \sum_{m} S_{im} \ g_m^{(k)}}{\sum_{m} S_{im}}\right)}{\sum_{m} S_{mj}}$$

- next iteration for the spectrum



lineout response (px i, energy #j);
 Computed in GEANT4



- summed lineout response for px. i, from experiment

Trial function-based minimization of the response error (TFM)

Parametrized by critical energy(E_c)

Functional form:
$$\frac{dN}{dE} = A \times E^{-2/3} \times e^{-\frac{E}{E_c}}$$

Minimizes the expression:

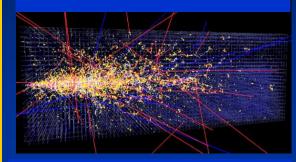
$$\min_{A,E_c} \left[r_i - \sum_j \left(S_{ij} \frac{dN(E_j)}{dE} dE_j \right) \right]$$

 S_{ii} : lineout response (px #i, energy #j); computed in GEANT4

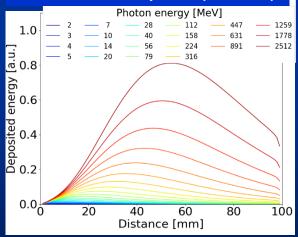
 r_i : lineout response for px i, from exp.

 E_i : energy #j

GEANT4 Simulation of LYSO



LYSO Lineout response (GEANT4)

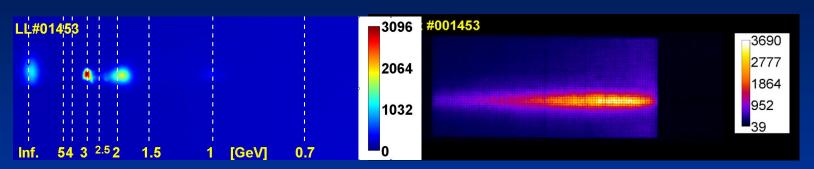


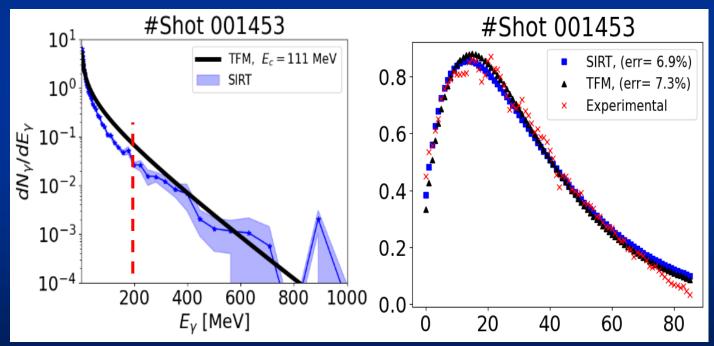
- D. Haden et al., Nucl. Inst. and Met. A 951, 163032 (2020)
- K. Behm et al., Review of Scientific Instruments 89, 113303 (2018)





Reconstruction of gamma-ray spectrum (2)





Linear Compton scattering:

$$\varepsilon_{\rm cutoff} = 2 (1 + \cos \theta) \gamma^2 \varepsilon_L$$
for E_e=3 GeV, $\varepsilon_{\rm cutoff} = 200$ MeV.

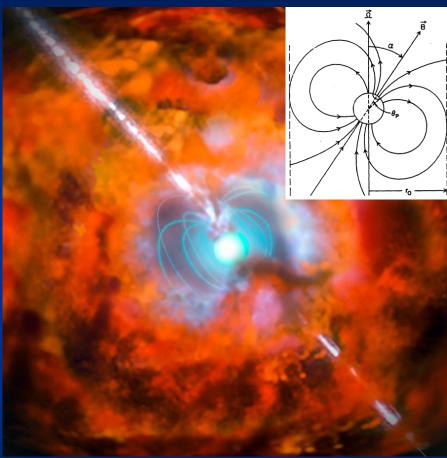
Nonlinear Compton scattering:

$$\varepsilon_{\gamma} = \frac{n}{1 + \frac{a_0^2}{2} + \frac{2n\gamma\varepsilon_L}{m_e c^2} (1 + \cos\theta)} \varepsilon_{\text{cutoff}}$$
or
$$n = \frac{\left(1 + \frac{a_0^2}{2}\right)}{\left(1 - \frac{\varepsilon\gamma}{2m_e c^2}\right)} \frac{\varepsilon_{\gamma}}{\varepsilon_{\text{cutoff}}}$$





Magnetar: Astrophysical QED lab

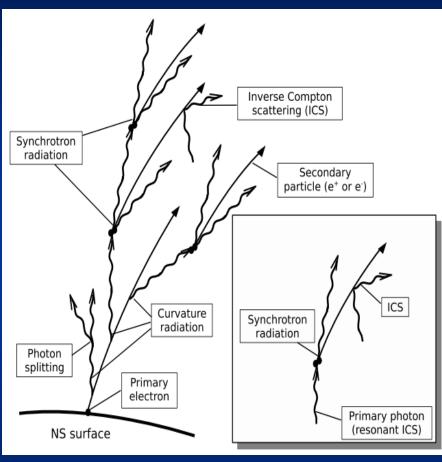


Gamma-ray burst and supernova powered by a magnetar: GRB 111209A/SN 2011 kl (eso 1527)

Magnetar

Extremely magnetized neutron star $B{\sim}50B_c~(B_c=4.4\times10^{13}~{\rm G})$ QED processes in the vicinity

- magnetic photon splitting $(\gamma + B \rightarrow \gamma \gamma)$
- magnetic pair creation $(\gamma + B \rightarrow e^+e^-)$
- inverse Compton scattering (resonant/non-resonant)
- → pair cascade
- $\rightarrow e^+e^-$ plasma
- vacuum birefringence
- → Astrophysical lab of strong-field QED



Medin and Lai, MNRAS 406, 1379 (2010)



Summary

- 1. Ultrahigh power CPA lasers have opened up new challenging research areas in strong field physics.
- 2. By applying the laser wakefield electron acceleration scheme, monoenergetic multi-GeV electron beams have been produced.
- 3. As part of strong field QED research, nonlinear Compton scattering (NCS) between a laser-driven GeV electron beam and an ultrahigh intensity laser pulse has been explored. The scattering of a multi-GeV electron with several hundred laser photons produced 100's MeV gamma-rays.
- 4. Strong field QED phenomena, such as radiation reaction and Breit-Wheeler pair production, will be also explored.

CoReLS website: https://corels_ibs.re.kr/html/corels_en/





