

Physics and applications of Laser Plasma Accelerators

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<https://www.weizmann.ac.il/complex/malka/home>

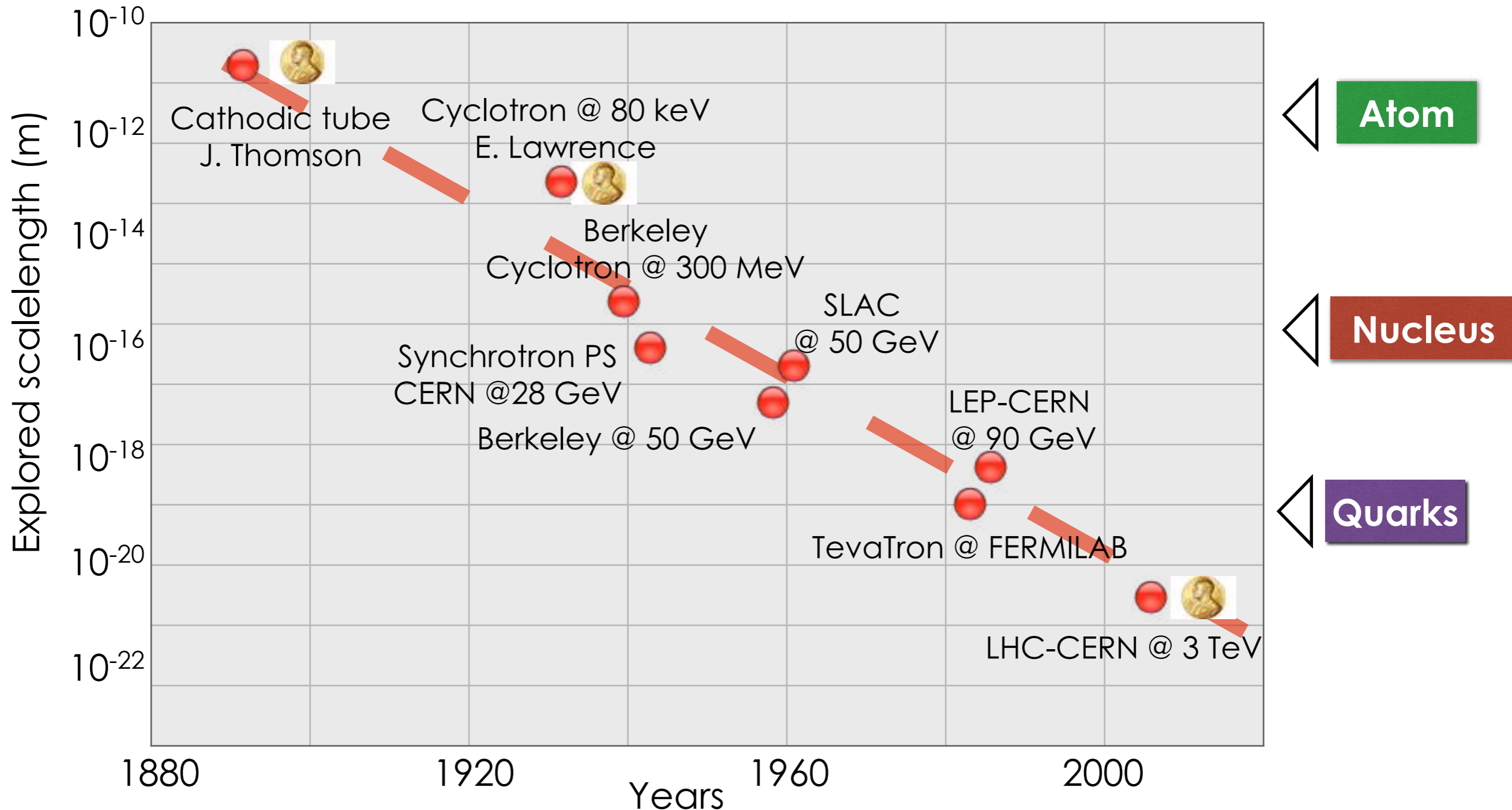
Outline

- Part I : Motivation, basis and principle
- Part II : External and Self-Injection in Laser Wakefield
- Part III : High quality electron beams in LPA with the colliding pulses scheme
- Part IV : Applications, conclusion and perspectives

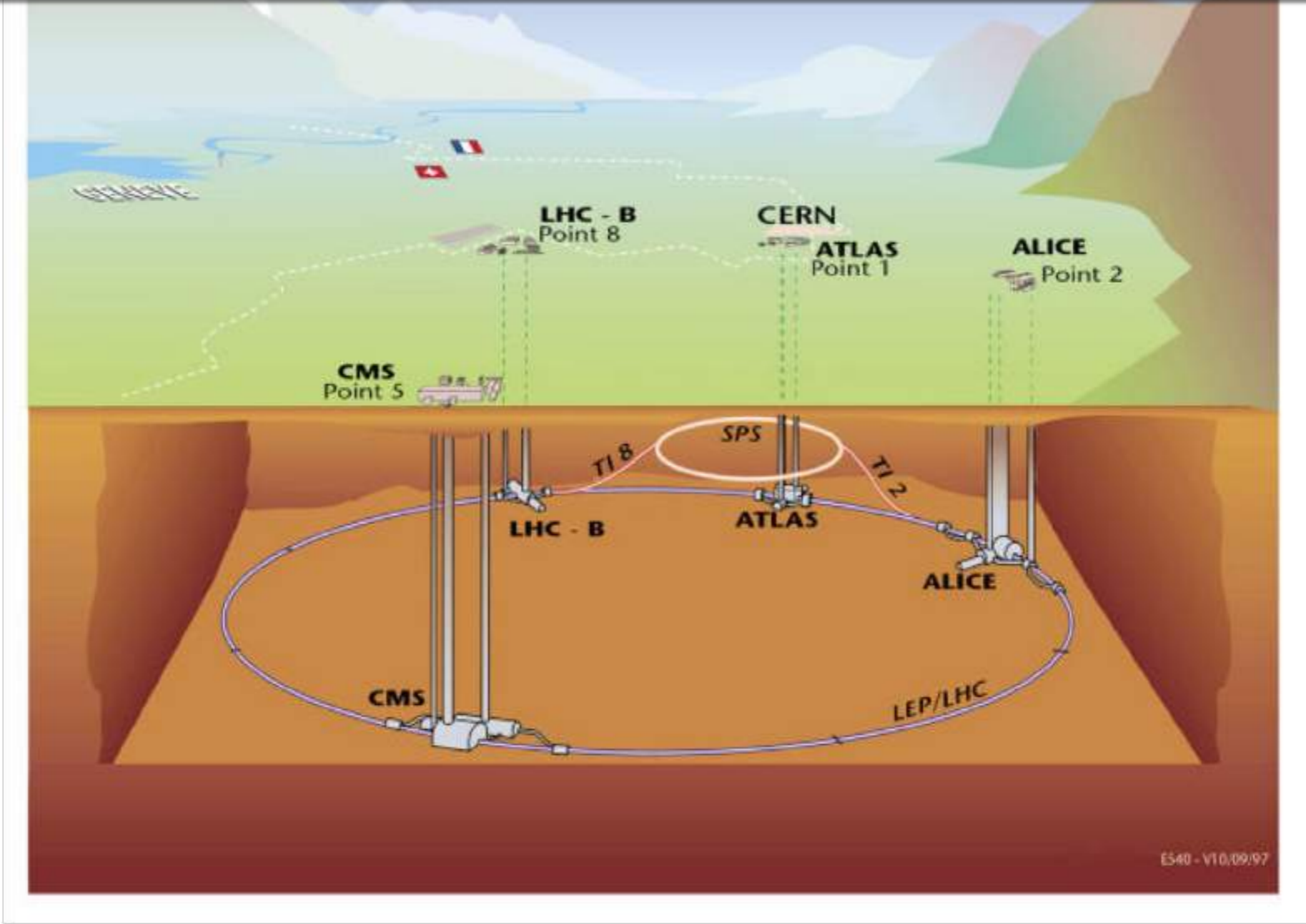
Part I : Motivation, basis and principle

- Introduction : context and motivations
- Electron in a laser field
- Laser driven plasma wave : theory
- Trapping Conditions

Accelerators: One century of exploration of the infinitively small



Overall view of LHC



9 km



Industrial Market for Accelerators

The development of state of the art accelerators for HEP has lead to :
research in other field of science (light source, spallation neutron sources...)
industrial accelerators (cancer therapy, ion implant., electron cutting &welding...)

Application	Total syst. (2007) approx.	System sold/yr	Sales/yr (M\$)	System price (M\$)
Cancer Therapy	9100	500	1800	2.0 - 5.0
Ion Implantation	9500	500	1400	1.5 - 2.5
Electron cutting and welding	4500	100	150	0.5 - 2.5
Electron beam and X rays irradiators	2000	75	130	0.2 - 8.0
Radio-isotope production (incl. PET)	550	50	70	1.0 - 30
Non destructive testing (incl. Security)	650	100	70	0.3 - 2.0
Ion beam analysis (incl. AMS)	200	25	30	0.4 - 1.5
Neutron generators (incl. sealed tubes)	1000	50	30	0.1 - 3.0
Total	27500	1400	3680	

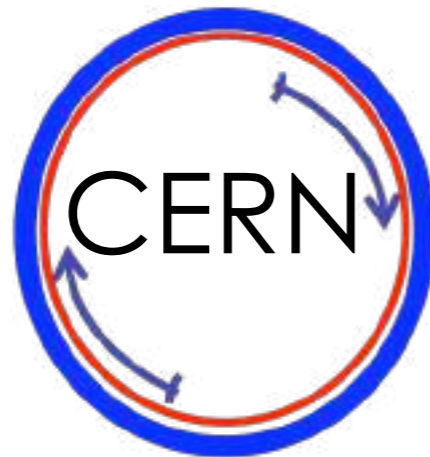
Plasma Accelerators : motivations



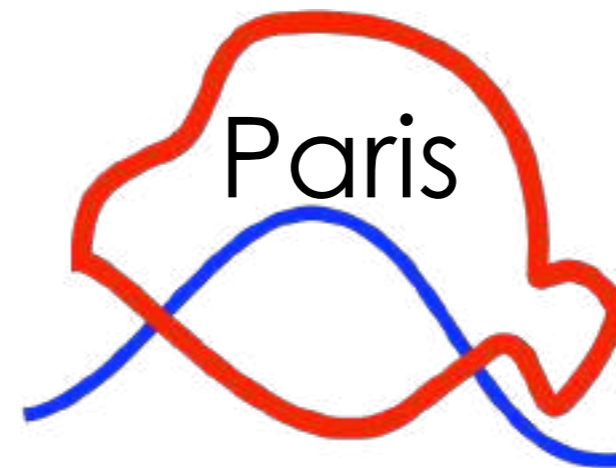
$E\text{-field}_{\max} \approx \text{few } 10 \text{ MeV /meter (Breakdown)}$
 $R > R_{\min}$ Synchrotron radiation

→ Energy ↗ → Length ↗ → Cost ↗

LHC
27 km



≈



Circle road
34 km

→ New medium : the plasma

Compactness of Laser Plasma Accelerators

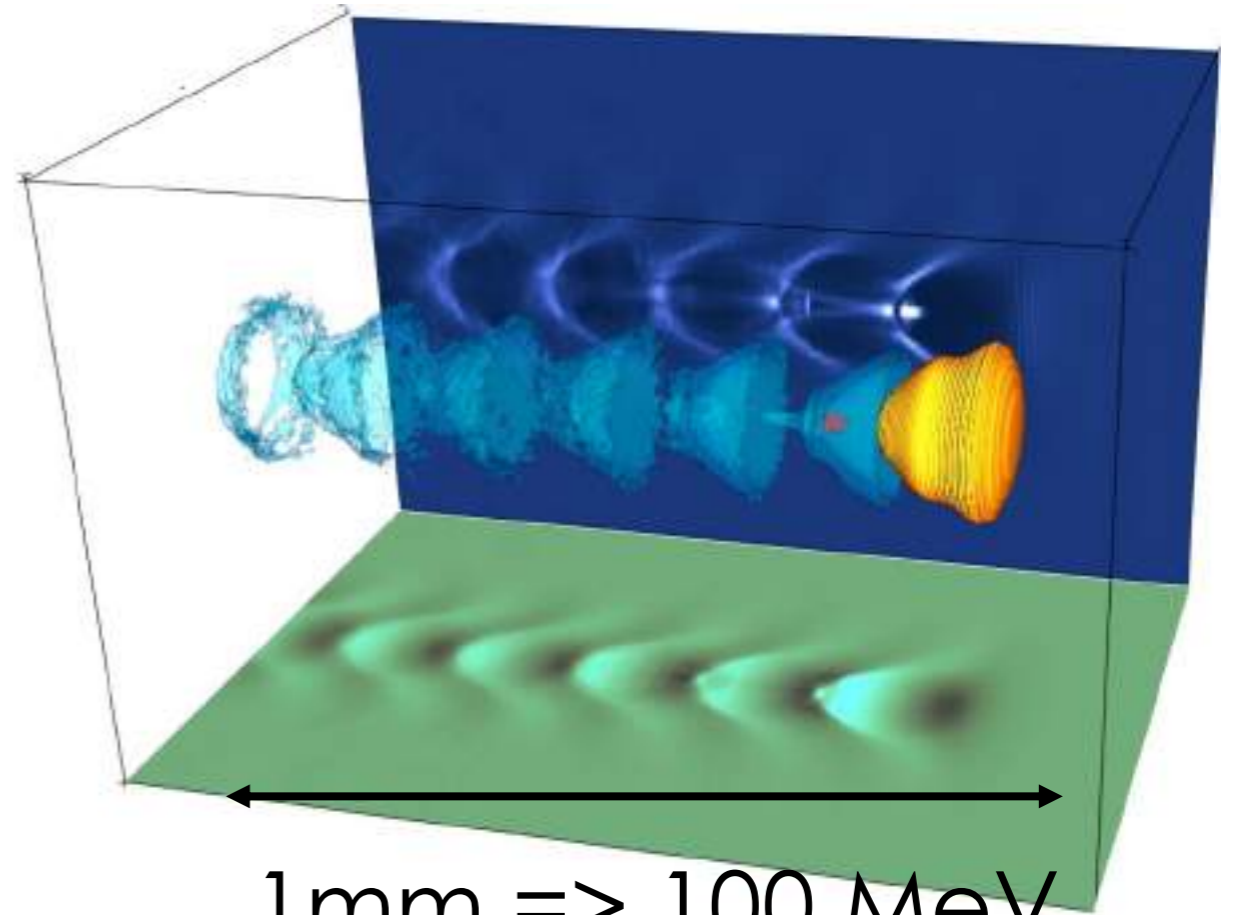


RF Cavity



1 m => 50 MeV Gain

Plasma Cavity



1 mm => 100 MeV

Electric field < 100 MV/m

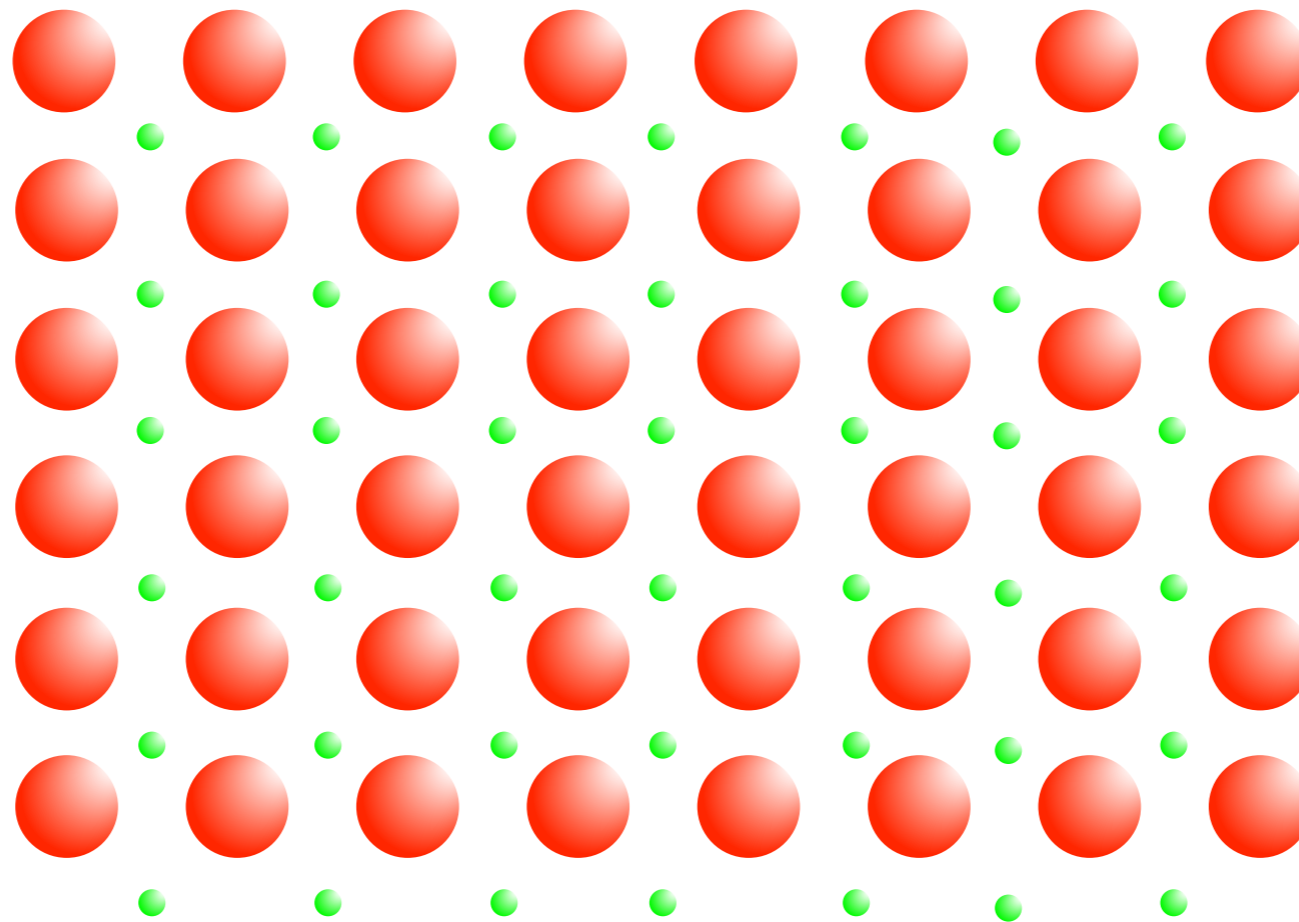
Electric field > 100 GV/m

V. Malka et al., Science **298**, 1596 (2002)

Why is a plasma useful ?



Plasma is an Ionized Medium \Rightarrow High Electric Fields

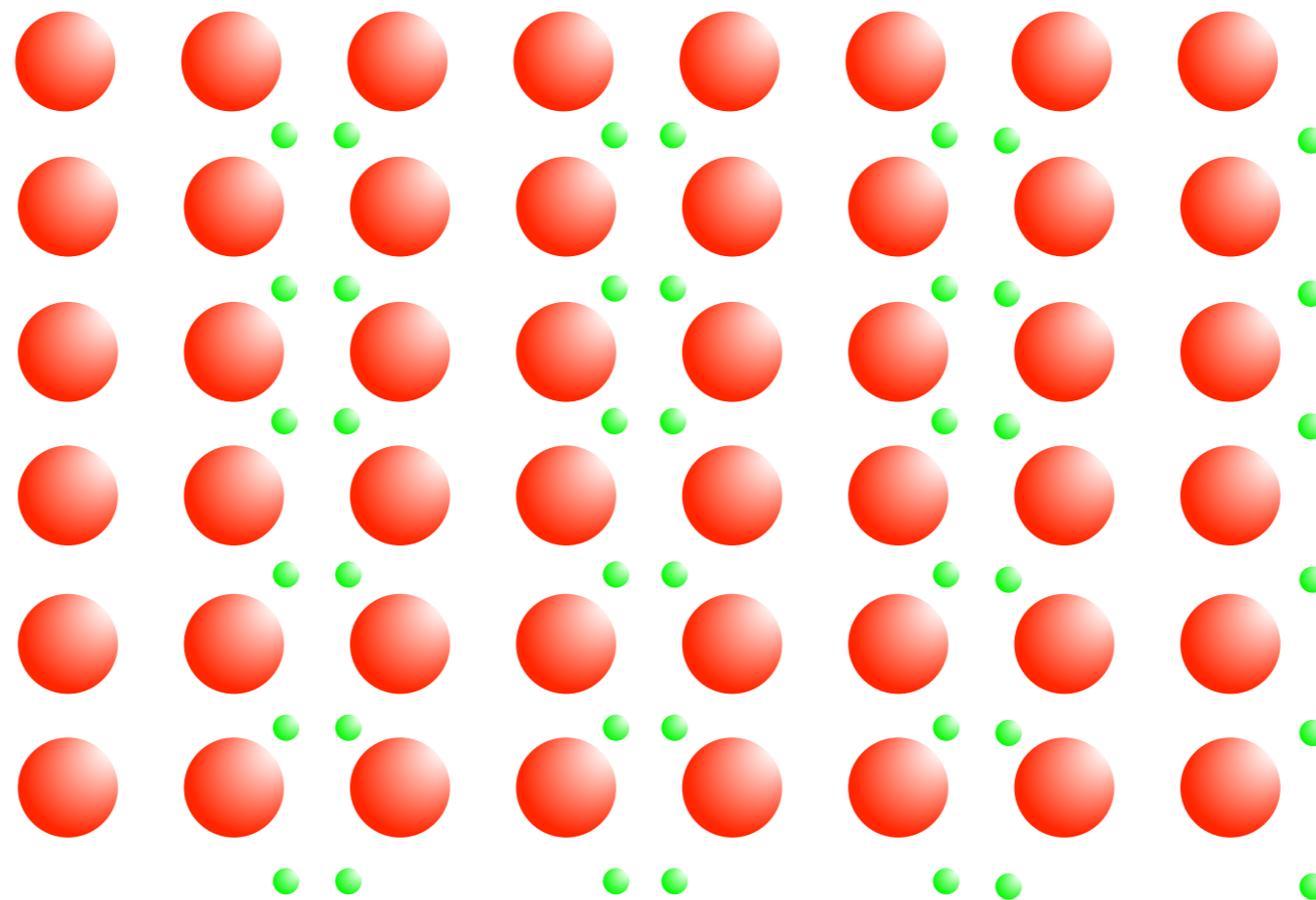


electrons plasma oscillation

Why is a plasma useful ?



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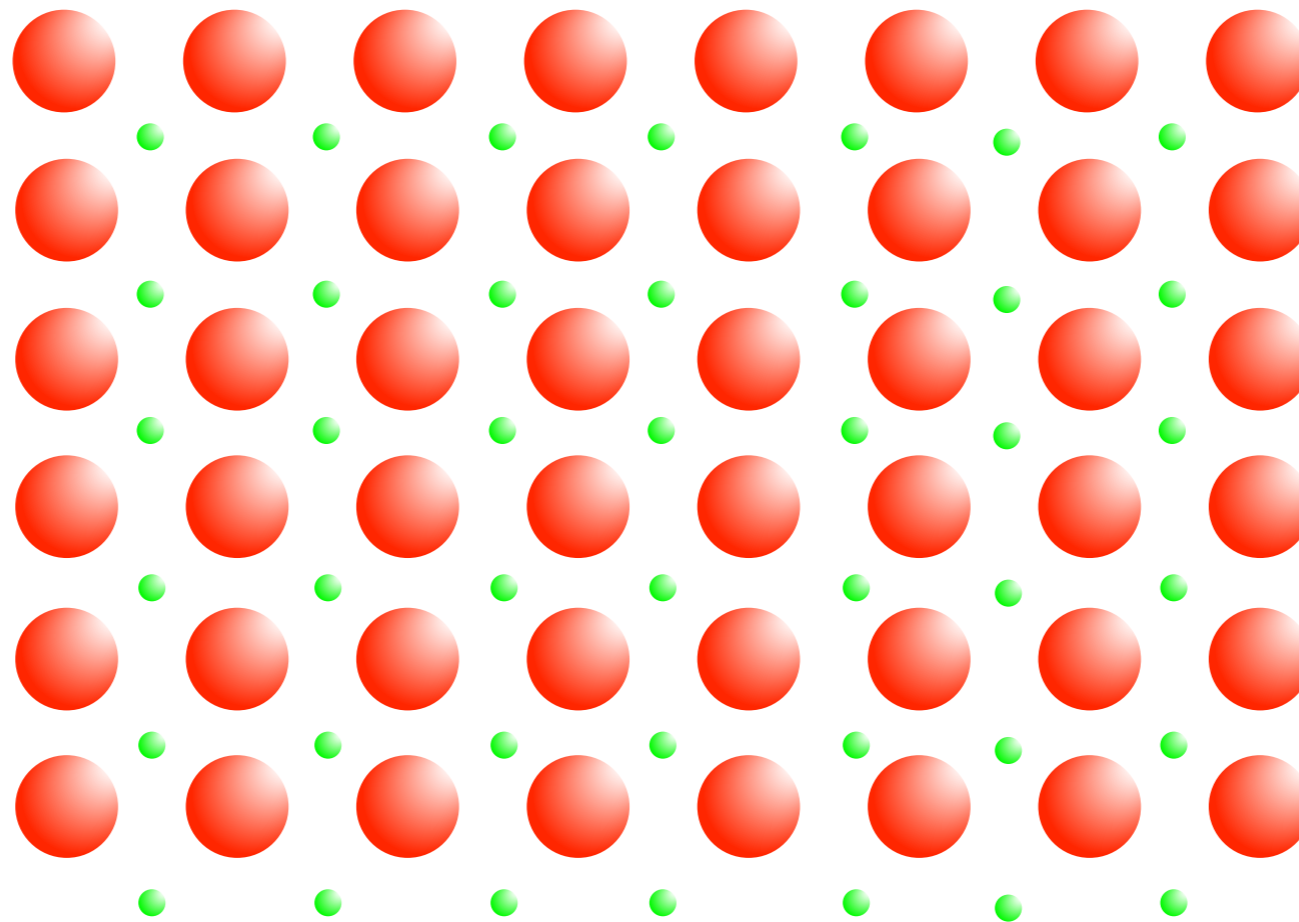


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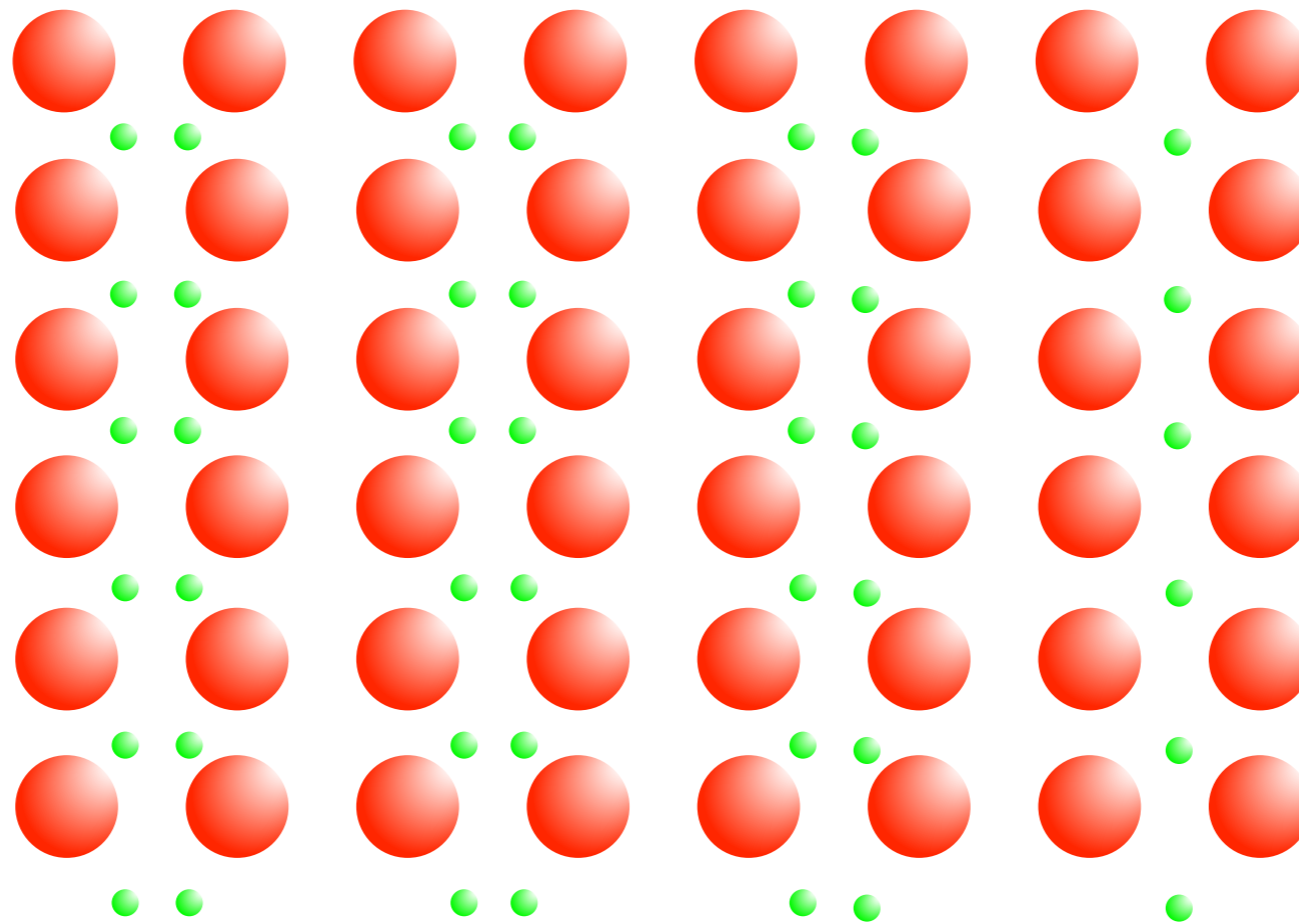


electrons plasma oscillation

Why is a plasma useful ?



Plasma is an Ionized Medium \Rightarrow High Electric Fields

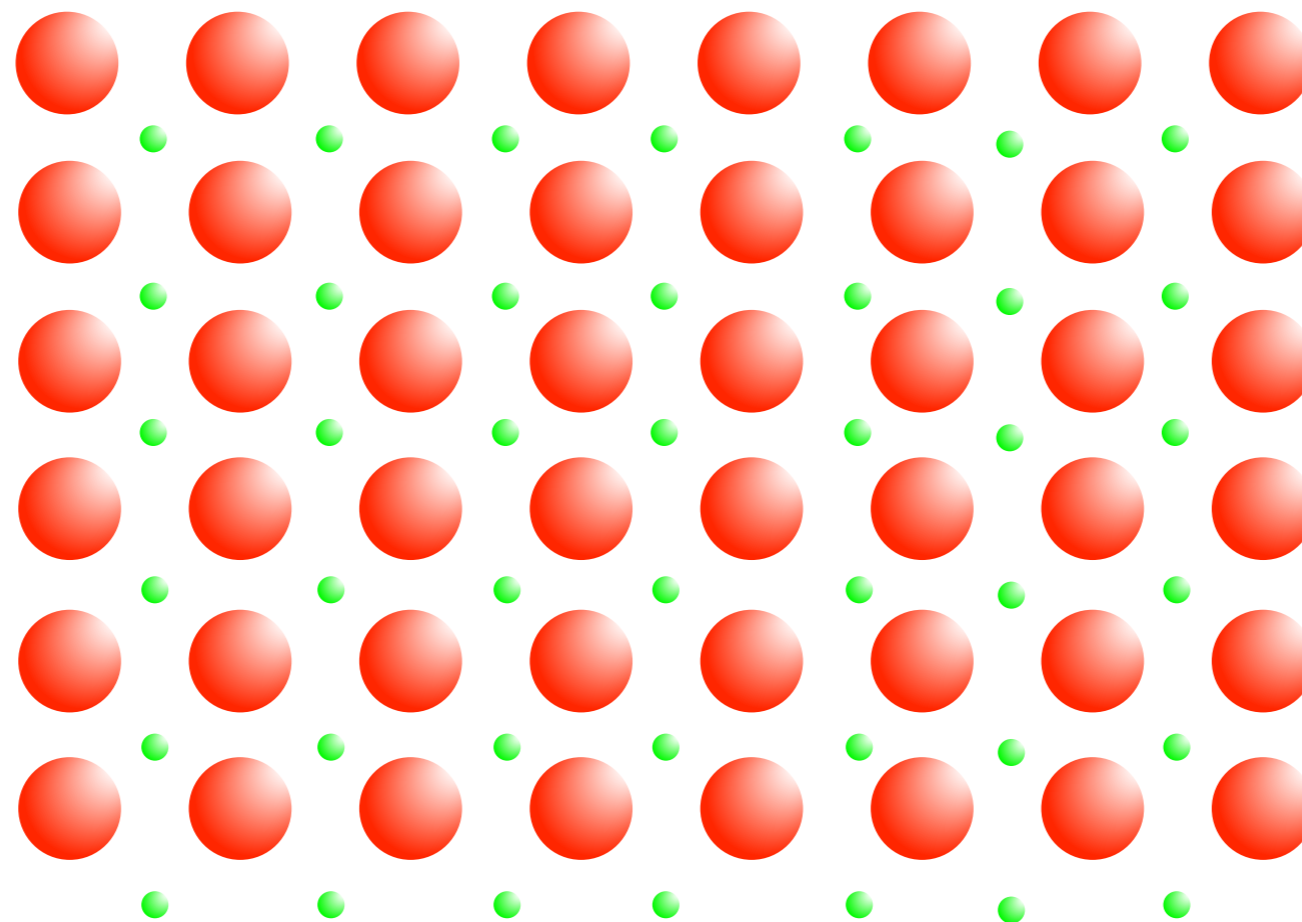


electrons plasma oscillation

Why is a plasma useful ?



Plasma is an Ionized Medium \Rightarrow High Electric Fields

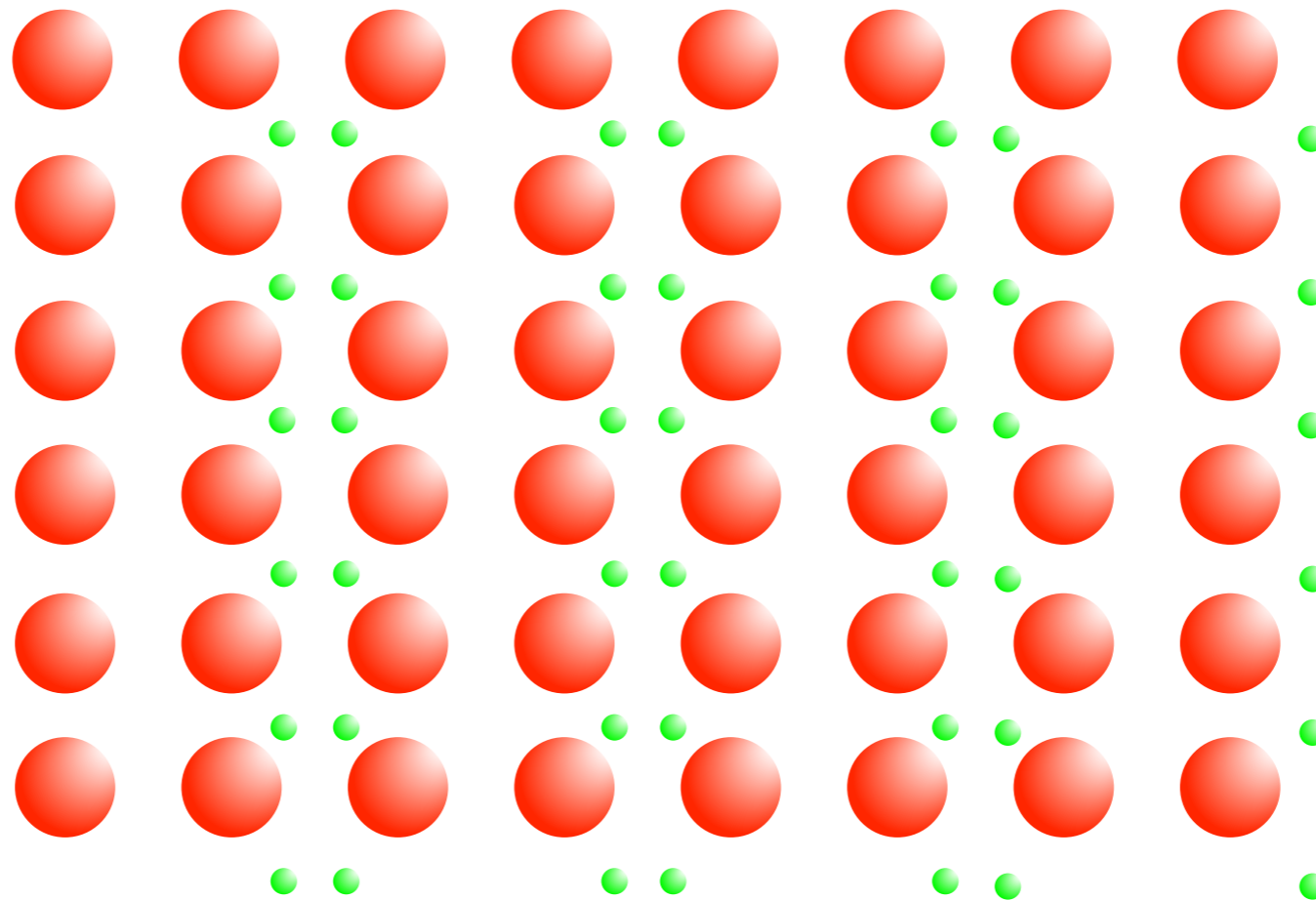


electrons plasma oscillation

Why is a plasma useful ?



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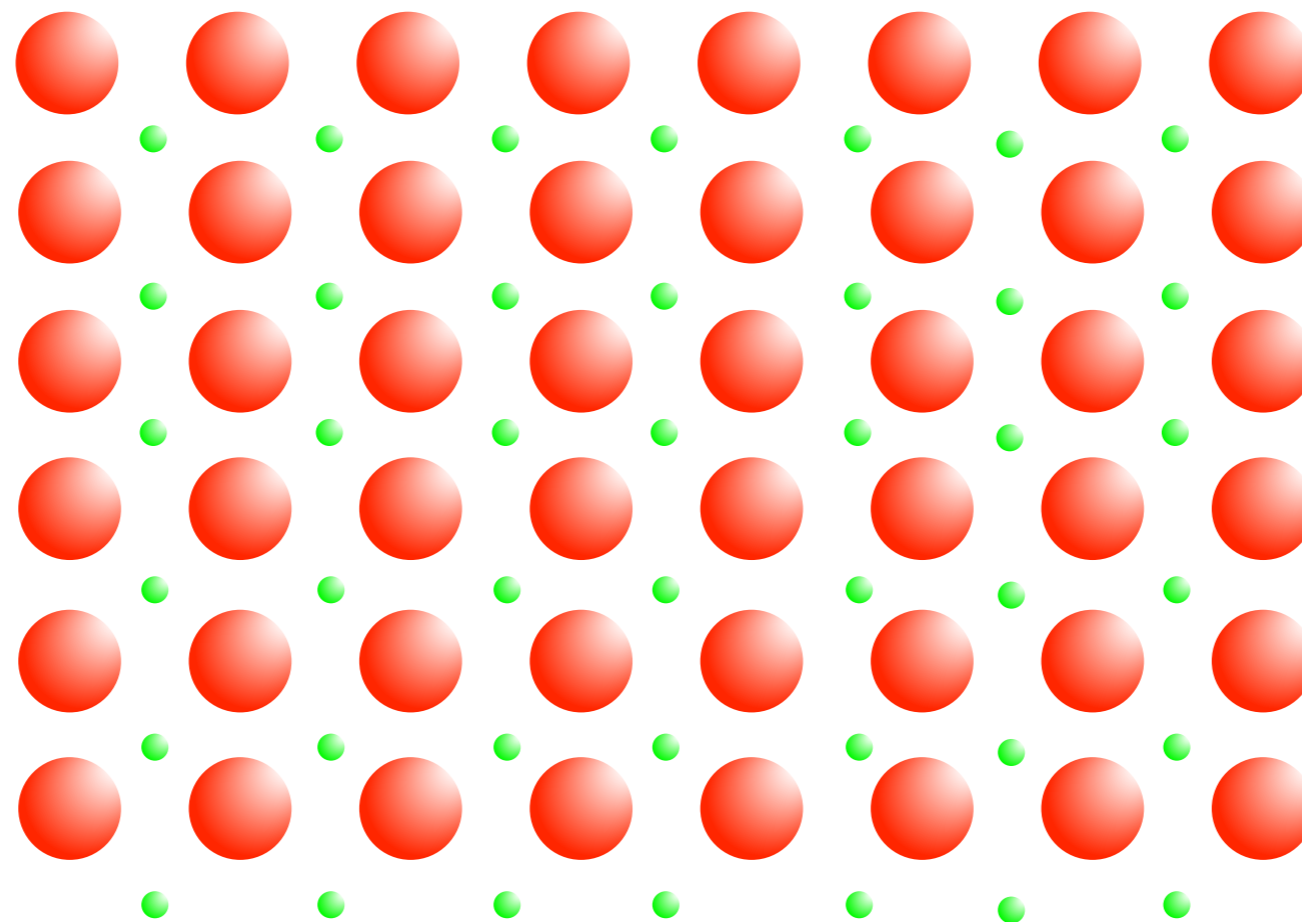


electrons plasma oscillation

Why is a plasma useful ?



Plasma is an Ionized Medium => High Electric Fields



electrons plasma oscillation

The electron plasma frequency : ω_p

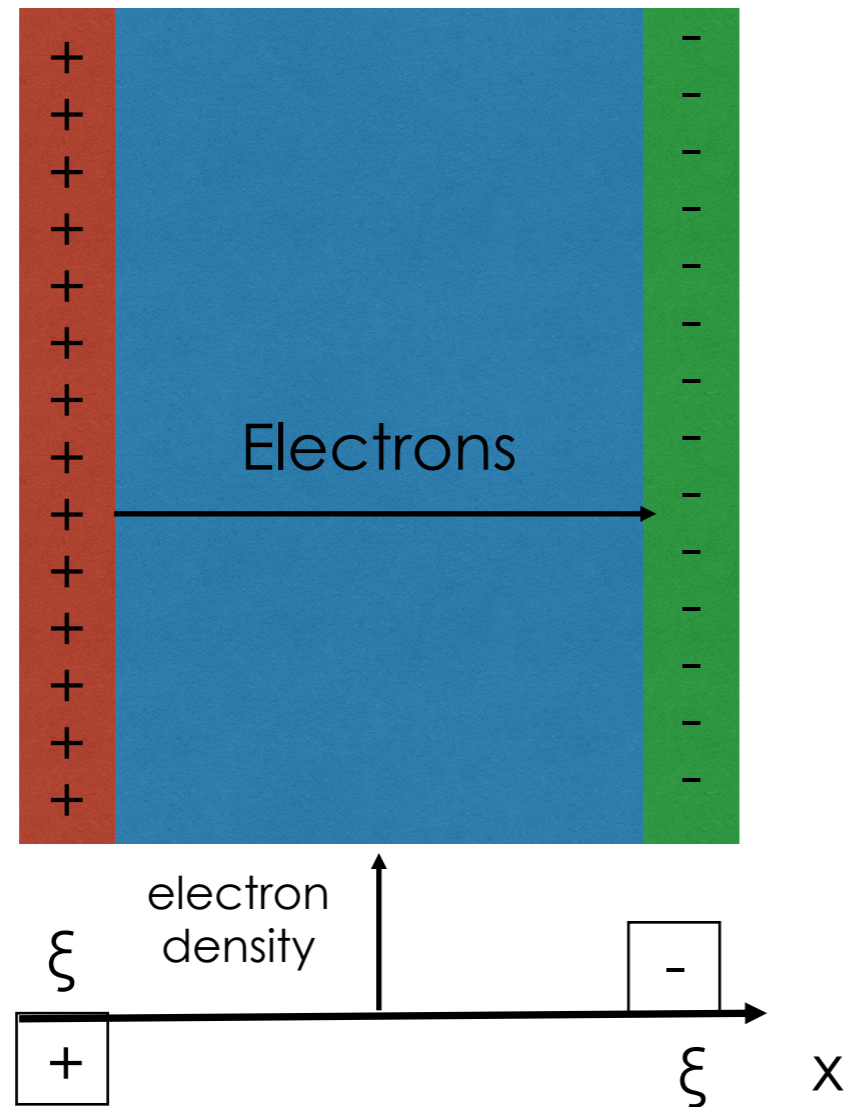


Neutral
plasma
 $Zn_e = n_i$



x

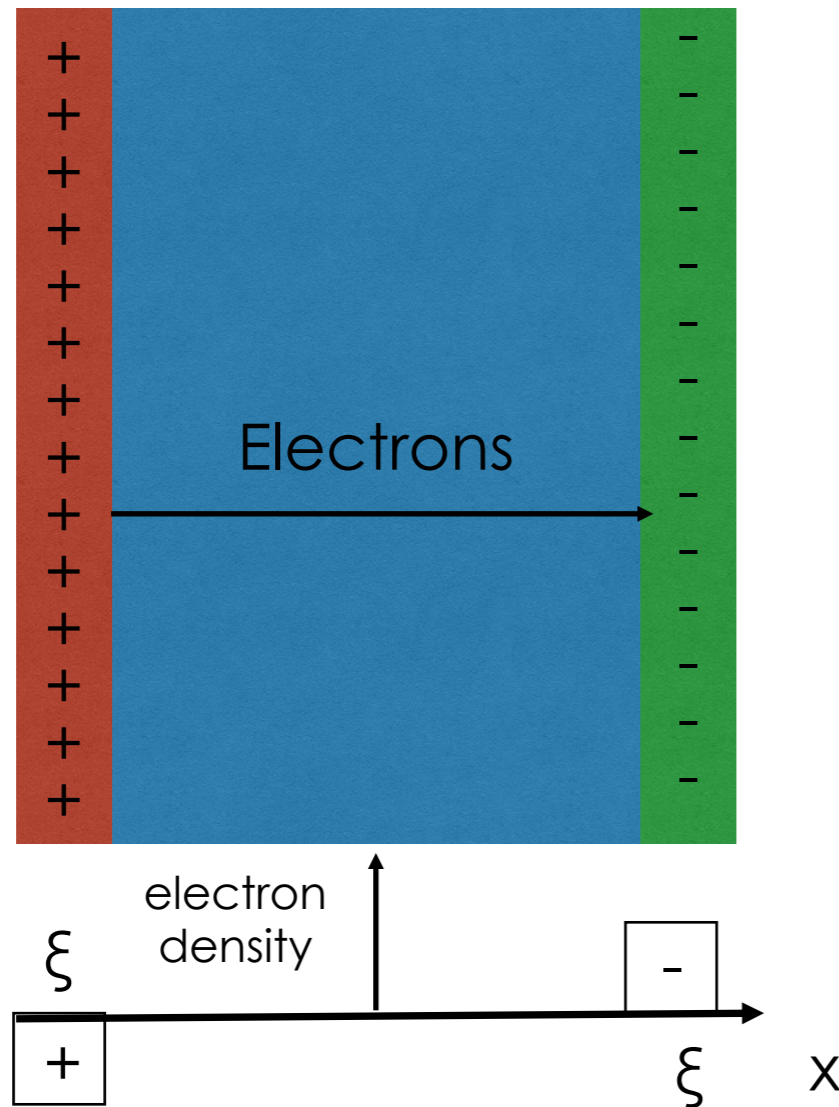
The electron plasma frequency : ω_p



$$E = \sigma/\epsilon_0 = n_e \xi e / \epsilon_0$$

$$F = qE$$

The electron plasma frequency : ω_p



$$E = \sigma/\epsilon_0 = n_e \xi e / \epsilon_0$$

$$F = qE$$

$$m_e d\xi^2/dt^2 = -eE$$

$$d\xi^2/dt^2 + (n_e e^2 / m_e \epsilon_0) \xi = 0$$

$$\omega_p = (n_e e^2 / m_e \epsilon_0)^{1/2}$$

V. I. Veksler, "Coherent Principle of Acceleration of Charged Particles." *Proceedings of the CERN Symposium on High Energy Accelerators and Pion Physics*, vol. 1. Geneva, 1956. Pages 80–83.



Laser Electron Accelerator

T. Tajima and J. M. Dawson

Department of Physics, University of California, Los Angeles, California 90024

(Received 9 March 1979)

An intense electromagnetic pulse can create a wake of plasma oscillations through the action of the nonlinear ponderomotive force. Electrons trapped in the wake can be accelerated to high energy. Existing glass lasers of power density 10^{18}W/cm^2 shone on plasmas of densities 10^{18}cm^{-3} can yield gigaelectronvolts of electron energy per centimeter of acceleration distance. This acceleration mechanism is demonstrated through computer simulation. Applications to accelerators and pulsers are examined.

Such a wake is most effectively generated if the length of the electromagnetic wave packet is half the wavelength of the plasma waves in the wake:

$$L_t = \lambda_w / 2 = \pi c / \omega_p. \quad (2)$$

An alternative way of exciting the plasmon is to inject two laser beams with slightly different frequencies (with frequency difference $\Delta\omega \sim \omega_p$) so that the beat distance of the packet becomes $2\pi c / \omega_p$. The mechanism for generating the wakes

=> Laser wakefield

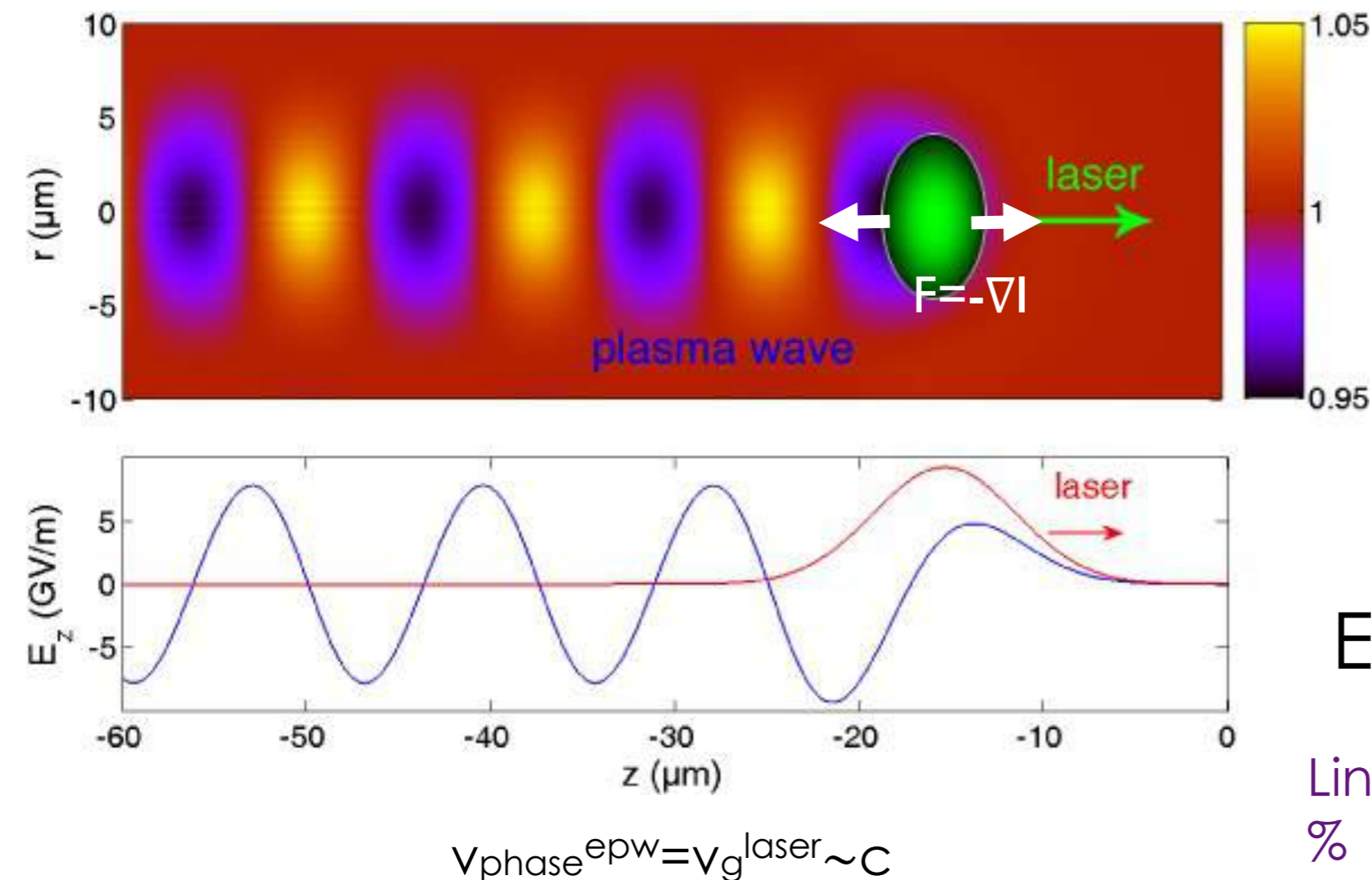
=> Laser beatwave

The linear wakefield regime: GV/m electric field

The laser wake field : broad resonance condition

$$T_{\text{laser}} \sim \pi / \omega_p \text{ with } \omega_p \sim n_e^{1/2} \text{ i.e. } \lambda_p \sim 1 / n_e^{1/2}$$

electron density perturbation & longitudinal wakefield



wave in the wake of a boat

$$E_z \text{ (GV/m)} \approx \delta n / n \times \sqrt{n}$$

Linear wakefield : $E_z = 1 \text{ GV/m}$ for 1 % density Perturbation at 10^{18} cc^{-1}

T. Tajima and J. Dawson, PRL **43**, 267 (1979)

The non-linear wakefield regime : 100's GV/m electric field



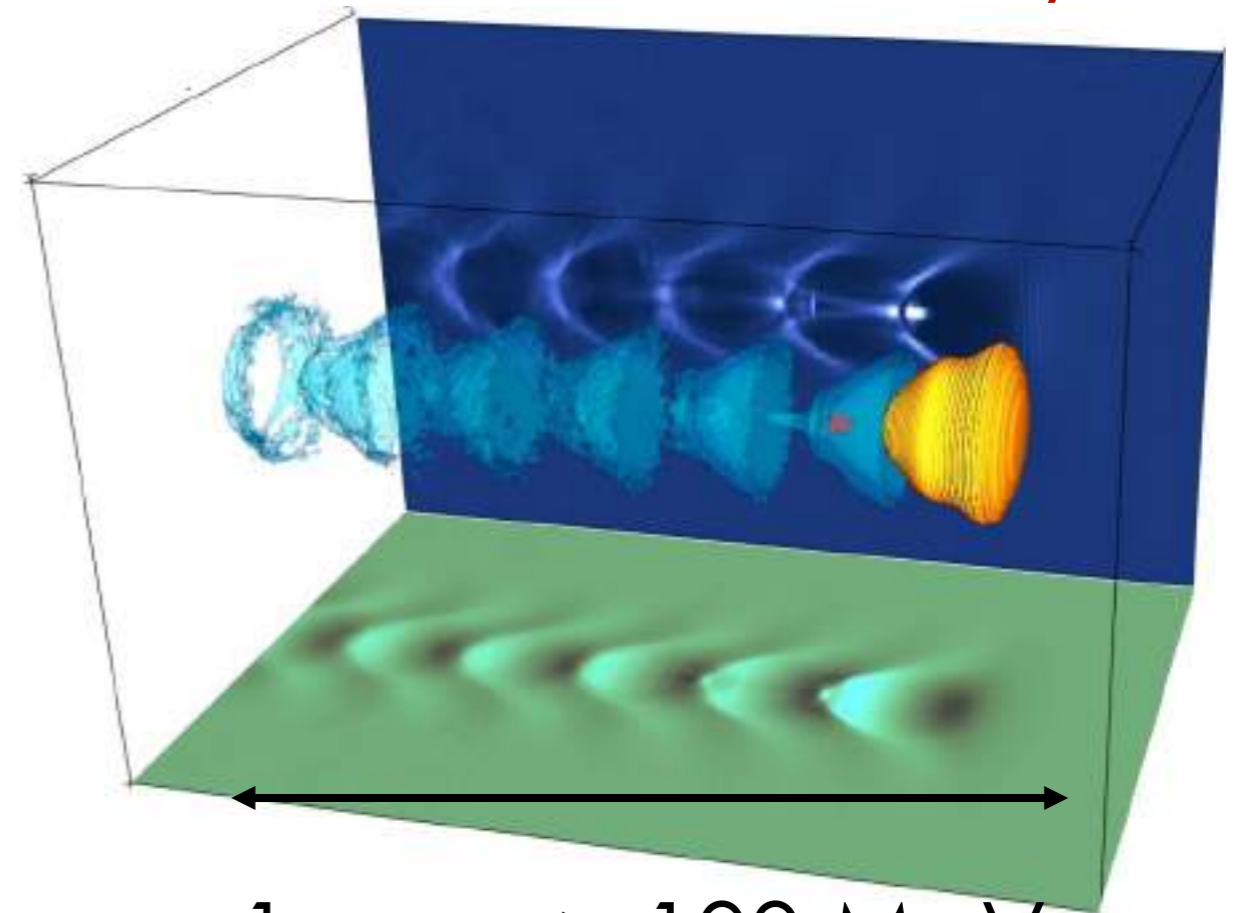
RF Cavity



1 m => 100 MeV Gain

Electric field < 100 MV/m

Plasma Cavity



1 mm => 100 MeV

Electric field > 100 GV/m

Non Linear Wakefield
V. Malka *et al.*, Science **298**, 1596 (2002)

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Laser intensity: definition



The laser electromagnetic wave is given by :

$$\mathbf{E}_L(z, t) = E_0/2 \cdot \exp[-i(k_0 z - \omega_0 t)] \mathbf{e}_x + c.c.$$

where k_0 is the laser wave vector and ω_0 the laser pulsation

Peak intensity:

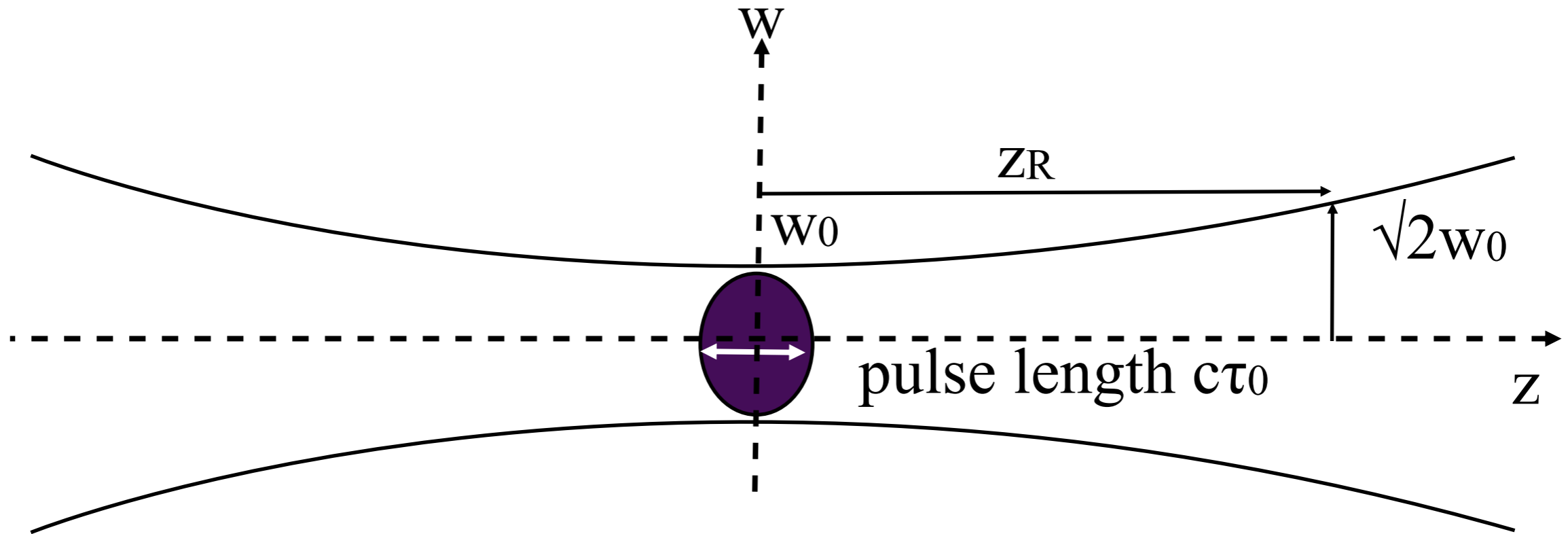
$$I_0 = \frac{1}{\mu_0} \langle \mathbf{E} \wedge \mathbf{B} \rangle = \frac{c\epsilon_0 E_0^2}{2}$$

For a gaussian beam at focus: $I(r, t) = I_0 \exp\left[-\frac{2r^2}{w_0^2}\right] \exp\left[-\frac{4 \ln 2 t^2}{\tau_0^2}\right]$

With peak intensity :

$$I_0 = \frac{2E}{\pi w_0^2 \tau_0}$$

Propagation of gaussian beam



Rayleigh length for which I_0 changes to $I_0/2$: $z_R = \pi w_0^2 / \lambda_0$

example : $\lambda_0 = 1 \mu\text{m}$, $w_0 = 20 \mu\text{m} \Rightarrow z_R = 1.2 \text{ mm}$



Lorentz factor : $\gamma = (1 - \frac{v^2}{c^2})^{-1/2}$

$$\gamma = \sqrt{1 + \frac{p^2}{m^2 c^2}}$$

Momentum : $\mathbf{p} = m\gamma\mathbf{v}$

Energy : $E = \gamma m_e c^2$ Kinetic energy : $E_{kin} = mc^2(\gamma - 1)$

Equation of motion : $\frac{d\mathbf{p}}{dt} = -e(\mathbf{E}_L + \mathbf{v} \wedge \mathbf{B}_L)$

For $v \ll c$ $\frac{dv_{osc}}{dt} = -e \frac{E_L}{m_e} = \frac{e}{m_e} \frac{\partial A}{\partial t}$

$$\frac{v_{osc}}{c} = a$$

$$a_0 = 0.85 [I_{18} (W/cm^2) \lambda (\mu m)^2]^{1/2}$$

$$mc^2 = 0.511 MeV \text{ for electrons}$$

The ponderomotive force :



First, linearize the equation of motion $\frac{d\mathbf{p}}{dt} = -e(\mathbf{E}_L + \mathbf{v} \wedge \mathbf{B}_L)$

$\mathbf{v} = \mathbf{v}_l + \mathbf{v}_{nl}$ with $\mathbf{v}_{nl} \ll \mathbf{v}_l$

$$\nabla \wedge \mathbf{E}_L = -\frac{\partial \mathbf{B}_L}{\partial t}$$

The second order gives $\frac{\partial \mathbf{v}_{nl}}{\partial t} = -(\mathbf{v}_l \nabla) \mathbf{v}_l - \frac{e}{m_e} (\mathbf{v}_l \wedge \mathbf{B}_L)$

by averaging over an optical cycle, one obtains : $m_e \frac{\partial \langle \mathbf{v}_{nl} \rangle_t}{\partial t} = -\frac{\nabla I}{2cn_c} = \mathbf{F}_p$

\mathbf{F}_p is called the ponderomotive force. This force repels charged particles from regions where the laser intensity gradient is large (whatever the sign of the charge). This ponderomotive force derives from a ponderomotive potential which is written as follow:

$$\phi_p = \frac{I_L}{2cn_c} = \frac{e^2 E_L^2}{4m_e \omega_0^2}$$

$$(\mathbf{v} \cdot \nabla) \mathbf{v} + \mathbf{v} \wedge (\nabla \wedge \mathbf{v}) = \frac{\nabla v^2}{2}$$

For an intensity of 10^{19} W/cm^2 @1micron, the ponderomotive potential is 1 MeV

Relativistic quantities & equation of motion



Equation of motion : $\frac{d\mathbf{p}}{dt} = -e(\mathbf{E}_L + \mathbf{v} \wedge \mathbf{B}_L)$

Maxwell's equation $\mathbf{B} = \nabla \wedge \mathbf{A} \quad \mathbf{E} = -\frac{\partial \mathbf{A}}{\partial t}$

Equation of motion : $\frac{d(\mathbf{p} - e\mathbf{A})}{dt} = -e(\nabla \mathbf{A}) \cdot \mathbf{v}$

Direction of propagation of the e.m. wave along x , \mathbf{A} is normal to x

$$\frac{d(\mathbf{p}_\perp - e\mathbf{A})}{dt} = 0 \quad \text{and} \quad \frac{dp_x}{dt} = -e\mathbf{v}_\perp \cdot \frac{\partial \mathbf{A}}{\partial x}$$

$$\frac{d\gamma mc^2}{dt} = \frac{e^2}{2m\gamma} \frac{\partial A^2}{\partial t} \quad (1)$$

and

$$\frac{dp_x}{dt} = -\frac{e^2}{2m\gamma} \frac{\partial A^2}{\partial x} \quad (2)$$

$$(1) - c^*(2) \Rightarrow$$

$$\gamma = 1 + \frac{p_x}{mc}$$

$$\mathbf{v} \wedge (\nabla \wedge \mathbf{A}) = (\nabla \mathbf{A}) \cdot \mathbf{v} - (\mathbf{v} \cdot \nabla) \mathbf{A} \quad (\nabla \mathbf{A}) \cdot \mathbf{v} \text{ being the summation on the same index of } v_j (\partial_i A^j) \mathbf{e}_i$$

Relativistic quantities & equation of motion



$$\frac{p_x}{mc} = \frac{1}{2} \left(\frac{e\mathbf{A}}{mc} \right)^2$$

$$\gamma = 1 + \frac{1}{2} \left(\frac{e\mathbf{A}}{mc} \right)^2$$

$$a_0 = \frac{e|\mathbf{A}|}{mc} = \frac{eE_0}{mc\omega_0}$$

$$a_0 = \left(\frac{e^2}{2\pi^2\epsilon_0 m^2 c^5} I_0 \lambda^2 \right)^{1/2} = 0.85 (I_{18} \lambda_{\mu m}^2)^{1/2}$$

$$\theta = \arctan\left(\frac{p_{\perp}}{p_x}\right) = \arctan(2/a) = \arctan\left(\sqrt{\frac{2}{\gamma-1}}\right)$$


Classical regime, $a \ll 1$, then $p_x \ll p_{\perp} \ll 1$, non relativistic transversale motion

Relativistic regime, $a > 1$, electron motion has a longitudinal component, that originates from the Lorentz force

Ultra-relativistic regime, $a \gg 1$, $p_x \gg p_{\perp} \gg 1$, motion mainly longitudinal

Relativistic quantities & equation of motion





$\vec{v} \wedge (\vec{\nabla} \wedge \vec{A}) = (\vec{\nabla} \wedge \vec{v}) \wedge \vec{A} - (\vec{v} \cdot \vec{\nabla}) \vec{A}$

$$\frac{d\vec{p}}{dt} = -e \left(\frac{d\vec{A}}{dt} - (\vec{v} \cdot \vec{\nabla}) \vec{A} + \vec{v} \wedge (\vec{\nabla} \wedge \vec{A}) \right) \Rightarrow \frac{d}{dt} (\vec{p} - e\vec{A}) = +e (\vec{\nabla} \wedge \vec{A}) \wedge \vec{v}$$

A ends of magnetic or potential along x
 A_y, A_z function of x $A \perp x$

$$\frac{d(p_x - eA)}{dt} = 0 \quad \frac{dp_x}{dt} = -e\vec{v} \cdot \frac{\partial \vec{A}}{\partial x}$$

$$\vec{E} = -e\vec{A} = m\delta\vec{v} \Rightarrow \vec{v} = \frac{e\vec{A}}{m\delta}$$

$$\vec{p} = e(\vec{E} + \vec{v} \wedge \vec{B}) \quad \vec{B} \wedge \vec{v} \wedge \vec{A} \quad \vec{E} = -\frac{\partial \vec{A}}{\partial t}$$

$$\frac{d\vec{A}}{dt} = \frac{\partial \vec{A}}{\partial t} + (\vec{v} \cdot \vec{\nabla}) \vec{A}$$

$$\vec{v} = \left(1 + \frac{p^2}{m^2 c^2} \right)^{-1/2} \vec{p}$$

$$\frac{dW}{dt} = \frac{d(\gamma mc^2)}{dt} = mc^2 \frac{d\delta}{dt} = mc^2 \frac{1}{2} \left(1 + \frac{p^2}{m^2 c^2} \right)^{-3/2} \frac{2\vec{p}}{m^2 c^2} \frac{d\vec{p}}{dt} = \frac{1}{2m} \frac{\vec{p}}{\delta^3} \cdot \frac{d\vec{p}}{dt}$$

$$= \frac{\vec{p}}{m\delta} \cdot (-e\vec{E} + \frac{\vec{p}}{m\delta} \wedge \vec{B}) = -\frac{e\vec{p}}{m\delta} \cdot \vec{E} = +\frac{e\vec{p}}{m\delta} \cdot \frac{\partial \vec{A}}{\partial t} = \frac{e}{m\delta} \frac{d}{dt} (\vec{p} \cdot \vec{A})$$

$$\frac{d(\gamma mc^2)}{dt} = \frac{e^2}{2m\delta} \frac{\partial A^2}{\partial t} \quad \text{①}$$

$$\frac{dp_x}{dt} = -e\vec{v} \cdot \frac{\partial \vec{A}}{\partial x} = -\frac{e^2}{m\delta} \frac{\vec{A} \cdot \vec{A}}{\partial x} = -\frac{e^2}{2m\delta} \frac{\partial A^2}{\partial x} \quad \text{②}$$

$$\text{①} - c \text{②}: \frac{e^2}{m\delta} \left(\frac{\partial A^2}{\partial t} + c \frac{\partial A^2}{\partial x} \right) = \frac{d(\gamma mc^2 - c p_x)}{dt} = \frac{e^2}{m\delta} \left(\frac{\partial}{\partial t} - \frac{\partial}{\partial x} \right) A^2 = 0$$

A function of $ct - x$: $\xi = ct - x$ $dt = d\xi$ $\frac{\partial}{\partial t} = \frac{\partial}{\partial \xi}$ $\frac{\partial}{\partial x} = -\frac{\partial}{\partial \xi}$

$$\gamma mc^2 - c p_x = mc^2 \quad \delta = 1 + \frac{p_x}{mc}$$

$$(\delta - 1)^2 mc^2 = p_x^2 \quad p_x^2 = p^2 - p_z^2 = [(\delta^2 - 1) - (\delta - 1)^2] m^2 c^2$$

$$p_x^2 = 2\delta(\delta - 1) m^2 c^2 = eA^2$$

$$\delta = 1 + \frac{1}{2} \left(\frac{eA}{mc} \right)^2$$

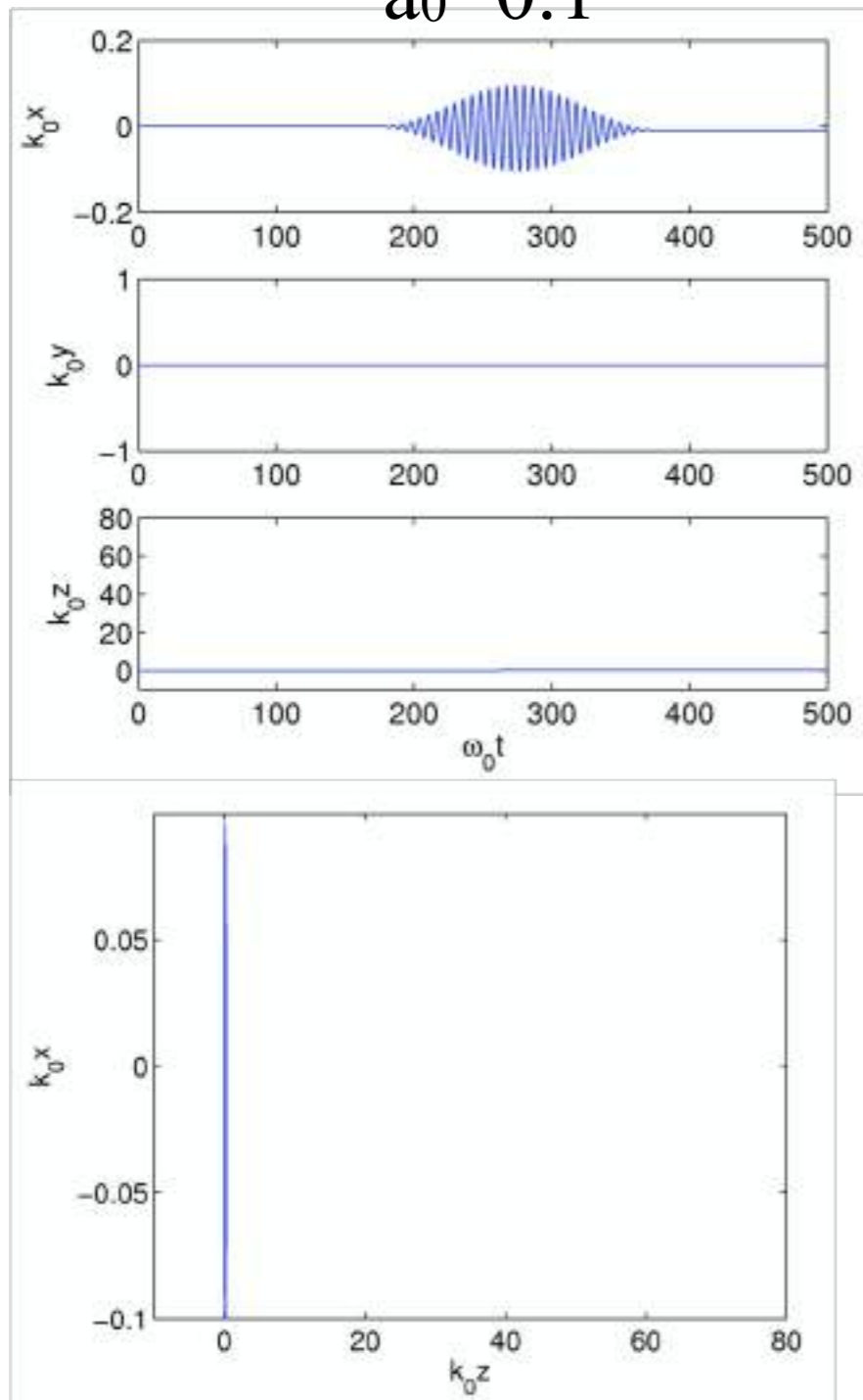
$$\frac{p_x}{mc} = \frac{1}{2} \left(\frac{eA}{mc} \right)^2$$

Electron motion in intense fields :

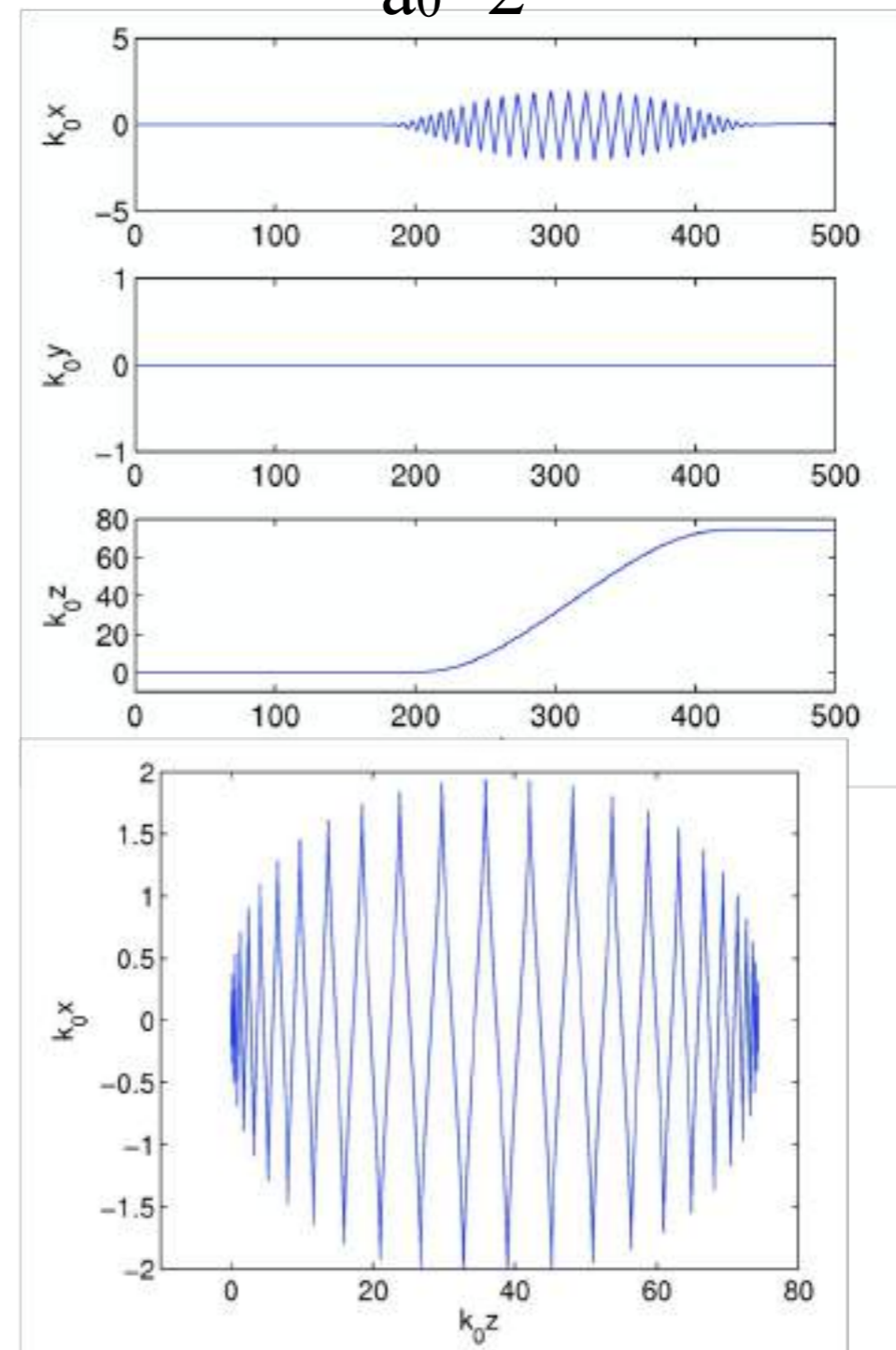


Laser linear polarization along x and propagating along z : $\frac{d\mathbf{p}}{dt} = -e(\mathbf{E}_L + \mathbf{v} \wedge \mathbf{B}_L)$

$a_0=0.1$



$a_0=2$



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- Ions are immobile : $\tau_{\text{laser}} \ll 1/\omega_{\text{pi}}$
- Plasma is a fluid of electrons : $n(\mathbf{r},t), v(\mathbf{r},t)$
- Plasma is cold : $v_{\text{osc}} \gg v_{\text{th}}$
- Plasma is underdense : $\omega_{\text{p}} \ll \omega_0$
- Laser field : $\mathbf{a} = a(r, z, t) \cos(k_0 z - \omega_0 t) \mathbf{e}_x$
- Envelop : $a^2(r, \zeta) = a_0^2 \exp(-\zeta^2 / L_0^2)$ with $\zeta = z - v_g t$
- Particle beam : $n_b(r, \zeta') = n_{b0} \exp(-\zeta'^2 / L_0^2) \exp(-r^2 / \sigma_b^2)$
with $\zeta' = z - v_b t$

Poisson's equation : general case



$$\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0} \quad \rho = -e(n - n_0) + qn_b \text{ with } q=-1 \text{ for an electron beam}$$

In addition, these fields can be written in terms of potentials :

$$\mathbf{E} = -\nabla\Phi - \frac{\partial\mathbf{A}}{\partial t} \quad \mathbf{B} = \nabla \wedge \mathbf{A}$$

Coulomb gauge so that $\nabla \cdot \mathbf{A} = 0$

$$\nabla^2\Phi = \frac{e}{\epsilon_0}(n + n_b - n_0)$$

Finally, one obtains the general Poisson's equation :

$$\nabla^2\Phi = \frac{en_0}{\epsilon_0} \left(\frac{\delta n}{n_0} + \frac{n_b}{n_0} \right)$$

Fluid equation :



Conservation equation

$$\frac{\partial n}{\partial t} + \nabla \cdot n \mathbf{v} = 0$$

Equation of motion for fluid electrons

$$\frac{\partial \mathbf{v}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{v} = -\frac{e}{m_e} (\mathbf{E} + \mathbf{v} \wedge \mathbf{B})$$

Which can be rewritten with « **L** » laser - high frequency :

$$\frac{\partial \mathbf{v}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{v} = -\frac{e}{m_e} (\mathbf{E}_L + \mathbf{v} \wedge \mathbf{B}_L - \nabla \Phi)$$

Fluid equation : general case



We now linearize the conservation equation in order to have the system of equations:

$$\frac{\partial \delta n}{\partial t} + n_0 \nabla \cdot \mathbf{v} = 0$$

Equation of motion for fluid electrons

$$\frac{\partial \mathbf{v}}{\partial t} = -c^2 \nabla \frac{a^2}{4} + \frac{e}{m_e} \nabla \Phi \quad \nabla^2 \Phi = \frac{en_0}{\epsilon_0} \left(\frac{\delta n}{n_0} + \frac{n_b}{n_0} \right)$$

Which gives :

$$\left(\frac{\partial^2}{\partial t^2} + \omega_p^2 \right) \frac{\delta n}{n_0} = c^2 \nabla^2 \frac{a^2}{4} - \omega_p^2 \frac{n_b}{n_0}$$

Fluid equation : general case



General equation :

$$\left(\frac{\partial^2}{\partial t^2} + \omega_p^2\right) \frac{\delta n}{n_0} = c^2 \nabla^2 \frac{a^2}{4} - \omega_p^2 \frac{n_b}{n_0}$$

The potential is given by :

$$\phi = e\Phi / m_e c^2 \quad \nabla^2 \phi = k_p^2 \delta n / n_0$$

Which gives for laser only :

$$\left(\frac{\partial^2}{\partial t^2} + \omega_p^2\right) \phi = \omega_p^2 \frac{a^2}{4}$$

Flowing window : in the laser frame



The laser driver moves at the velocity of light (a is a function of $\zeta = z - v_g t$), so it is practical to change variables in order to follow the laser pulse according to : $\tau = t$ and $\zeta = z - v_g t$.

$$\begin{aligned}\frac{\partial}{\partial t} &= \frac{\partial}{\partial \tau} - v_g \frac{\partial}{\partial \zeta} \\ \frac{\partial}{\partial z} &= \frac{\partial}{\partial \zeta} \\ \frac{\partial^2}{\partial t^2} &= \frac{\partial^2}{\partial \tau^2} + v_g^2 \frac{\partial^2}{\partial \zeta^2} - 2v_g \frac{\partial^2}{\partial \zeta \partial \tau} \\ \frac{\partial^2}{\partial z^2} &= \frac{\partial^2}{\partial \zeta^2}\end{aligned}$$

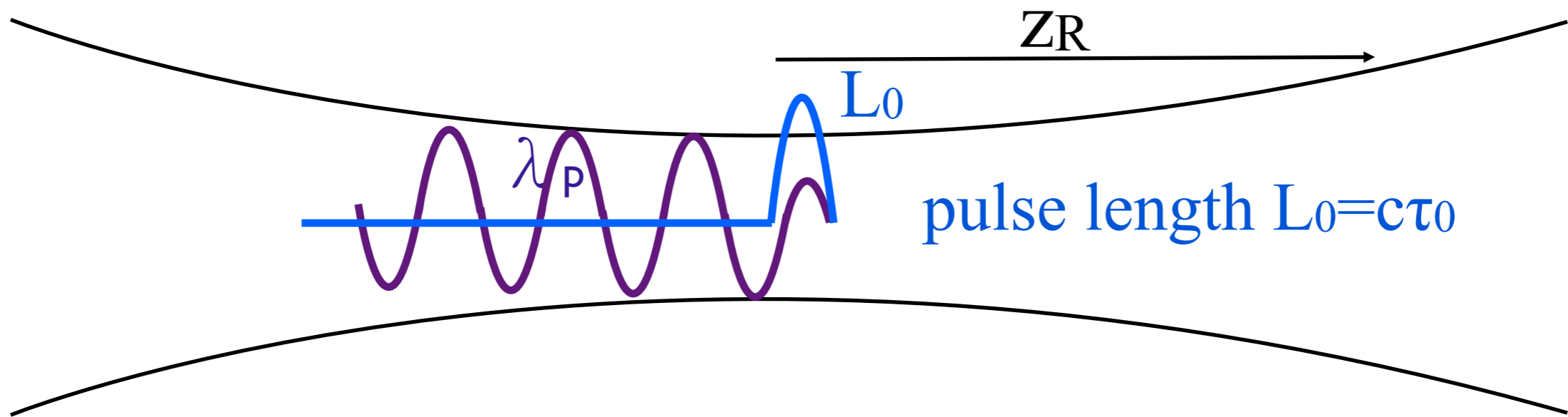
$$\left(\frac{\partial^2}{\partial \tau^2} + v_g^2 \frac{\partial^2}{\partial \zeta^2} - 2v_g \frac{\partial^2}{\partial \zeta \partial \tau} + \omega_p^2 \right) \phi = \omega_p^2 \frac{a^2}{4}$$

Quasi static approximation



Neglect the derivatives in τ versus ζ one

Physics meaning : adiabatic response of the laser due to the slow evolution of the laser



$$\left(\frac{\partial^2}{\partial \zeta^2} + k_p^2\right)\phi = k_p^2 \frac{a^2}{4}$$



Equazioni de l'onde plasma : régime linéaire

in matière peu collisionnelle : onde de plasma $\omega_p \ll \omega_c$
 densité perturbée $\rightarrow \delta n$

Eq Maxwell ; $\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0} = -\frac{e}{\epsilon_0} (\delta n - n_0)$ $\vec{E} = -\frac{\partial \vec{A}}{\partial t} - \nabla \phi$ $\vec{B} = \nabla \wedge \vec{A}$ $\nabla \cdot \vec{A} = 0$

on a démontré que $\boxed{\vec{F}_p = -m_e c^2 \frac{\nabla^2 a^2}{4} - m_e \frac{\partial^2 a^2}{\partial t^2}}$ Eq $\frac{\partial n}{\partial t} + \nabla \cdot n \vec{v} = 0$

$n = \delta n + n_0$ linéaire $\frac{\partial \delta n}{\partial t} + n_0 \nabla \cdot \vec{v} = 0$ $\nabla \cdot \vec{E} = -\nabla^2 \phi = -\frac{e}{\epsilon_0} (\delta n - n_0)$

$\frac{\partial n}{\partial t} = -\frac{e}{m} (\vec{E} + \nabla \wedge \vec{A}) = -\frac{e}{m} (\vec{E}_{\text{ext}} + \nabla \wedge \vec{A}_{\text{ext}} + \vec{E}_{\text{plasma}}) = -c^2 \frac{\nabla^2 a^2}{4} - \frac{e}{m} \frac{\partial \vec{A}_{\text{plasma}}}{\partial t} = \frac{e}{m} \frac{\partial}{\partial t} \left(\frac{e}{m_e} \frac{\partial \vec{A}_{\text{plasma}}}{\partial t} \right)$

$\frac{\partial^2 \delta n}{\partial t^2} - c^2 \frac{\nabla^2 \delta n}{4} - \frac{e}{m} \nabla \cdot \vec{E}_{\text{plasma}} = -c^2 \frac{\nabla^2 a^2}{4} + \frac{e^2}{m \epsilon_0} \delta n = -\frac{\delta^2 n}{n_0 c^2}$

$\frac{\partial^2 \delta n}{\partial t^2} + \frac{n_0 e^4}{m \epsilon_0} \delta n = m_e c^2 \frac{\nabla^2 a^2}{4}$ $\epsilon = \frac{n_0 e^4}{n_0 c^2}$

$\boxed{\left(\frac{\partial^2}{\partial t^2} + \omega_p^2 \right) \delta = c^2 \frac{\nabla^2 a^2}{4}}$

$a \rightarrow a(x, \xi)$ $\xi = ct - z$

$\left(\frac{\partial^2}{\partial \xi^2} + \frac{\omega_p^2}{c^2} \right) \delta = \frac{\nabla^2 a^2}{4} = \left(\frac{\partial^2}{\partial \xi^2} + k_p^2 \right) \delta$

$\left(\frac{\partial^2}{\partial \xi^2} + k_p^2 \right) \frac{1}{k_p} \frac{\partial^2 \phi}{\partial \xi^2} = \frac{\nabla^2 a^2}{4}$

$\left(\frac{\partial^2}{\partial \xi^2} + k_p^2 \right) \phi = \frac{k_p^2 a^2}{4}$

$\partial_\xi = \frac{\partial}{\partial t} - \frac{\partial}{\partial z}$ $\frac{\partial^2}{\partial \xi^2} = \frac{\partial^2}{\partial t^2} - \frac{\partial^2}{\partial z^2}$ $\frac{\partial^4}{\partial t^4} = \frac{\partial^4}{\partial z^4}$

$k_p = \frac{\omega_p}{c}$ $\phi = e\phi / mc^2$ $\delta = \frac{\delta n}{n_0}$

or $\nabla^2 \phi = \frac{e \delta n}{\epsilon_0} \rightarrow \nabla^2 \phi = \frac{m_e e^4}{\epsilon_0 m c^2} \delta$

$\nabla^2 \phi = \frac{m_e e^4}{\epsilon_0 m c^2} \delta = \frac{e^2}{\epsilon_0} \frac{\delta n}{n_0}$

$\rightarrow \delta = \frac{k_p^2}{\epsilon_0} \nabla^2 \phi$



Quasi static approximation

$$\left(\frac{\partial^2}{\partial \zeta^2} + k_p^2\right)\phi = k_p^2 \frac{a^2}{4}$$

Solution of the equation =0 for $\zeta = +\infty$
(no perturbation before the laser pulse)

$$\longrightarrow \phi(r, \zeta) = -\frac{k_p}{4} \int_{\zeta}^{+\infty} a^2(\zeta') \sin(k_p(\zeta - \zeta')) d\zeta'$$

$$\text{At } \zeta = -\infty, a^2 = 0 \longrightarrow \phi(r, \zeta) = -\frac{k_p}{4} \int_{-\infty}^{+\infty} a^2(\zeta') \sin(k_p(\zeta' - \zeta')) d\zeta'$$

$$\phi(r, \zeta) = -\frac{k_p}{4} (\sin(k_p \zeta) \int_{-\infty}^{+\infty} a^2(\zeta') \cos(k_p \zeta') d\zeta' + \cos(k_p \zeta) \int_{-\infty}^{+\infty} a^2(\zeta') \sin(k_p(\zeta')) d\zeta')$$

Since a^2 is an even function, the second term is nul, then:

$$\phi(r, \zeta) = -\frac{k_p}{4} \sin(k_p \zeta) \text{TF}(a^2)$$

For a gaussian beam,

$$a(r, \zeta) = a_0 \exp\left(-\frac{r^2}{w_0^2}\right) \exp\left(-2 \ln(2) \frac{\zeta^2}{c^2 \tau^2}\right)$$

$$f(x) = e^{-\alpha \frac{x^2}{2}} \rightarrow \hat{f}(p) = \frac{1}{\sqrt{\alpha}} e^{-\frac{p^2}{2\alpha}}$$

Solution of the envelop equation



Solution (after the gaussian laser pulse have gone):

$$\text{Potential: } \phi = -\sqrt{\pi} a_0^2 \frac{k_p L_0}{4} e^{-k_p^2 L_0^2 / 4} e^{-r^2 / \sigma^2} \sin(k_p \zeta)$$

$$\text{Electric field: } \frac{\mathbf{E}}{E_0} = -\frac{1}{k_p} \nabla \phi = -\frac{1}{k_p} \left(\mathbf{e}_z \frac{\partial}{\partial \zeta} + \mathbf{e}_r \frac{\partial}{\partial r} \right) \phi$$

$$\text{Longitudinal E: } \frac{E_z}{E_0} = \sqrt{\pi} a_0^2 \frac{k_p L_0}{4} e^{-k_p^2 L_0^2 / 4} e^{-r^2 / \sigma^2} \cos(k_p \zeta)$$

$$\text{Transversal E: } \frac{E_r}{E_0} = -\sqrt{\pi} a_0^2 \frac{L_0 r}{\sigma^2} e^{-k_p^2 L_0^2 / 4} e^{-r^2 / \sigma^2} \sin(k_p \zeta)$$

$$E_0 \text{ Wave breaking E field: } E_0 = \frac{m_e c \omega_p}{e} \sim n^{1/2}$$

$$L_0 = \frac{c \tau_0}{2\sqrt{\log 2}}$$

Solution for the density perturbation



From the Poisson's equation, one then obtains

Longitudinal density perturbation :

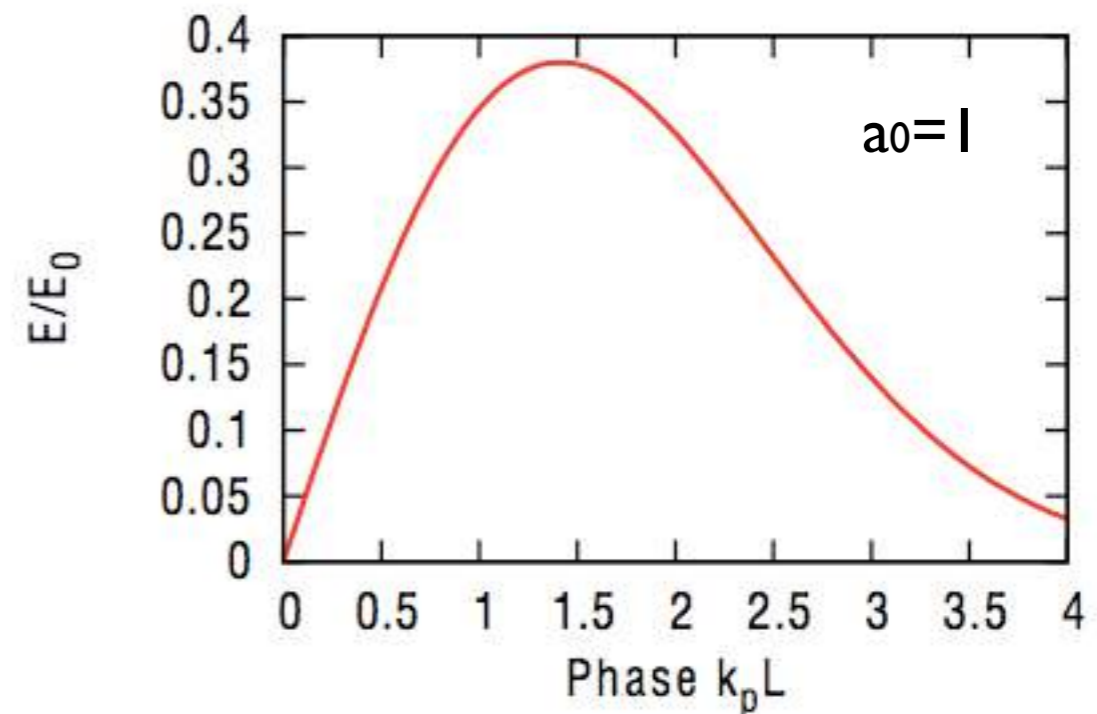
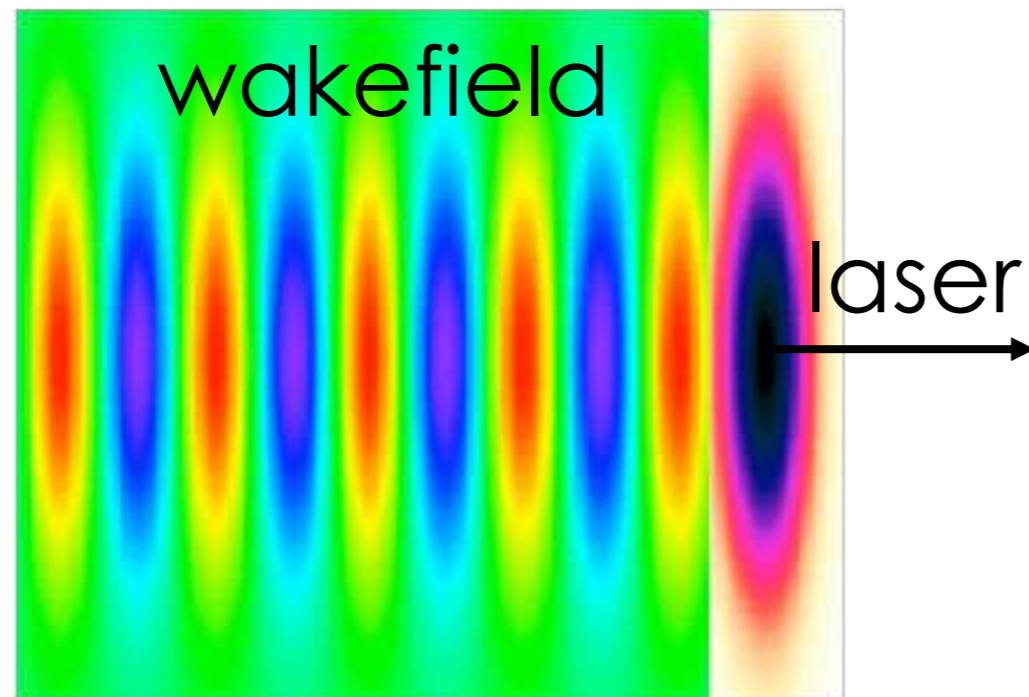
$$\frac{\delta n_z}{n_0} = \sqrt{\pi} a_0^2 \frac{k_p L_0}{4} e^{-k_p^2 L_0^2 / 4} e^{-r^2 / \sigma^2} \sin(k_p \zeta)$$

Radial density perturbation :

$$\frac{\delta n_r}{n_0} = \frac{\delta n_z}{n_0} \frac{4}{k_p^2 \sigma^2} \left(1 - \frac{r^2}{\sigma^2}\right)$$

$$\phi = \sqrt{\pi} a_0^2 \frac{k_p L_0}{4} e^{-k_p^2 L_0^2 / 4}$$

Resonance condition for Laser Wakefield



Optimum potential: $\frac{\partial \phi}{\partial L_0} = 0$ which gives $k_p L_0 = \sqrt{2}$
 $(\delta n_z / n_0)_{max} \approx 0.4 a_0^2$

In the laser wakefield the resonance is very broad

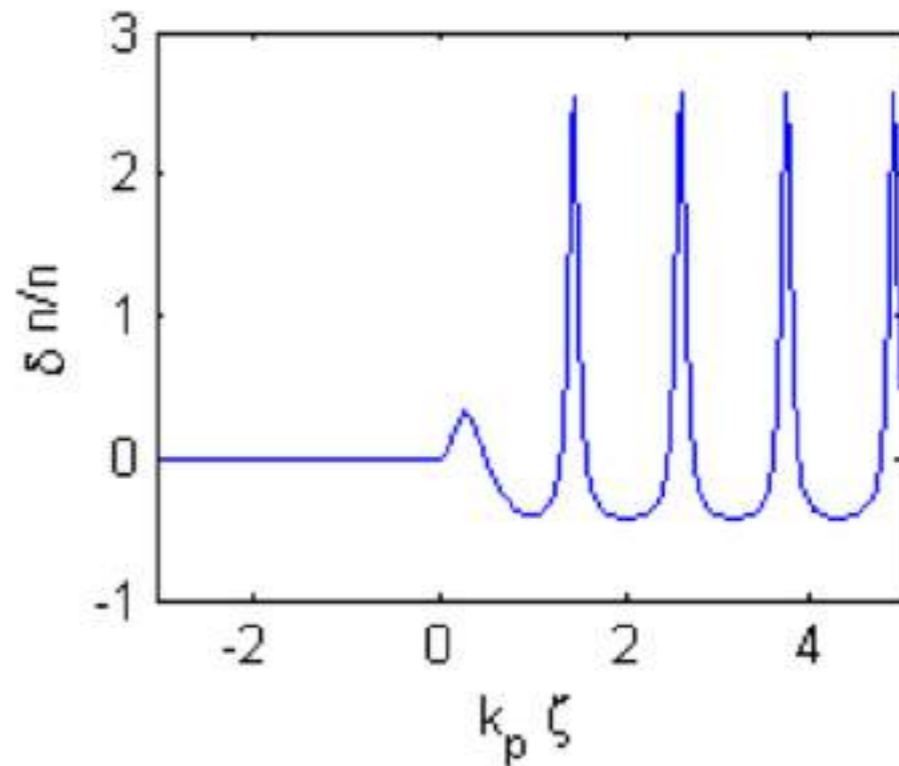
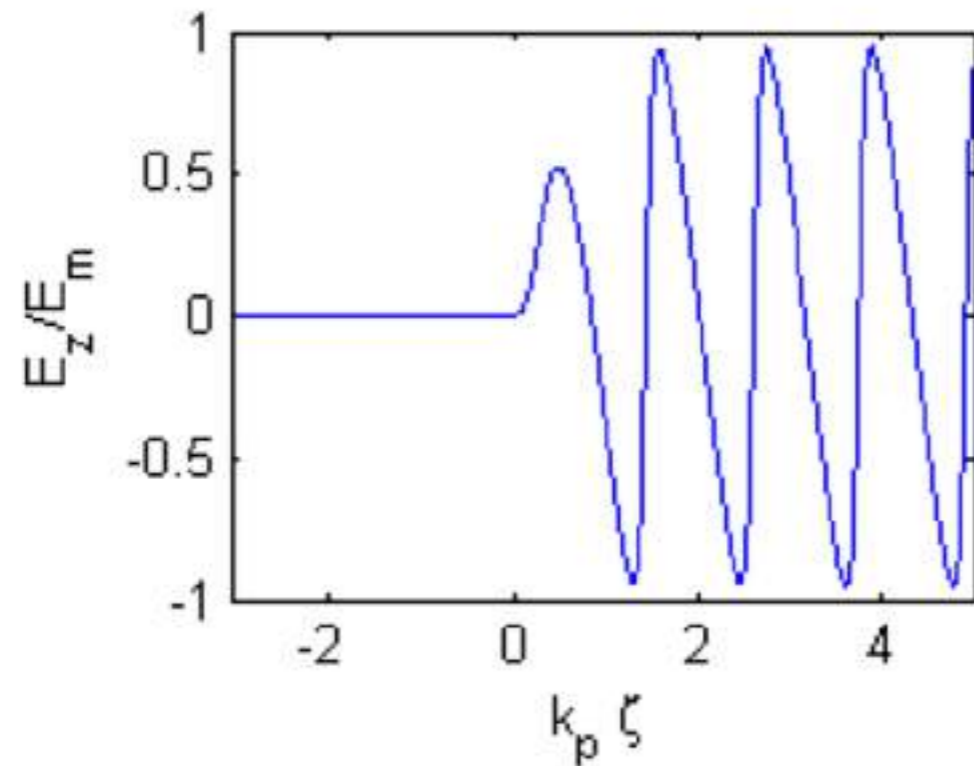
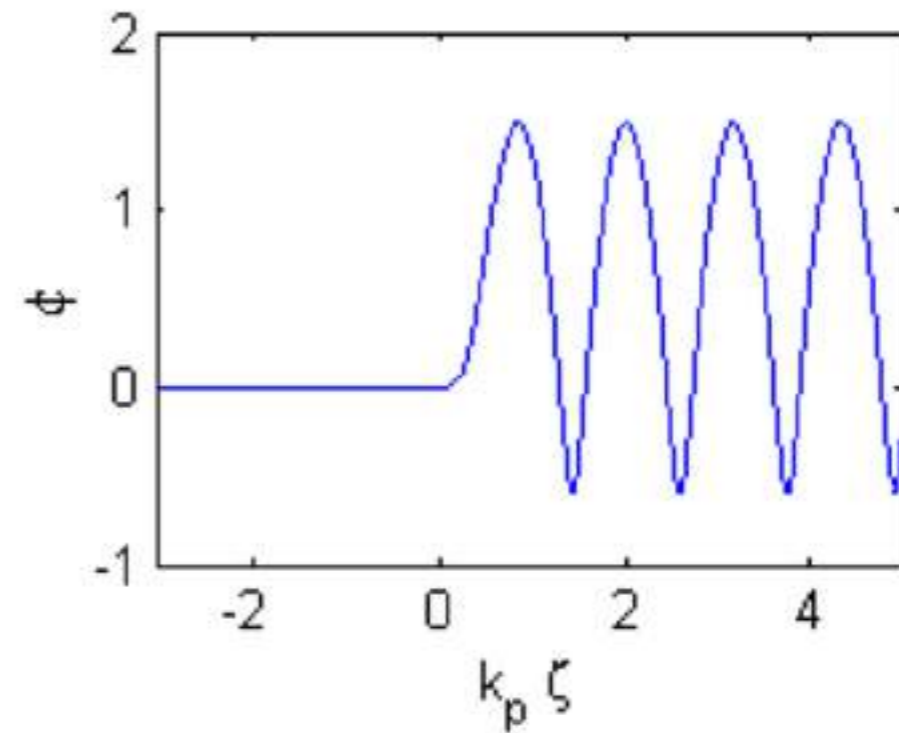
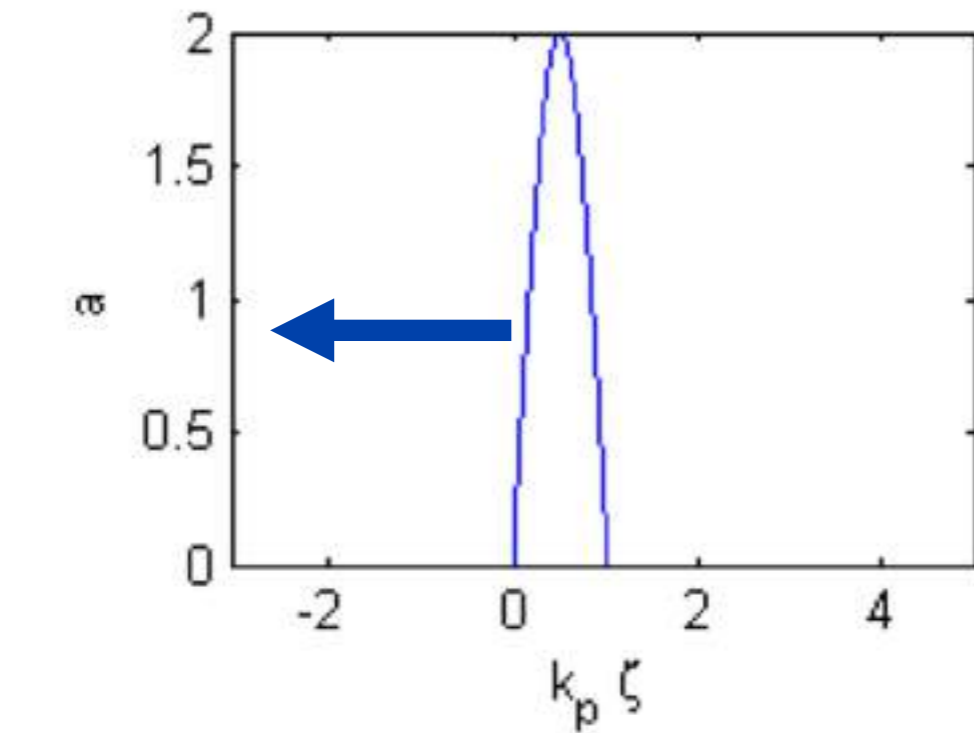
$$n_e (\text{cm}^{-3}) = \frac{1.7 \times 10^{21}}{\tau_{FWHM}^2 (\text{fs})} \Rightarrow 30 \text{ fs @ } 1.9 \times 10^{18} \text{ cm}^{-3}$$

Gorbunov et al. Sov. Phys. JETP 66 (87)

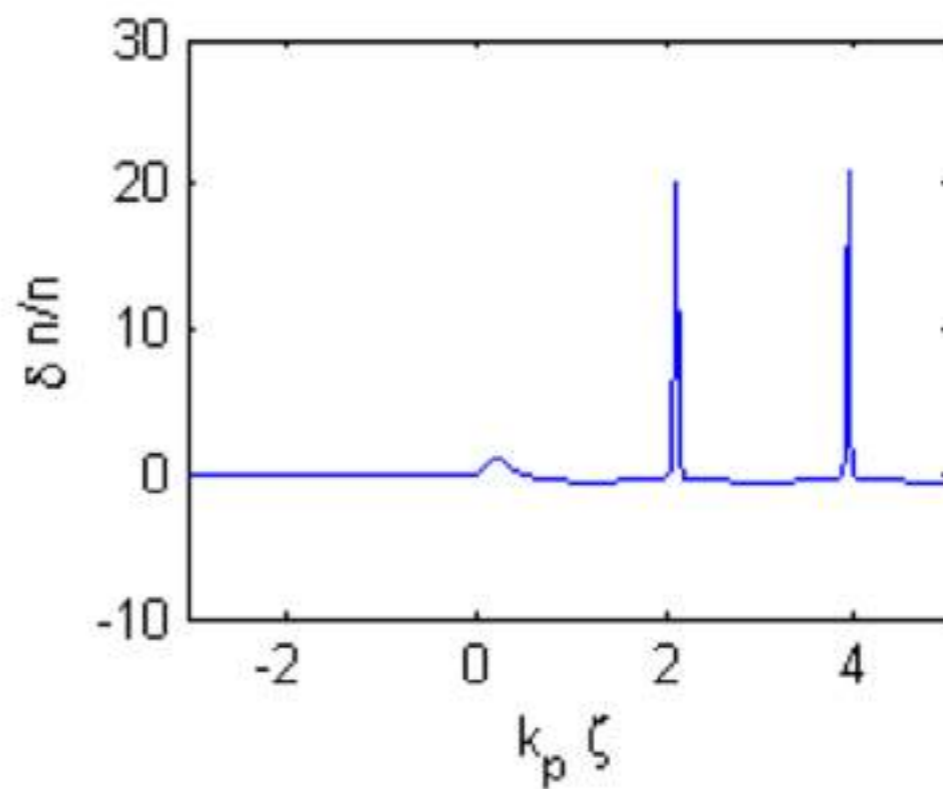
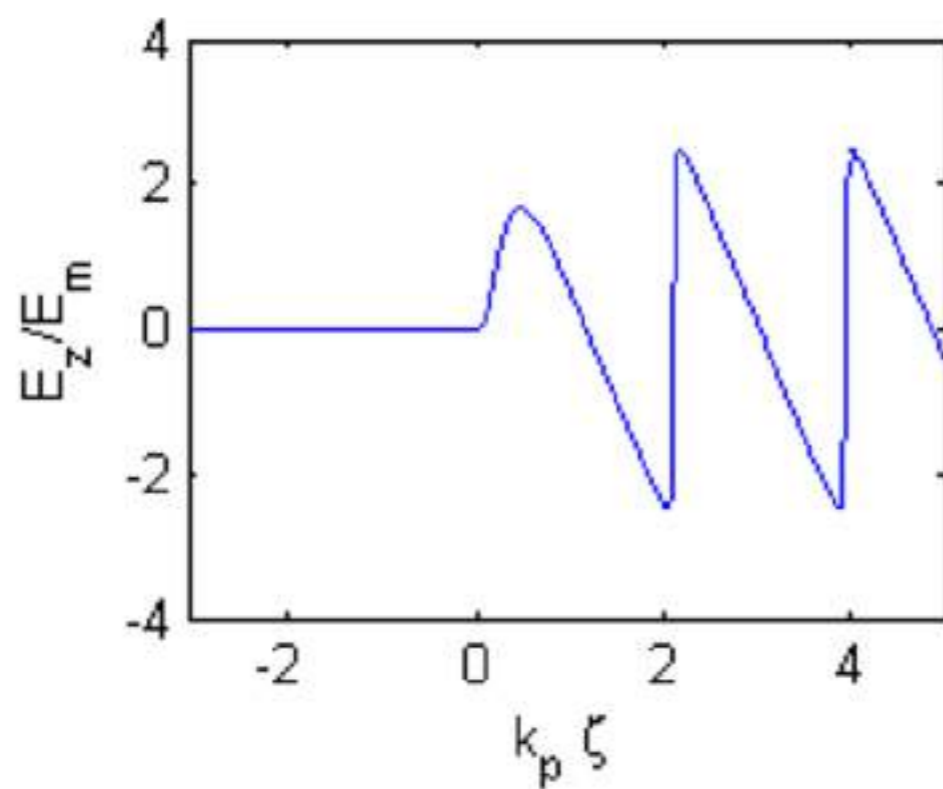
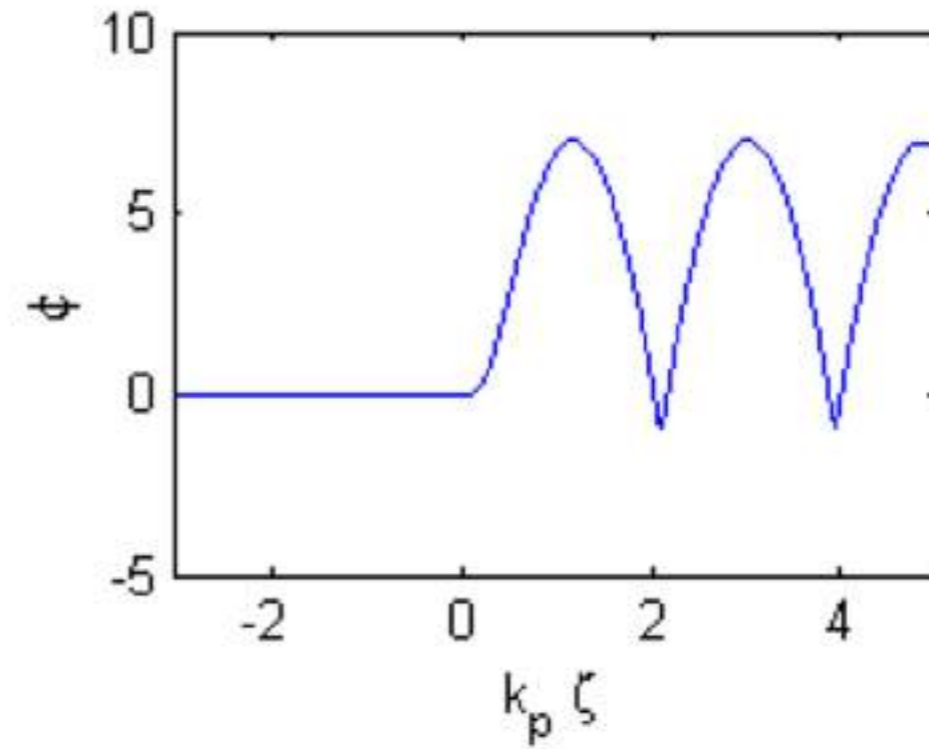
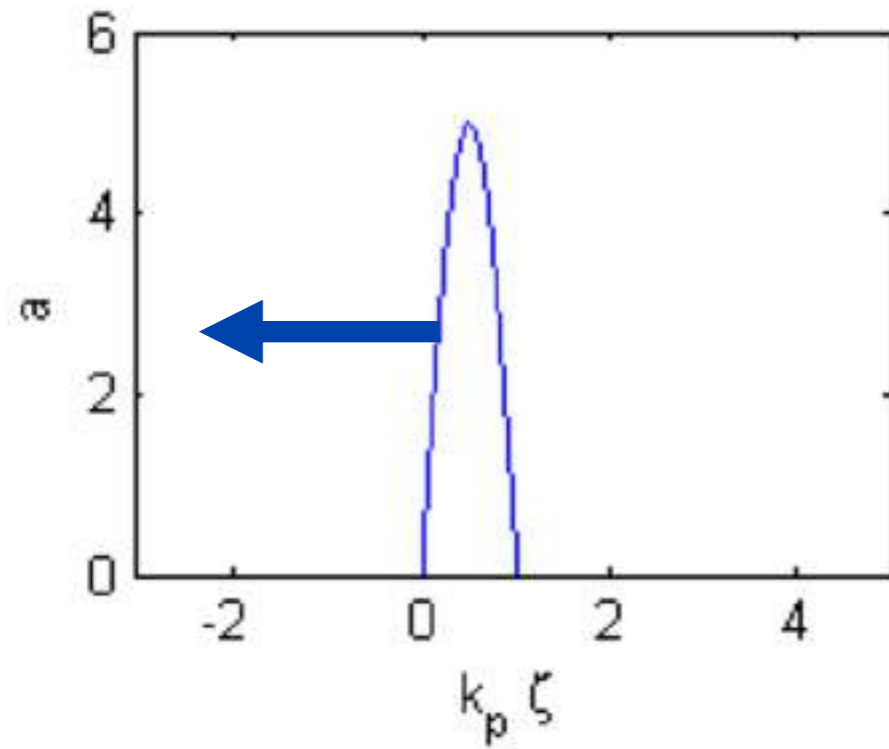
Twist movie: the resonance



Non Linear Plasma waves 1D : $a_0=2$ (30fs)



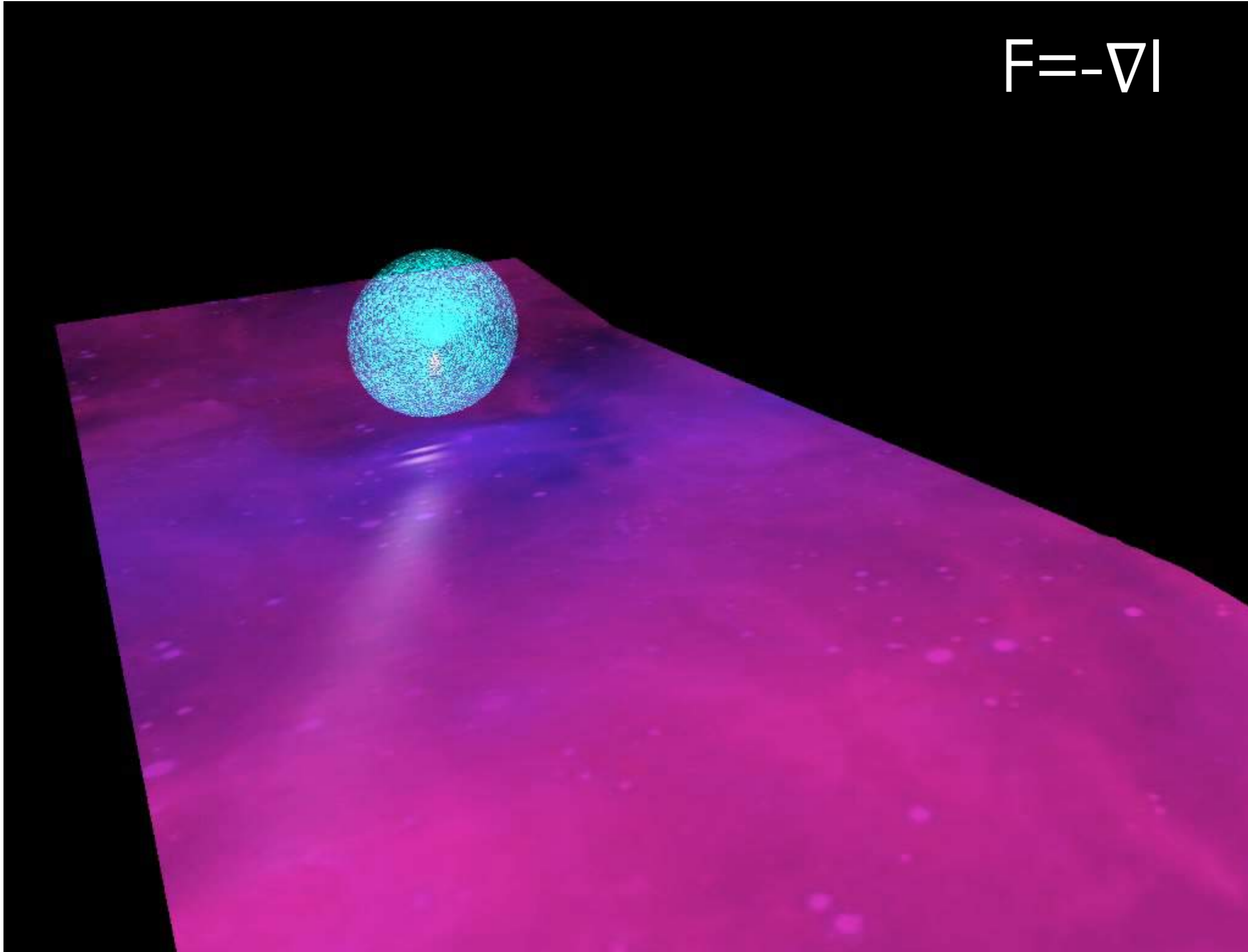
Non Linear Plasma waves 1D : $a_0=5$ (30fs)



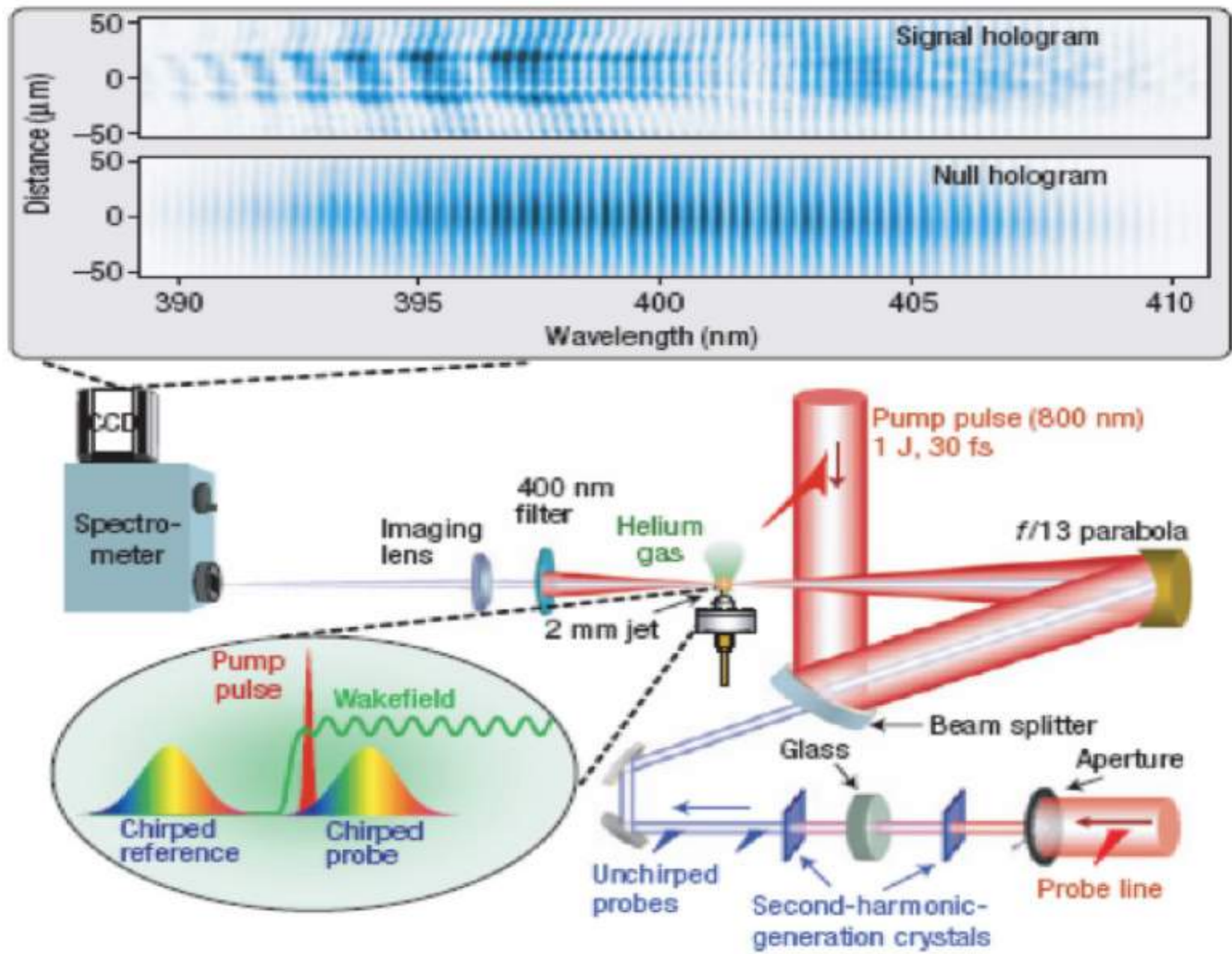
The Forced laser wakefield



$$F = -\nabla V$$

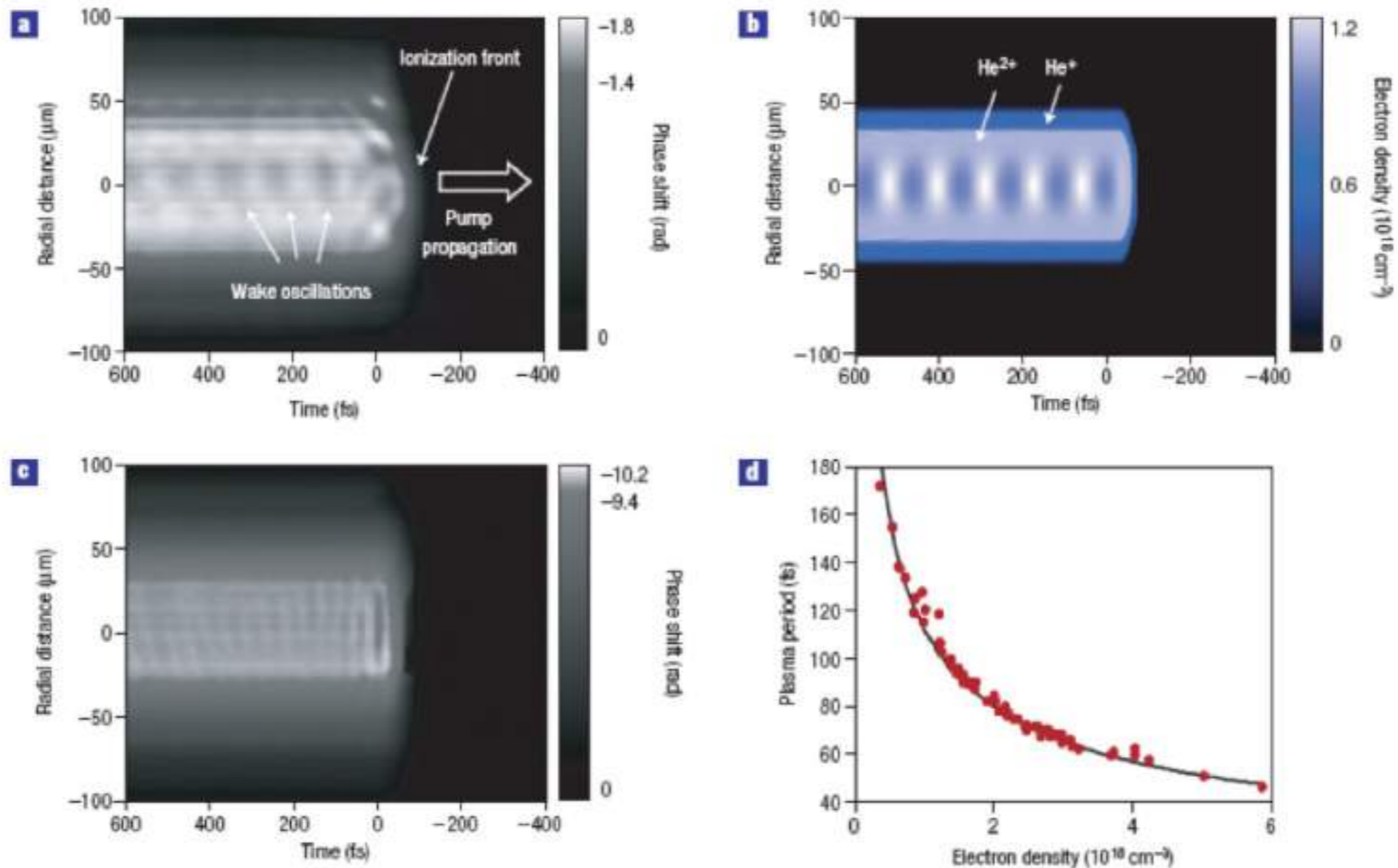


Snapshots of laser wakefield



N. H. Matlis *et al.* , Nature Physics 2006

Snapshots of laser wakefield



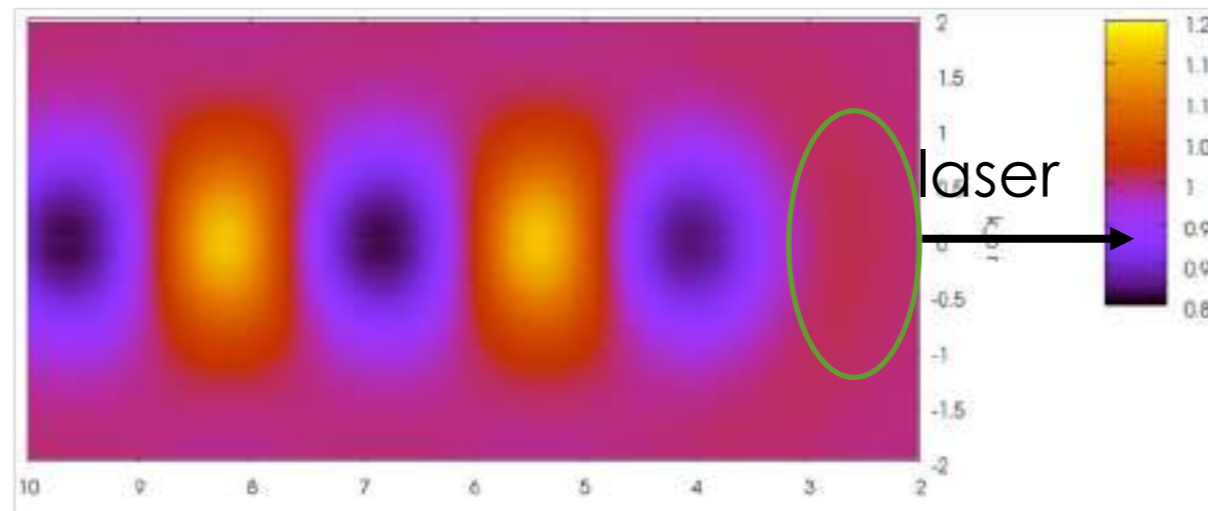
Small amplitude wakes with flat wavefronts. a) probe phase shift 10TW, 30 fs at $0.95 \times 10^{19} \text{cm}^{-3}$.
b) Simulated wake density profile. c) same than a) at $5.9 \times 10^{19} \text{cm}^{-3}$. d) wake period versus n_e .

N. H. Matlis *et al.*, Nature Physics 2006

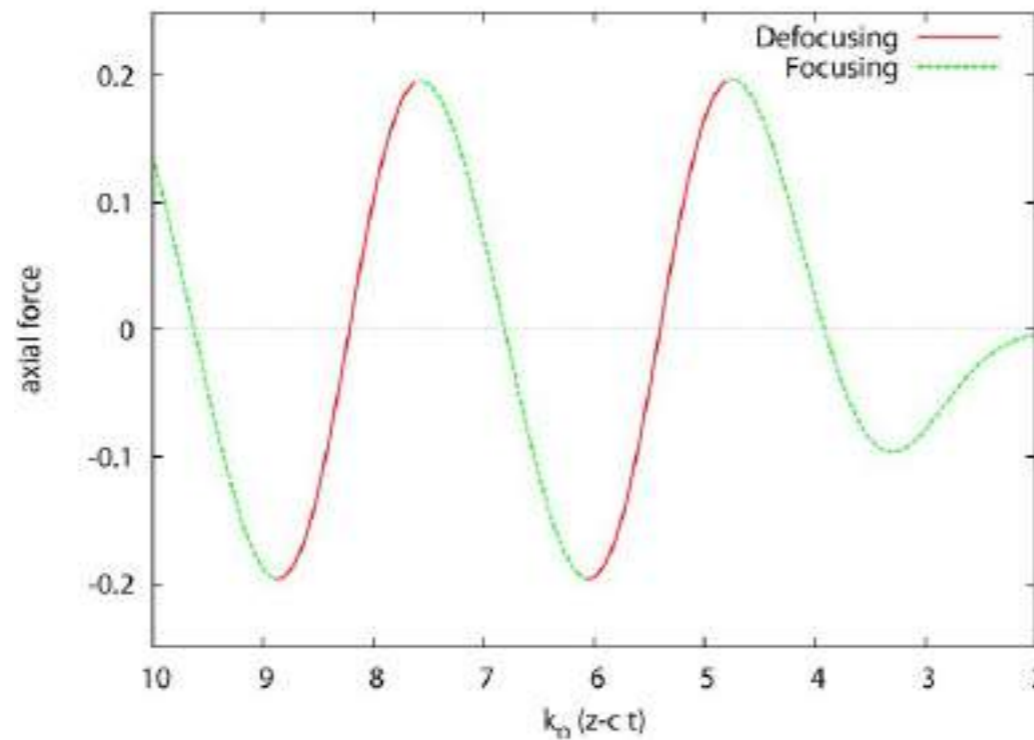
Accel./decel.-focusing/defocusing fields: Linear case



$a_0=0.5$



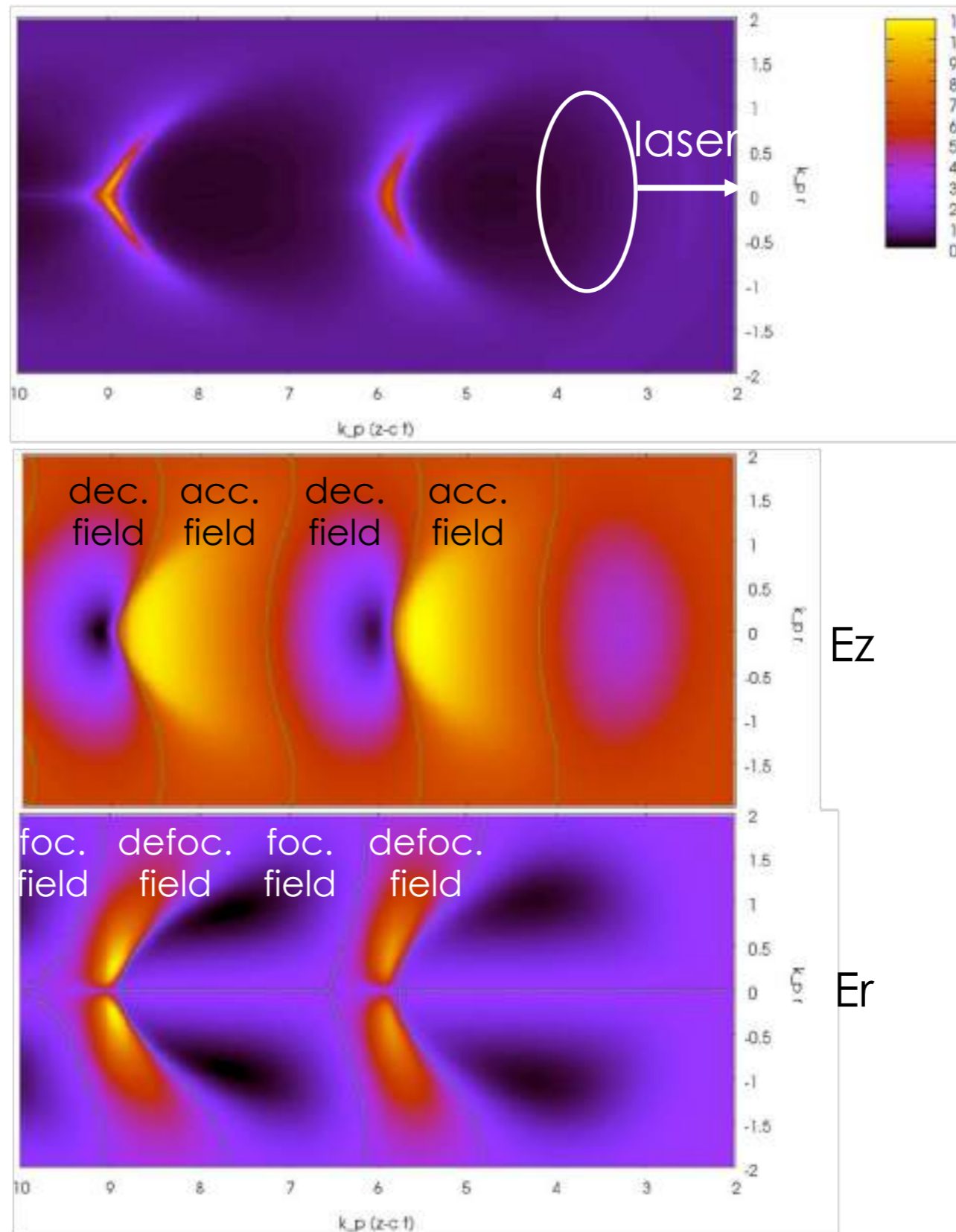
electron density



Accel./decel.-focusing/defocusing fields: Non-Linear case



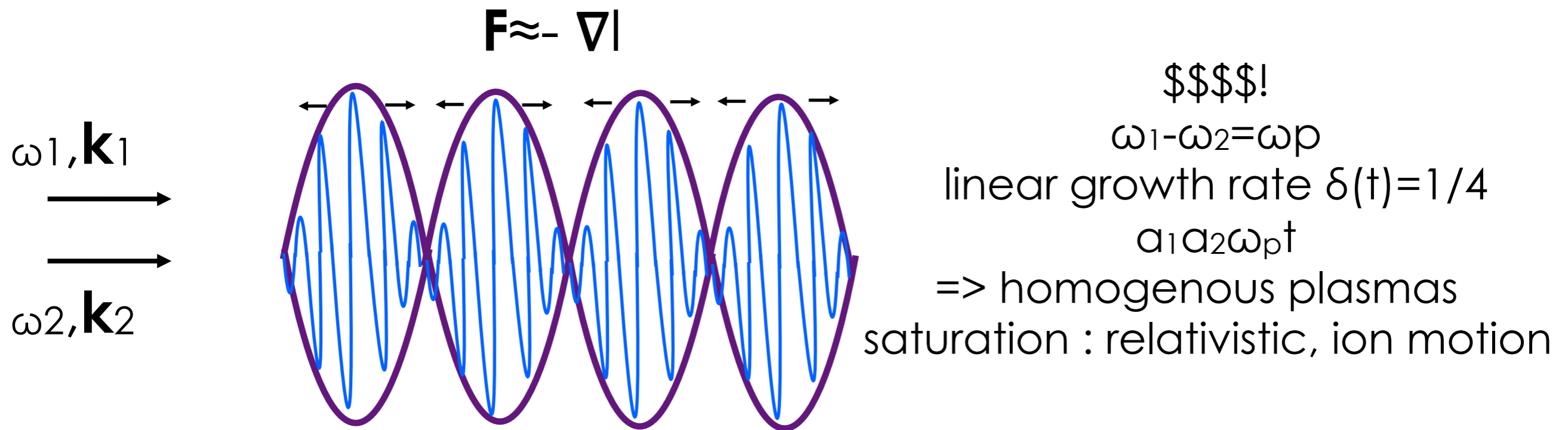
$$a_0=2$$



1985-1995 How to excite a plasma wave ? LBW



The laser beat waves : $T_L \gg T_p$



Train of short resonant pulses

Optical demonstration by Thomson scattering :

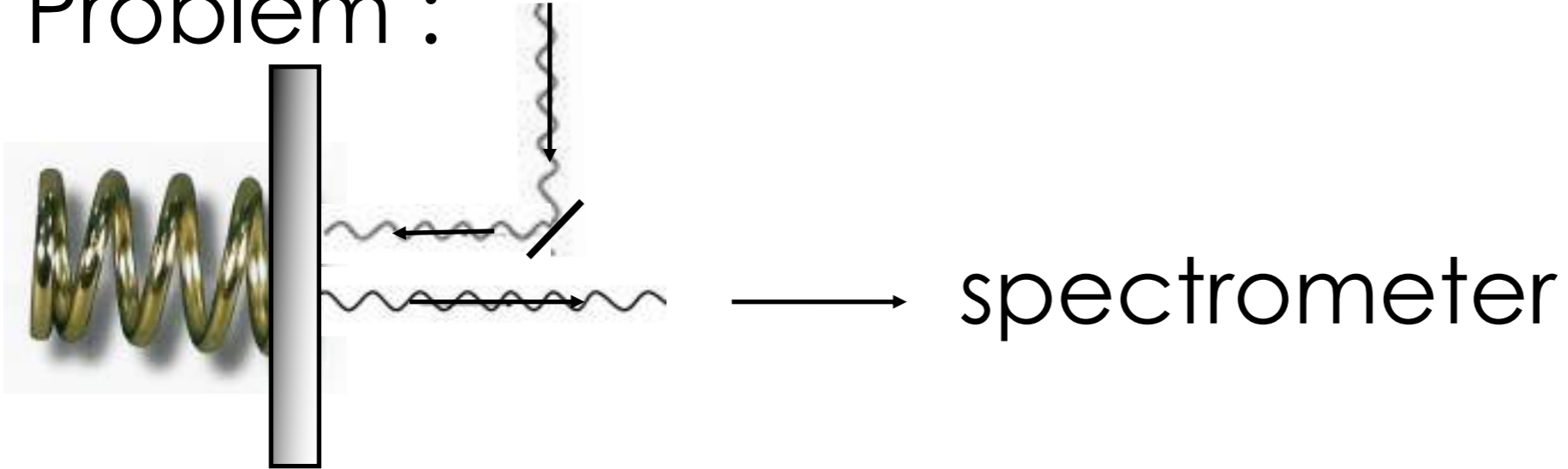
Clayton *et al.* PRL 1985, Amiranoff *et al.* PRL 1992, Dangor *et al.* Phys. Scripta 1990

Chen, Introduction to plasma physics and controlled fusion, 2nd Edition, Vol.1, (1984)

Analogy : oscillating mirror's problem



Problem :



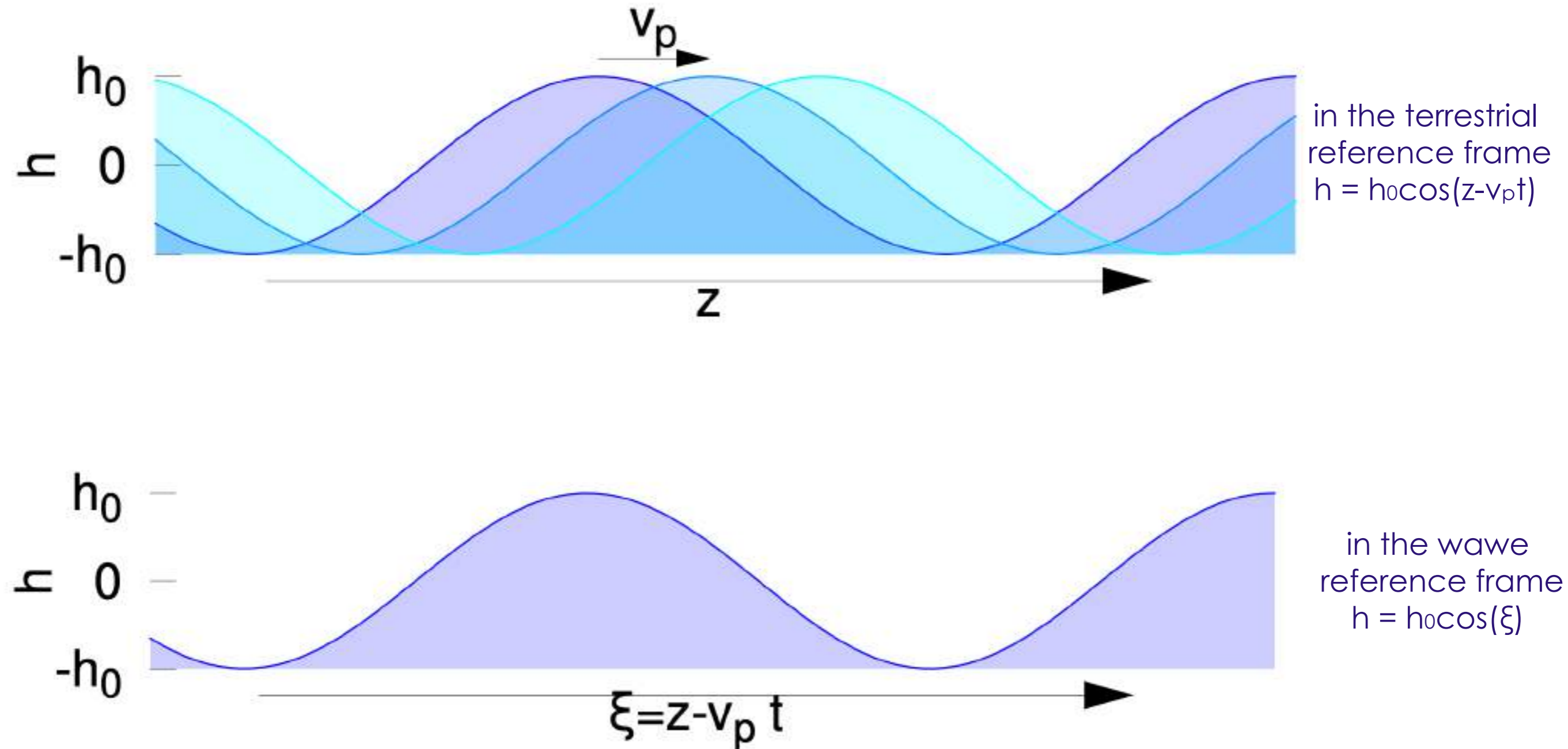


- Introduction : context and motivations
- Electron in a laser field
- Laser driven plasma wave : theory
- **Trapping Conditions**

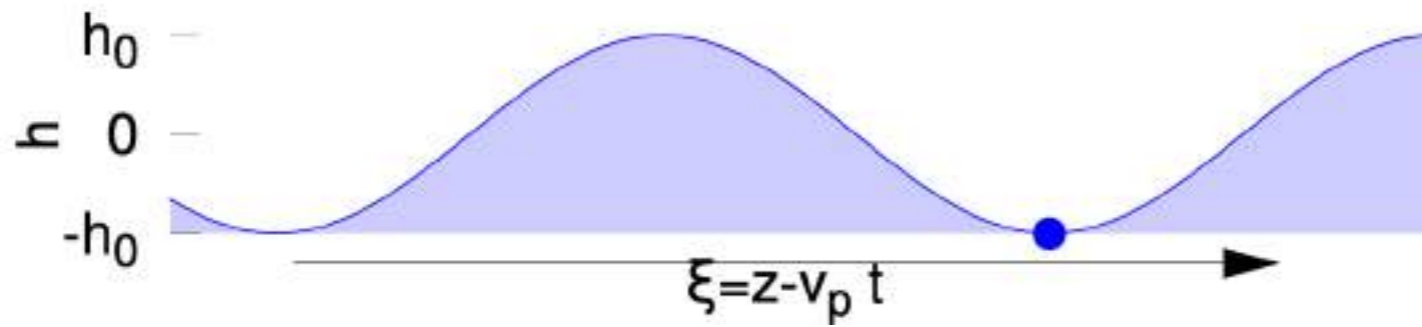
Part I : Motivation, basis and principle

- Introduction : context and motivations
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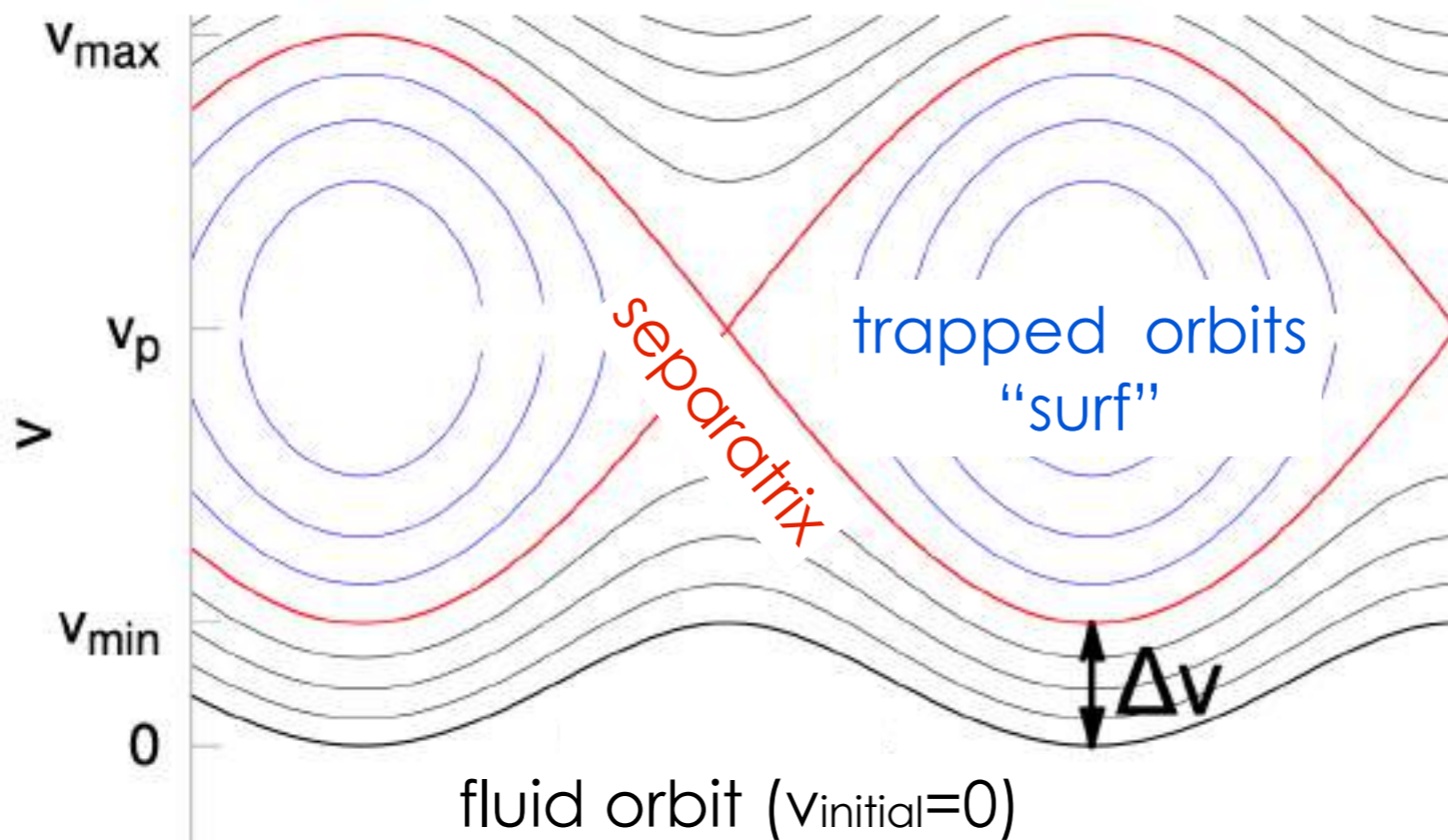
Injection criteria : the surfer



Injection criteria : the surfer experiences



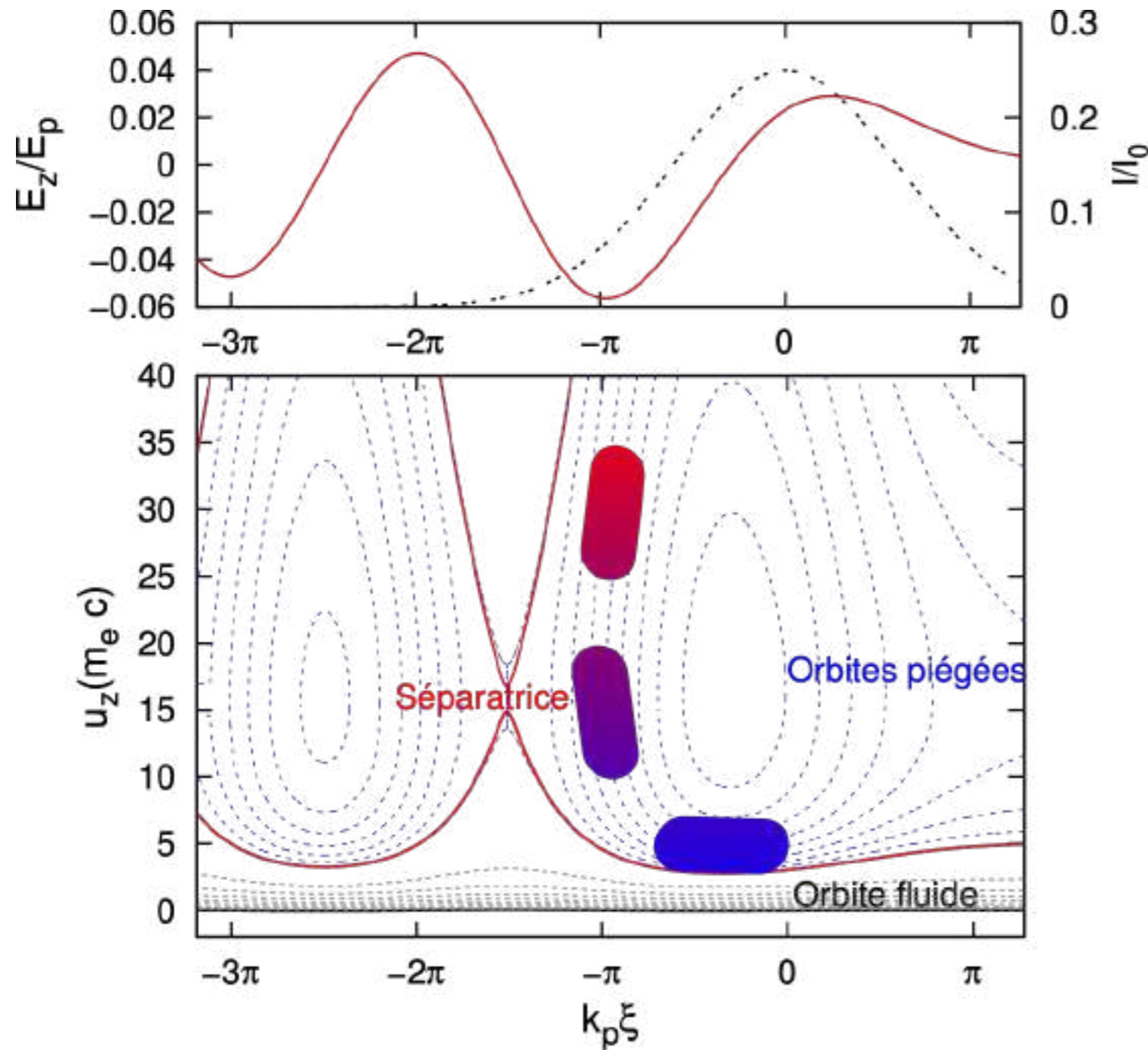
phases space (ξ , $v-v_p$)



conclusions :

- Trapped orbits allow higher energy gain
- One needs to transmit enough velocity Δv

1 D maximum energy gain : $W_{\max}: eE_p L_{\text{deph}}$



In plasma wave :

- E field is not homogenous
- Volume in phase space is conserved
- very small initial volume

external injection :

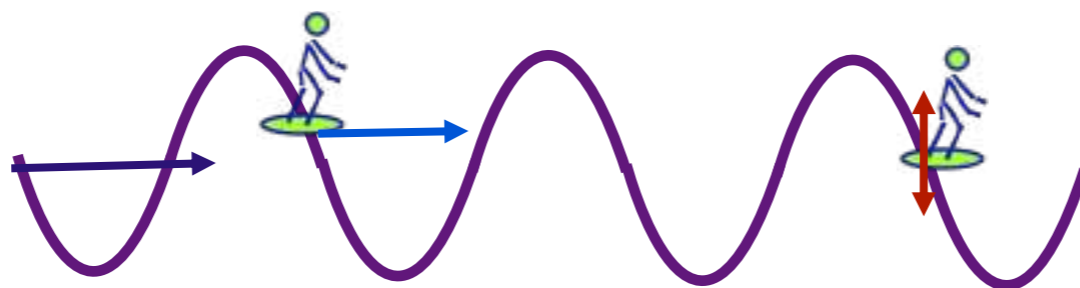
- Size $\approx \mu\text{m}$
- Length $\approx \mu\text{m}$ (fs)
- Synchronization \approx fs
- Control ?

=> very challenging with conventional accelerator

Trapping energy : analogy electron/surfer

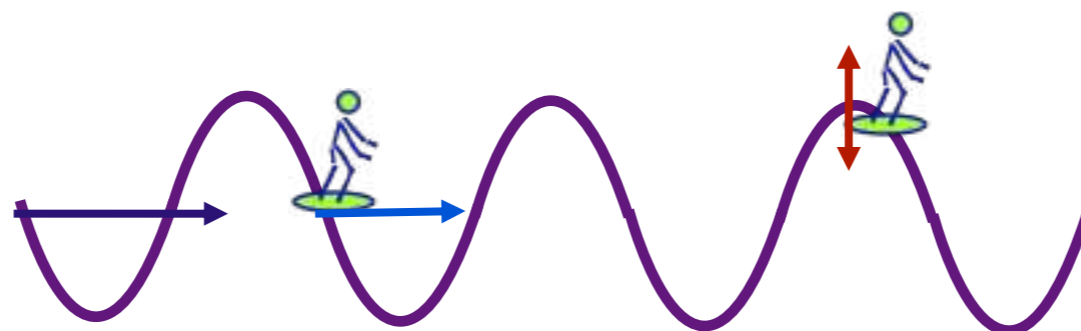


surfer with enough
initial velocity



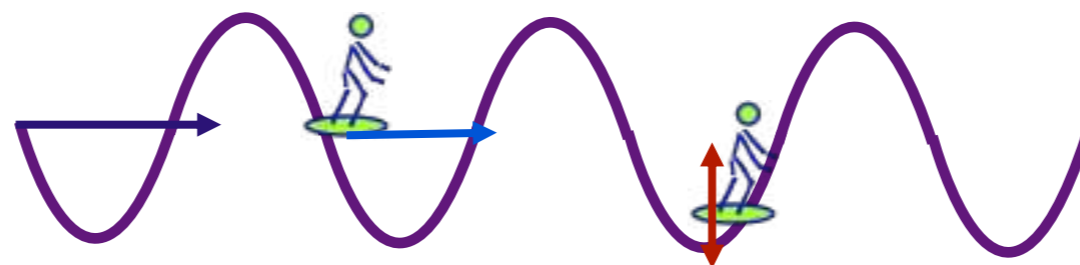
surfer initially at rest

surfer with enough
initial velocity



surfer initially at rest

surfer with enough
initial velocity



surfer initially at rest

Trapping energy : analogy electron/surfer



Single electron dynamic in a plasma wave:



For a sinusoidal plasma wave, plasma wave, $\delta n = \delta n_e \sin(k_p z - \omega_p t)$ where ω_p and k_p are the angular frequency and the wave number of the plasma wave.

This density perturbation leads to a perturbation of the electric field $\delta \vec{E}$ via the Poisson equation

$$\vec{\nabla} \cdot \delta \vec{E} = -\frac{\delta n e}{\epsilon_0}$$

This gives

$$\delta \vec{E}(z, t) = \frac{\delta n_e e}{k_p \epsilon_0} \cos(k_p z - \omega_p t) \vec{e}_z$$

Because we want to describe the electron acceleration to relativistic energies by a plasma wave, we consider now a plasma wave with a phase velocity is close to the speed of light $v_p = \omega_p / k_p \sim c$. Let $E_0 = m_e c \omega_{pe} / e$. The electric field becomes :

$$\delta \vec{E}(z, t) = E_0 \frac{\delta n_e}{n_e} \cos(k_p z - \omega_p t) \vec{e}_z$$

One notice that the electric field is dephased by $-\pi/4$ with respect to the electron density.

Single electron dynamic in a plasma wave:



Let's now describe the evolution of an electron placed in the electric field. The goal is to obtain the required conditions for trapping to occur.

The following variables are introduced to describe the electron in the laboratory frame : z the position, t the associated time, β the velocity normalized to c , $\gamma = 1/\sqrt{1 - \beta^2}$ the associated Lorentz's factor.

In plasma wave frame z' , t' , β' and γ' represent the equivalent quantities.

The plasma wave frame is in uniform constant translation at speed $v_p = \beta_p c$. One writes γ_p the Lorentz's factor associated to this velocity.

The Lorentz's transform allows to switch from the laboratory frame to the

wave frame :

$$z' = \gamma_p(z - v_p t)$$
$$ct' = \gamma_p(ct - x \times v_p/c)$$
$$\gamma' = \gamma\gamma_p(1 - \vec{\beta} \cdot \vec{\beta}_p)$$

In the new frame, the electric field remains unchanged $\delta\vec{E}'$

$$\delta\vec{E}'(z') = \delta\vec{E}(z, t) = E_0 \frac{\delta n_e}{n_e} \cos(k_p z' / \gamma_p) \vec{e}_z \quad \text{and} \quad \vec{F}' = -e\delta\vec{E}' \equiv -\vec{\nabla}'\Phi'$$

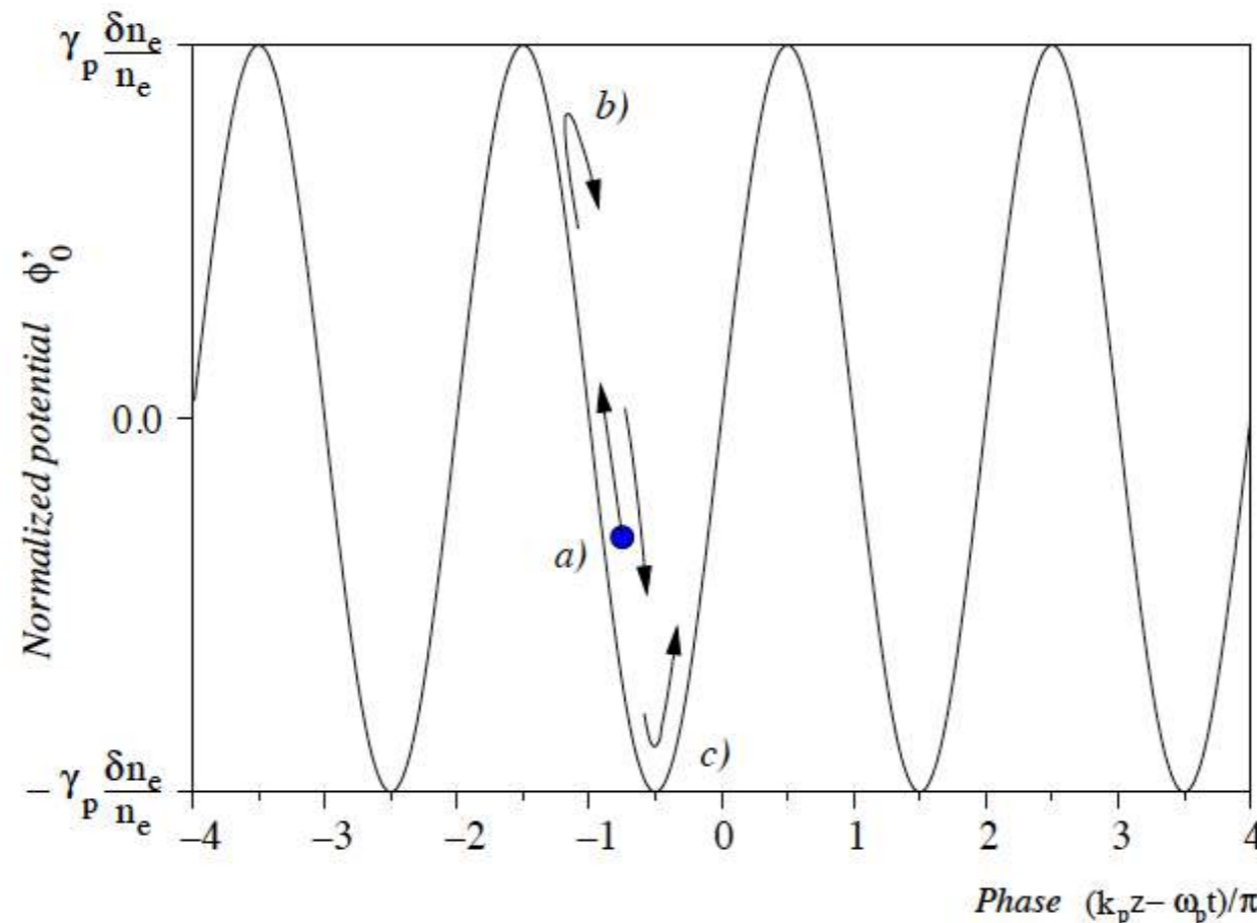
Single electron dynamic in a plasma wave:



This leads to $\Phi'(z') = mc^2 \gamma_p \frac{\delta n_e}{n_e} \sin(k_p z' / \gamma_p) \equiv mc^2 \phi'(z')$

The total energy conservation for the particle in this frame compared to the initial energy at the injection time (labelled with subscript 0) gives:

$$\gamma'(z') + \phi'(z') = \gamma'(z'_0) + \phi'(z'_0)$$



Trajectory of an electron injected in the potential of the plasma wave in the frame of the wave. The letters correspond to the instant when : a) the electron is injected in the wave, b) the electron travels at the speed of the plasma wave, c) the electron has the maximal velocity and enters the decelerating part of the wave.

Single electron dynamic in a plasma wave:



Conservation energy equation gives the relation between the electron energy and its position in the plasma wave. The previous figure illustrates the motion of an electron injected in this potential. Finally, we perform the reverse Lorentz's transform to give this energy in the laboratory frame.

For $\beta' > 0$, the scalar product $\vec{\beta} \cdot \vec{\beta}_p$ is positive, then :

$$\gamma = \gamma' \gamma_p + \sqrt{\gamma'^2 - 1} \sqrt{\gamma_p^2 - 1}$$

For $\beta' < 0$, the scalar product $\vec{\beta} \cdot \vec{\beta}_p$ is negative, then :

$$\gamma = \gamma' \gamma_p - \sqrt{\gamma'^2 - 1} \sqrt{\gamma_p^2 - 1}$$

This separatrix gives the minimum and maximum energies for trapped particles. This is comparable to the hydrodynamic case, where a surfer has to crawl to gain velocity and to catch the wave. In terms of relativistic factor, γ has to belong to the interval $[\gamma_{min}; \gamma_{max}]$ with :


$$\gamma_{min} = \gamma_p(1 + 2\gamma_p\delta) - \sqrt{\gamma_p^2 - 1} \sqrt{(1 + 2\gamma_p\delta)^2 - 1}$$

$$\gamma_{max} = \gamma_p(1 + 2\gamma_p\delta) + \sqrt{\gamma_p^2 - 1} \sqrt{(1 + 2\gamma_p\delta)^2 - 1}$$

where $\delta = \delta n_e / n_e$ is the relative amplitude of the density perturbation.

Single electron dynamic in a plasma wave:





$m_e = m_0 + \delta m_e$

$$\vec{m} = \delta m_e \cos(k_p z - \omega_p t) \hat{z}$$

$$\nabla \cdot (\delta \vec{E}) = -\frac{\delta m_e}{\epsilon_0}$$

$$\int \delta \vec{E} \cdot d\vec{l} = \frac{\delta m_e}{\epsilon_0} \cos(k_p z - \omega_p t) \hat{z} = \frac{\delta m_e c}{\epsilon_0 k_p} \cos(k_p z - \omega_p t)$$

$$E_0 = \frac{m_0 c \omega_p}{e} \quad \delta \vec{E} = \left(\frac{e \omega_p}{\epsilon_0 k_p} \times \frac{m_0 \omega_p}{m_e c} \right) \delta m_e \cos(k_p z - \omega_p t) \hat{z}$$

$$\omega_p^2 = \frac{n e^2}{m \epsilon_0} \quad v_p = \frac{c \omega_p}{\omega}$$

$$\frac{\delta E(z,t)}{\omega_p} \frac{m_0 \omega_p^2}{c} \frac{c}{e} \frac{\delta m_e}{n} = E_0 \frac{\delta m_e}{n_e} \cos(k_p z - \omega_p t)$$

Frame \rightarrow labor Lorentz transform

Frame \rightarrow plasma wave

$$z' = \gamma_p (z - v_p t)$$

$$t' = \gamma_p (t - z \frac{v_p}{c^2})$$

$$\delta = \gamma_p \delta_p (1 - \beta \cdot \beta_p)$$

$$\delta E'(z') = \delta E(z) = E_0 \frac{\delta m_e}{n_e} \cos\left(\frac{k_p z'}{\delta}\right) \hat{z}$$

$$\vec{F} = -e \delta \vec{E}' = -\nabla \phi' \Rightarrow \frac{e \epsilon_0}{k_p} \frac{\delta m_e}{n_e} \sin\left(\frac{k_p z'}{\delta}\right) \hat{z} = \phi' + \delta \frac{m_0 \omega_p^2 c^2}{\omega_p^2}$$

$$\phi'(z') = m c^2 \frac{\delta m_e}{n_e} \sin\left(\frac{k_p z'}{\delta}\right) = m c^2 \phi(z')$$

$$\delta(z) + \phi(z) = \delta(z_0) + \phi(z_0)$$

$$E_0 = \frac{m_0 \omega_p c}{e}$$

ϕ' normalized potential

$$\phi' = \frac{\phi}{m c^2}$$

Reverse Lorentz

$$\delta = \delta_p + \beta' \cdot \beta_p$$

$$\gamma' = \gamma_p \delta \sin(k_p x') = \omega t$$

$$\delta_p = \delta_p \gamma_p = (\gamma^2 - 1) \left(\frac{v_p}{c} \right)$$

$$\gamma' = 1 + \delta \gamma_p \delta$$

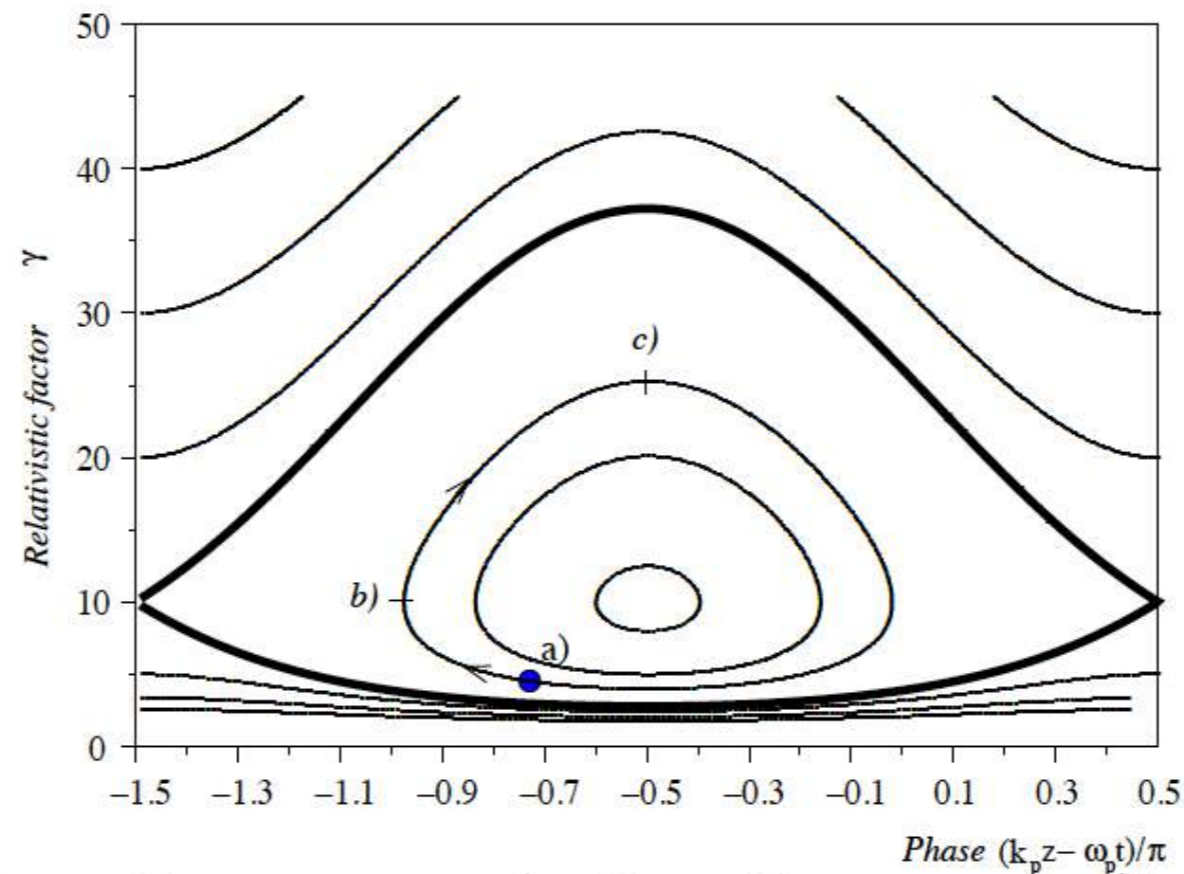
$$\gamma'_+ = 1 + 2 \delta \gamma_p \delta$$

Single electron dynamic in a plasma wave:



One deduces that the maximum energy gain ΔW_{max} for a trapped particle is reached for a closed orbit with maximum amplitude. This corresponds to the injection at γ_{min} on the separatrix and its extraction at γ_{max} . The maximum energy gain is then written $\Delta W_{max} = (\gamma_{max} - \gamma_{min})mc^2$

At low density $n_e \ll n_c$, one has $\gamma_p = \omega_0/\omega_p \gg 1$ and $\Delta W_{max} = 4\gamma_p^2 \frac{\delta n_e}{n_e} mc^2$



Electron trajectory in a plasma wave in the phase space $(k_p z - \omega_p t, \gamma)$ for $\gamma_p = 10$ and $\delta n_e/n_e = 0.05$. The thick line represents the separatrix. Closed orbits are trapped trajectories and open orbits are untrapped trajectories. The letters match the instants defined in caption of the previous figure

Outline

- Part I : Motivation, basis and principle
- Part II : External and Self-Injection in Laser Wakefield
- Part III : High quality electron beams in LPA with the colliding pulses scheme
- Part IV : Applications, conclusion and perspectives

Part II : External and Self-Injection in LWF

- External injection : Laser wakefield and Beatwave experiments
- Self-injection : Self-Modulated Laser and Forced Wakefield
- Bubble regime
- Ionisation Injection, Gradient and Longitudinal injection

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Laser Electron Accelerator

T. Tajima and J. M. Dawson

Department of Physics, University of California, Los Angeles, California 90024

(Received 9 March 1979)

An intense electromagnetic pulse can create a weak of plasma oscillations through the action of the nonlinear ponderomotive force. Electrons trapped in the wake can be accelerated to high energy. Existing glass lasers of power density 10^{18}W/cm^2 shone on plasmas of densities 10^{18}cm^{-3} can yield gigaelectronvolts of electron energy per centimeter of acceleration distance. This acceleration mechanism is demonstrated through computer simulation. Applications to accelerators and pulsers are examined.

Such a wake is most effectively generated if the length of the electromagnetic wave packet is half the wavelength of the plasma waves in the wake:

=> Laser wakefield

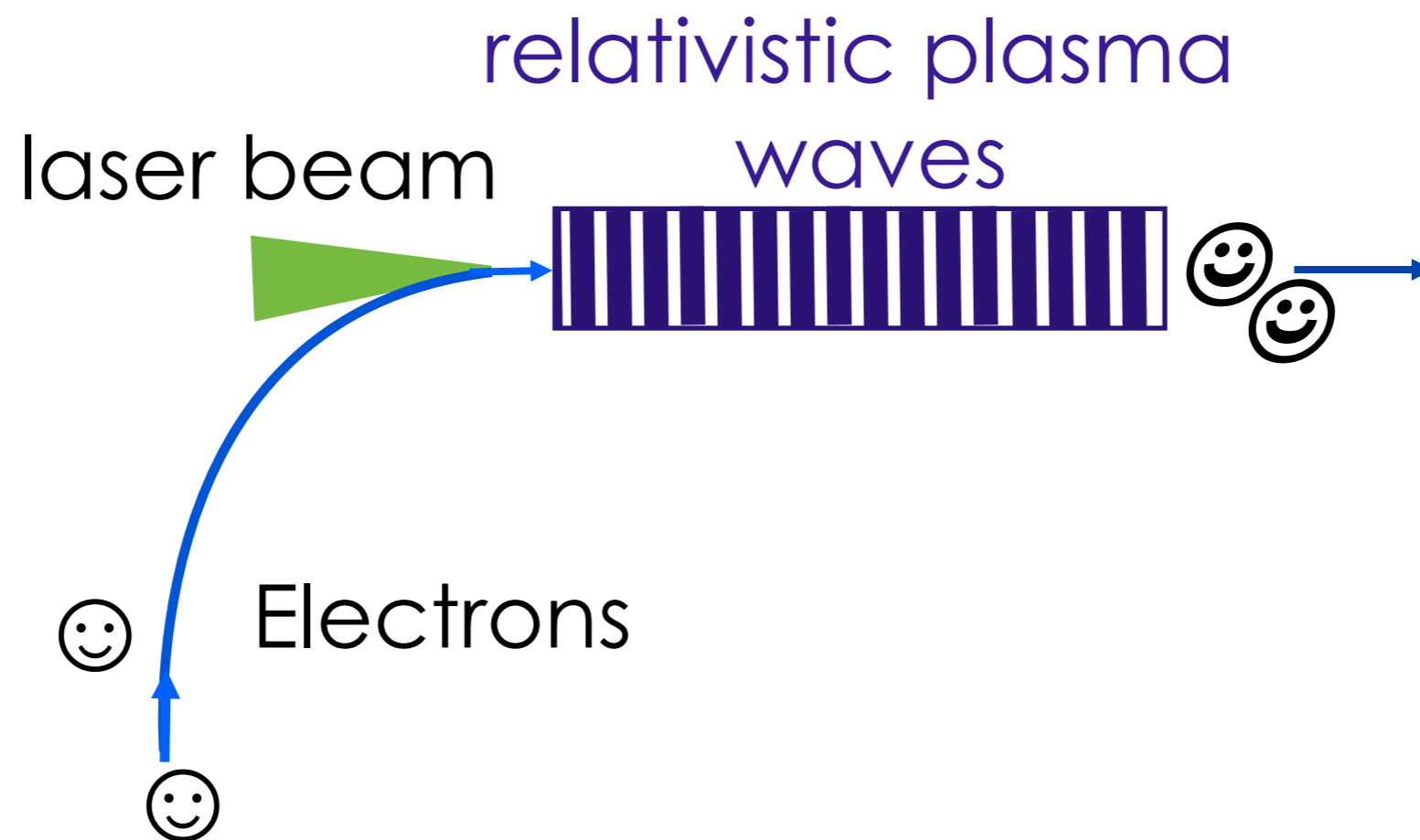
$$L_t = \lambda_w / 2 = \pi c / \omega_p. \quad (2)$$

An alternative way of exciting the plasmon is to inject two laser beams with slightly different frequencies (with frequency difference $\Delta \omega \sim \omega_p$) so that the beat distance of the packet becomes $2\pi c / \omega_p$. The mechanism for generating the wakes

=> Laser beatwave

External injection of electrons in LBW

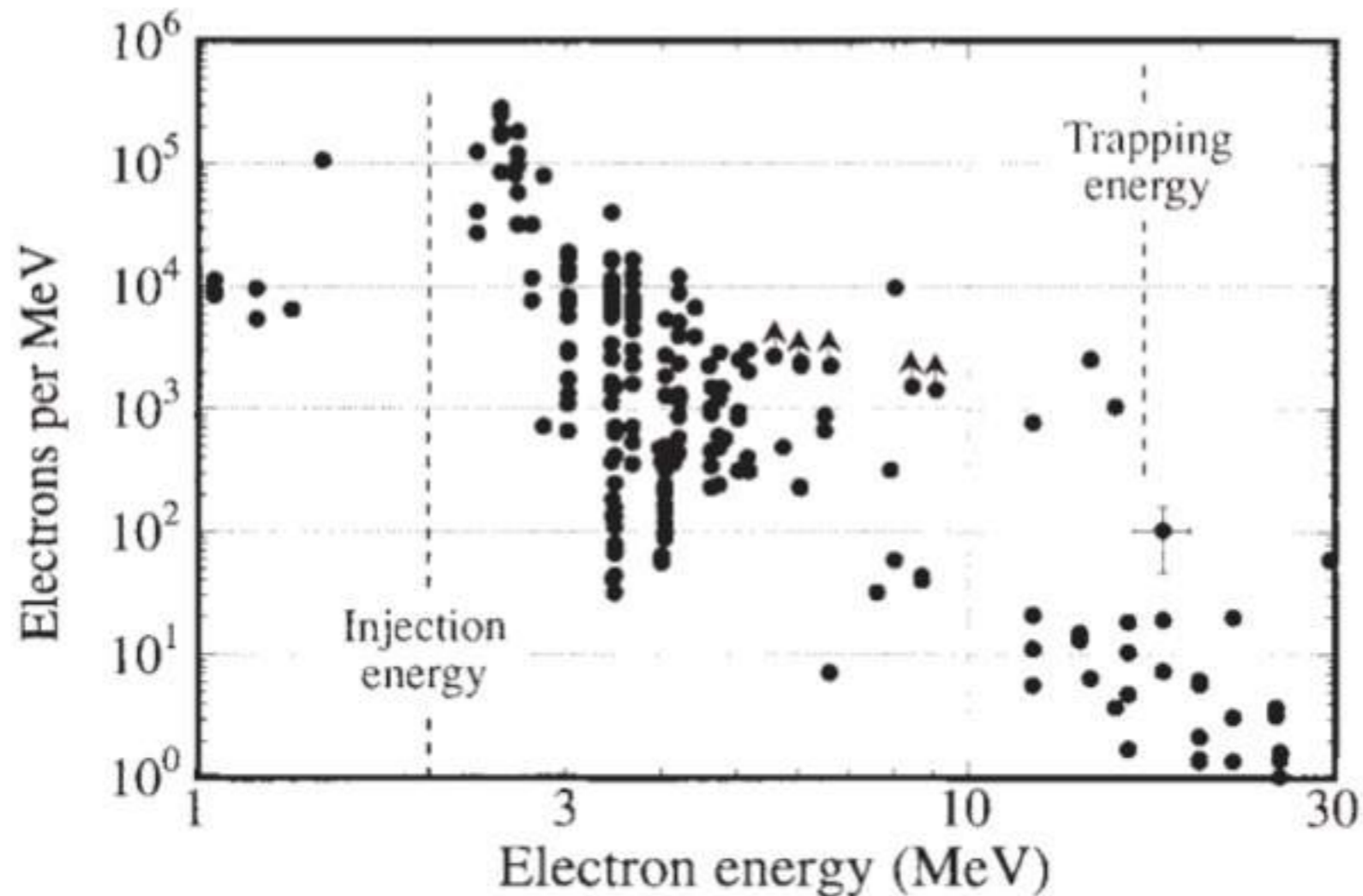
Scheme of principle of the first experiments :
the laser Beat Wave (LBW)



1992-1994 Accelerated electrons in LBWF



The 2-MeV electrons are accelerated up to ≈ 28 MeV
Electron spectra indicate an E_{field} of ≈ 2.8 GV/m



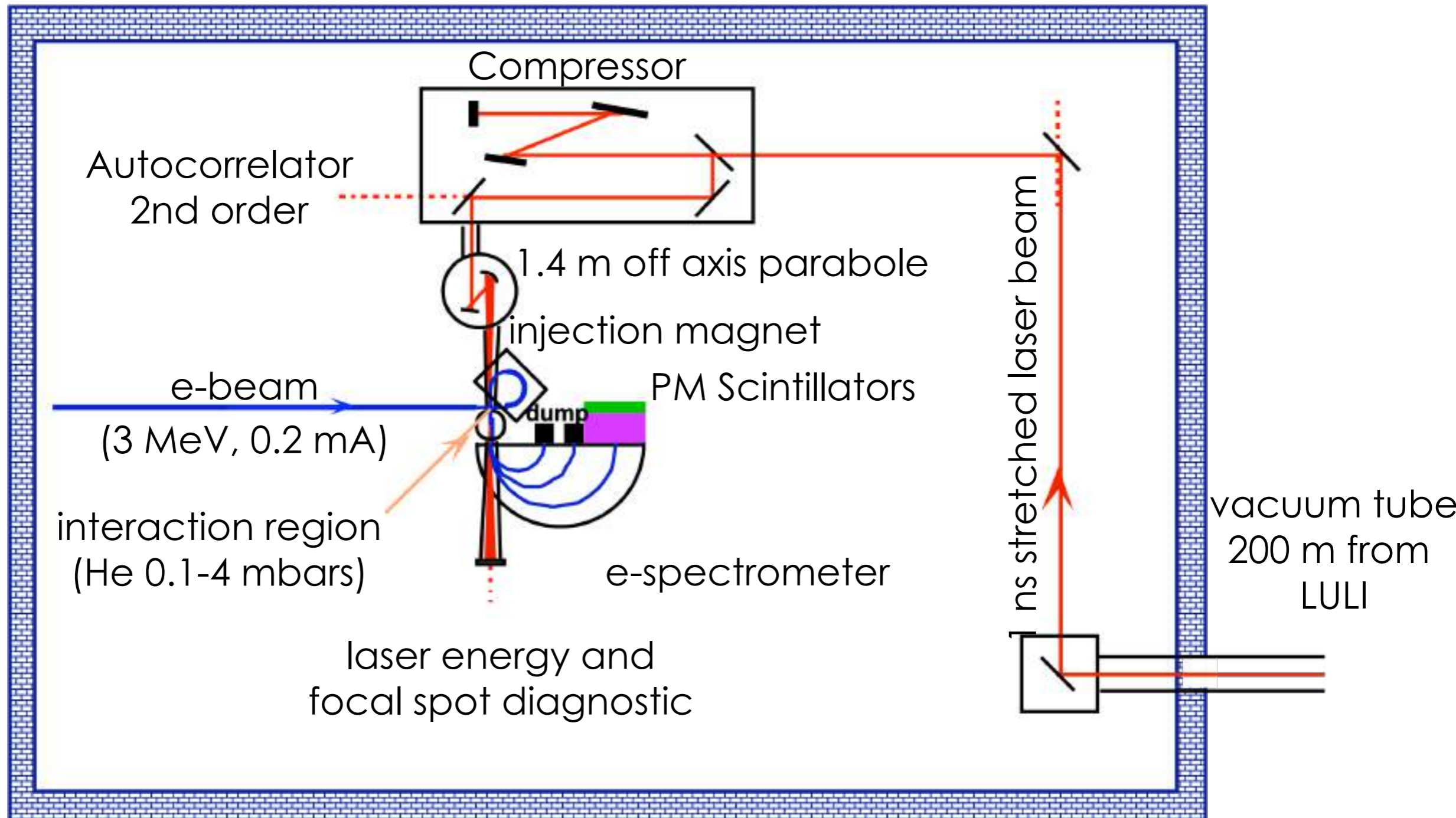
M. Everett *et al.*, Nature 1994

Electron gain demonstration Few MeV's:

Kitagawa *et al.* PRL 1992, Clayton *et al.* PRL 1993, N. A. Ebrahim *et al.*, J. Appl. Phys. 1994, Amiranoff *et al.* PRL 1995



Electron spectra indicate an E_{field} of $\approx 1 \text{ GV/m}$

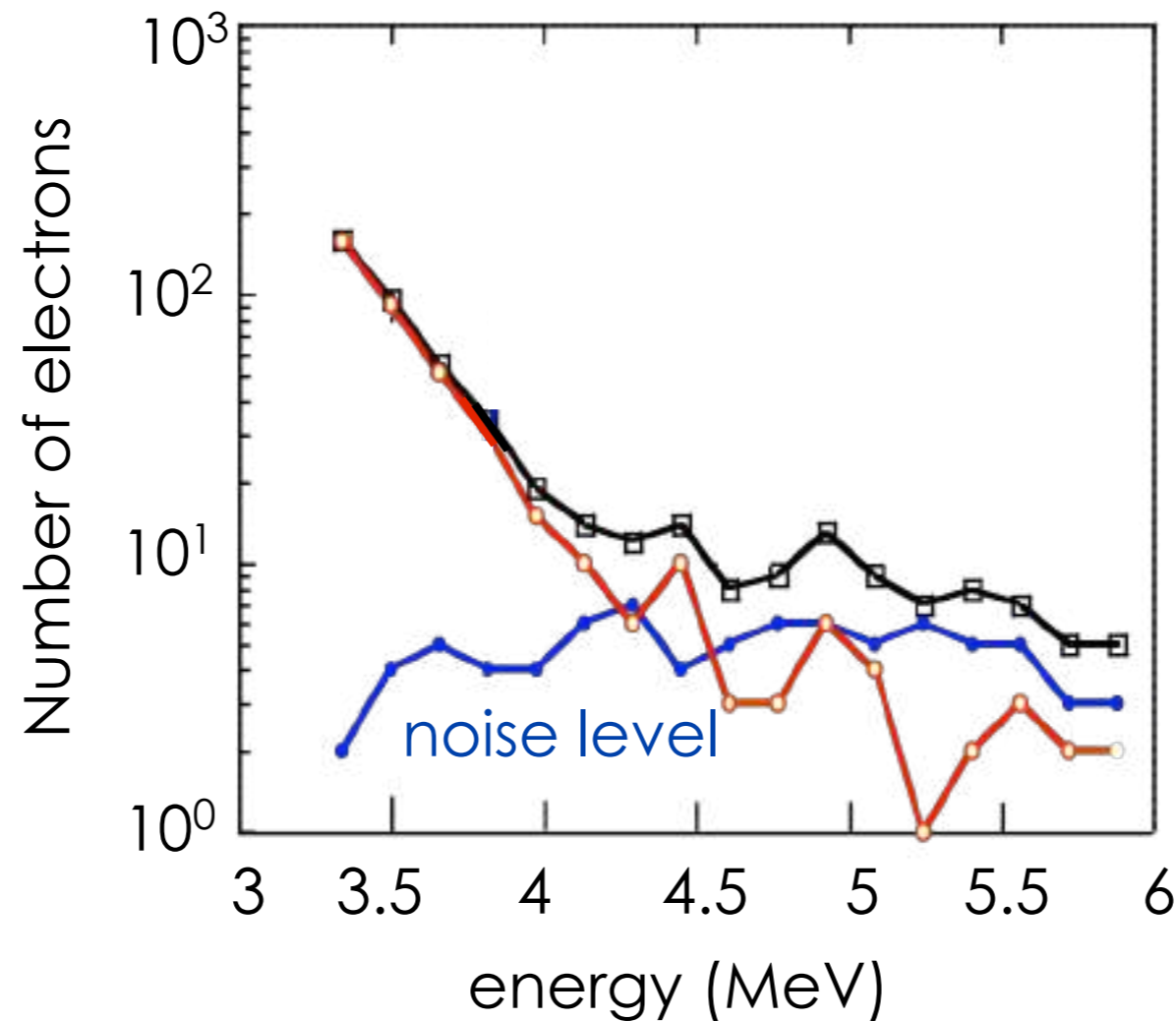


1998 Accelerated electrons in LWF



LULI/LPNHE/LSI/IC

The 3-MeV electrons are accelerated up to ≈ 4.5 MeV
Electron spectra indicate an E_{field} of ≈ 1.4 GV/m



2.5 J, 350 fs, 10^{17} W/cm², 0.5 mbar of He

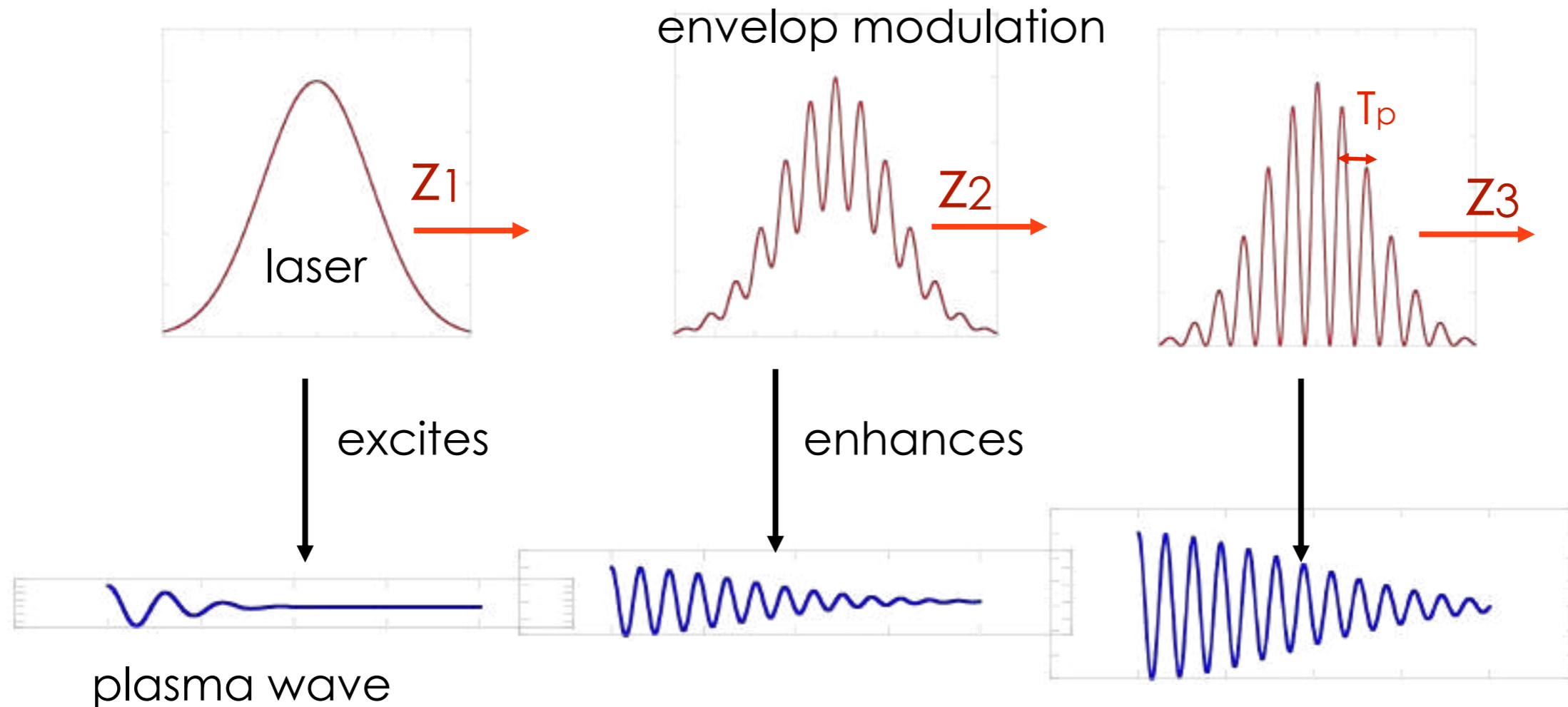
F. Amiranoff *et al.*, PRL 1998

Part II : External and Self-Injection in LWF

- External injection : Laser wakefield and Beatwave experiments
- Self-injection : Self-Modulated Laser and Forced Wakefield
- Bubble regime
- Ionisation Injection, Gradient and Longitudinal injection

1992 How to excite a plasma wave: The SMLWF

Self modulated laser wakefield scheme : $cT_{\text{laser}} \gg T_p$
(Andreev *et al.*, Antonsen *et al.*, Sprangle *et al.* 1992)



$P_L > P_c(\text{GW}) = 17 n_c/n_e$ then wavebreaking can occur

The Relativistic self focusing

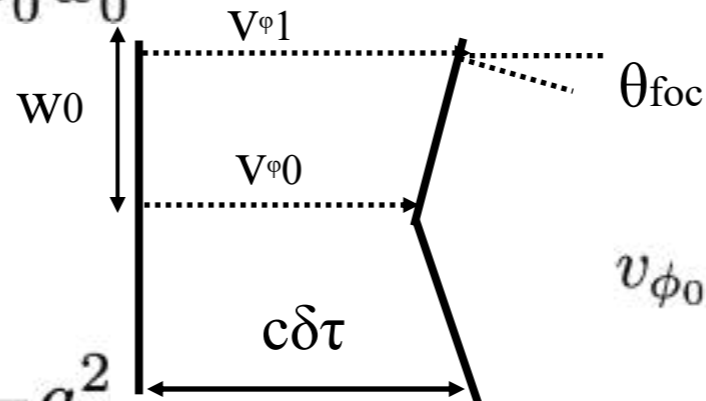


For a gaussian beam, in vacuum near the focus : $w = w_0(1 + t^2/t_R^2)^{1/2}$

Diffraction : $\frac{d^2w}{c^2 d\tau^2} |_{diff.} = \frac{w_0}{z_R^2} = \frac{4c^2}{\omega_0^2 w_0^3}$

Relativistic self focusing :

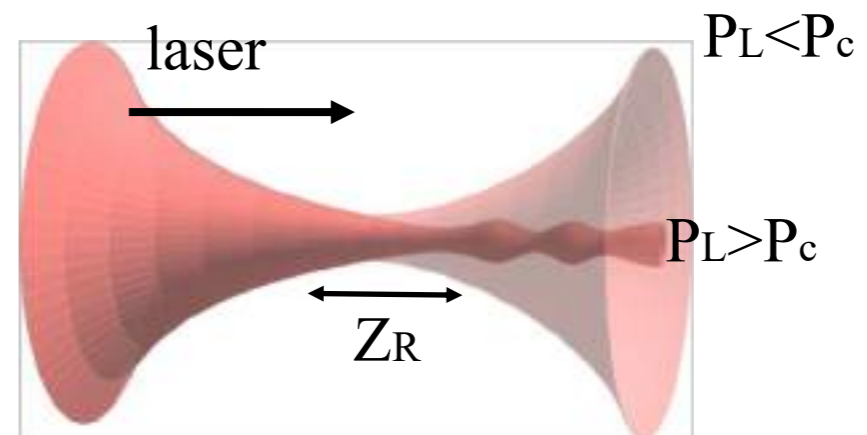
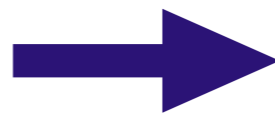
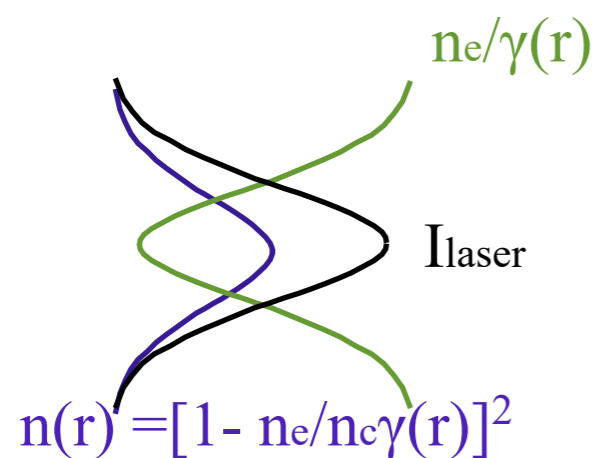
$\frac{d^2w}{c^2 d\tau^2} |_{foc.} = -\frac{v_{\phi 1} - v_{\phi 0}}{w_0} = \frac{\omega_p^2}{8\omega_0^2 w_0} a_0^2$



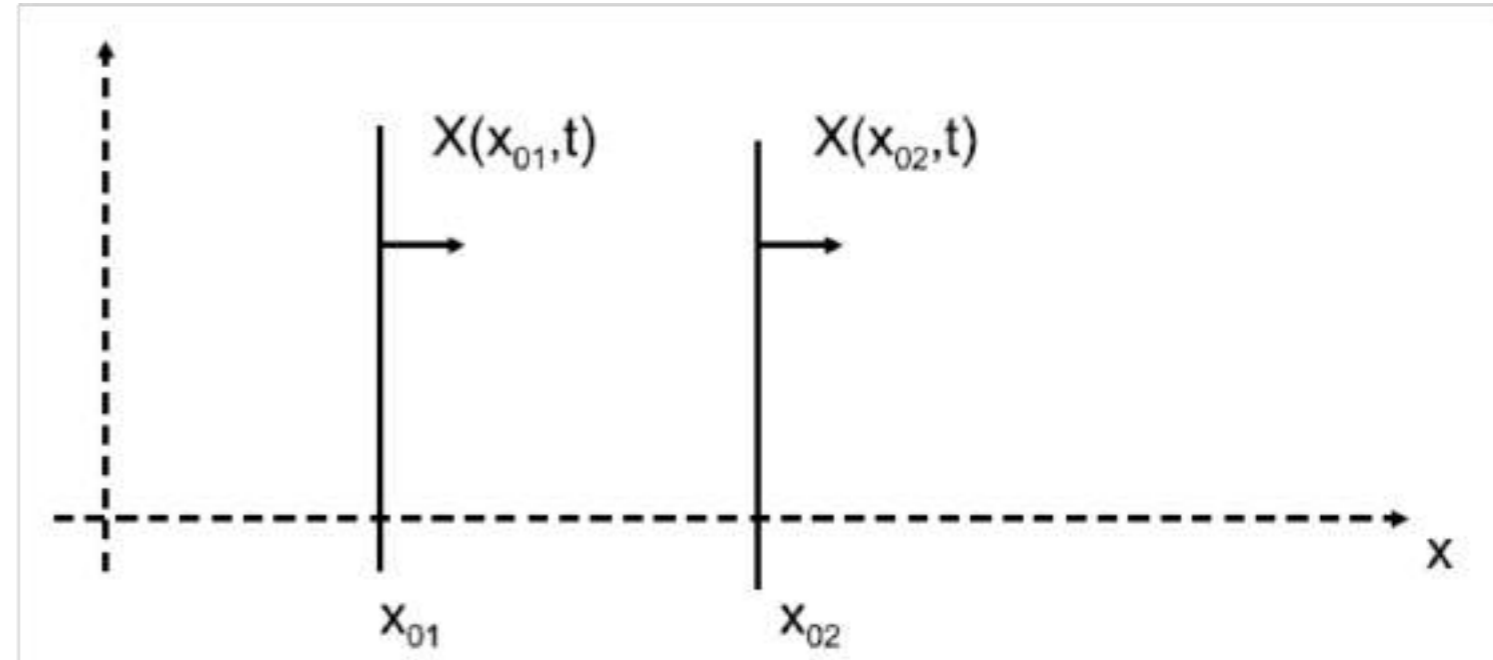
$v_{\phi 1} = c(1 + \omega_p^2/2\omega_0^2)$

$v_{\phi 0} = c[1 + \omega_p^2/2\omega_0^2(1 - a_0^2/4)]$

$\frac{\partial^2(w/w_0)}{c^2 \partial \tau^2} = \frac{w_0^3}{z_R^2 w^3} (1 - \frac{P}{P_c})$ with $P_c [GW] = 17 \frac{\omega_0^2}{\omega_p^2}$



Wave breaking

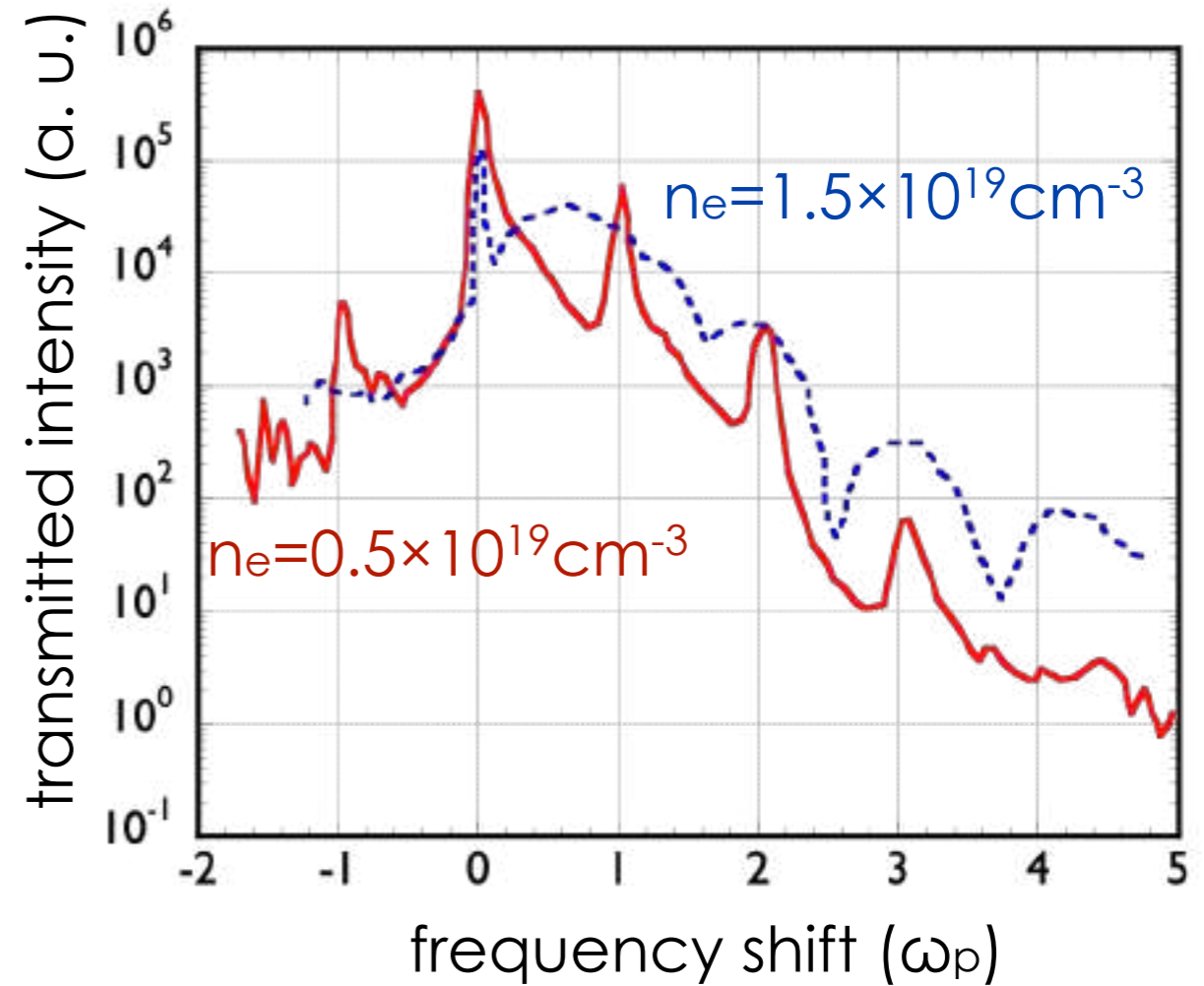
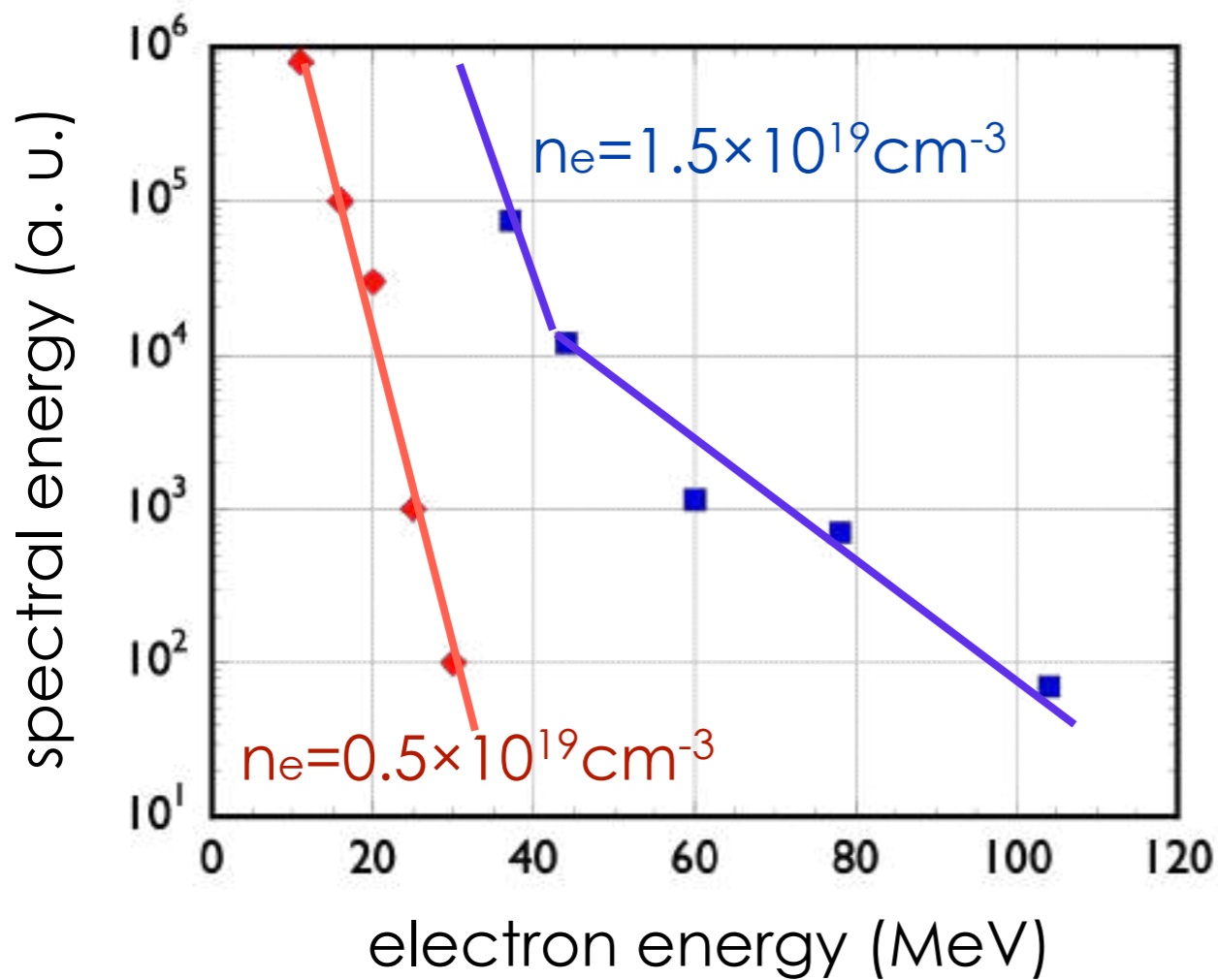


- 1D picture : slides of electrons oscillate at ω_p
- When the trajectories crossed each other: wavebreaking
- Which occurs when each slides displace by λ_p

Wave breaking



1995 Relativistic wave breaking (RAL/IC/UCLA/LULI)



- Multiple satellites : high amplitude plasma waves
- Broadening at higher densities
- Loss of coherence of the relativistic plasma waves

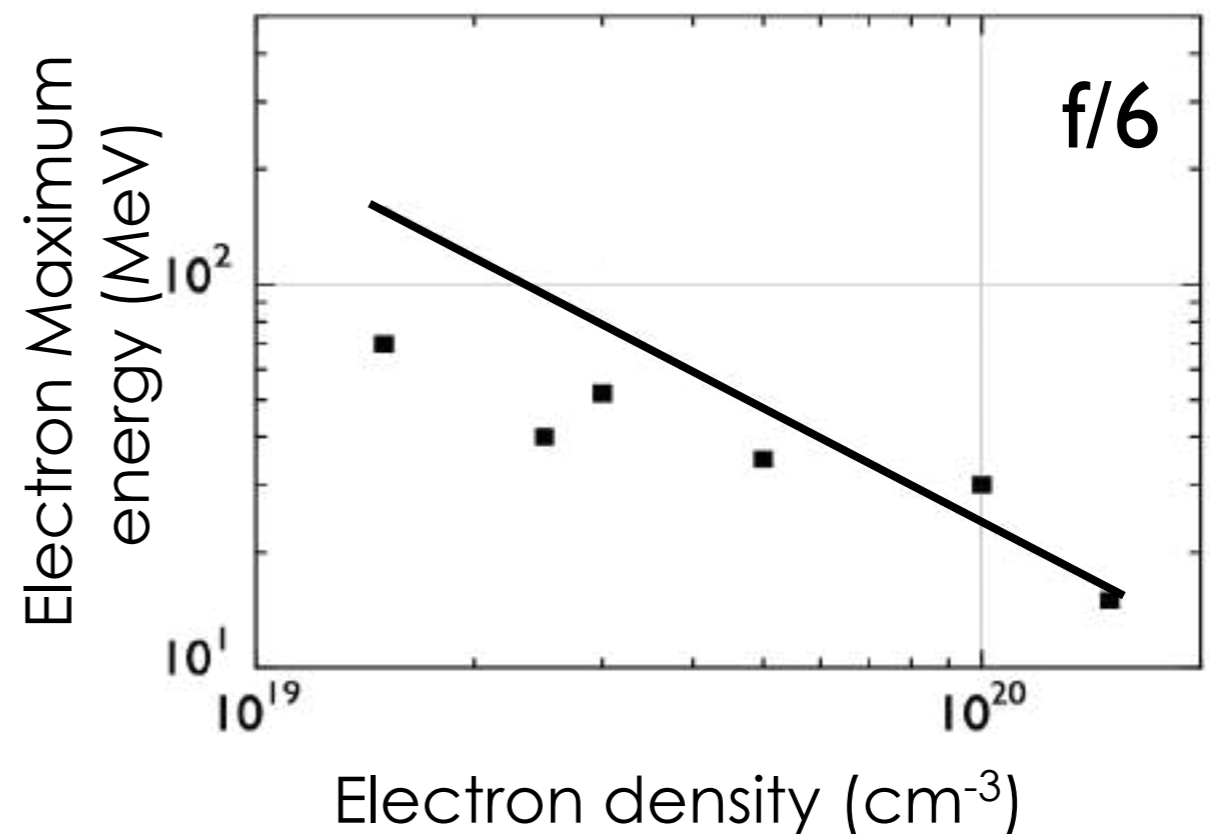
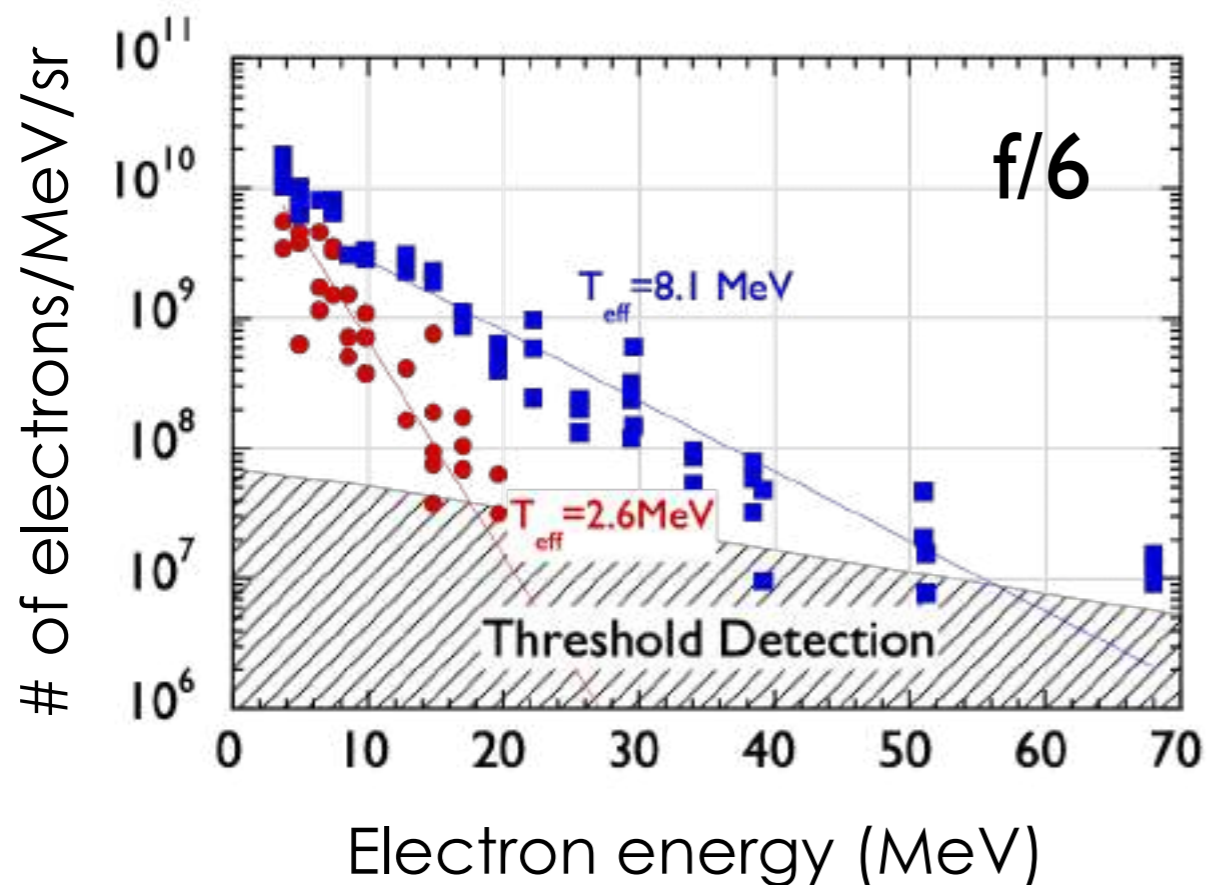
A. Modena et al., Nature (1995)

2001 SMLWF with 10 Hz laser



Spectra : E_{\max} increases when n_e decreases

Parameters: $n_e=5 \times 10^{19} \text{cm}^{-3}$ & $1.5 \times 10^{20} \text{cm}^{-3}$, $\tau_L=35 \text{fs}$, $E=0.6 \text{J}$, $I_L= 2 \times 10^{19} \text{W/cm}^2$

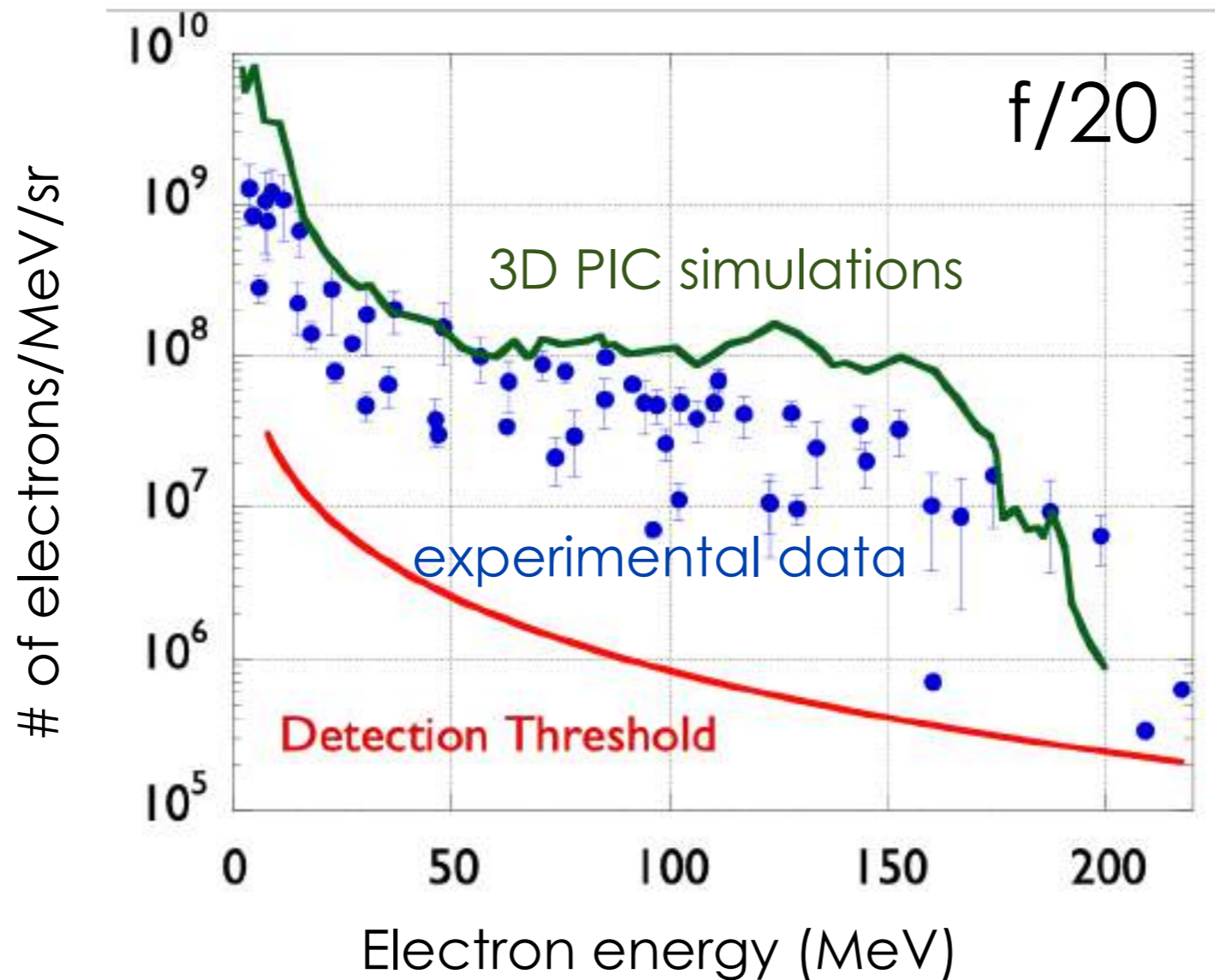


V. Malka et al., Phys. of Plasmas **8**, 6 (2001)

2002 The Forced Laser Wakefield: the NL regime



Parameters: $n_e=1.5 \times 10^{19} \text{cm}^{-3}$, $\tau_L=35 \text{fs}$, $E=0.6 \text{J}$, $I_L=1 \times 10^{18} \text{W/cm}^2$ with $k_p w_0 > 1$



V. Malka *et al.*, *Science* **298**, 1596 (2002)

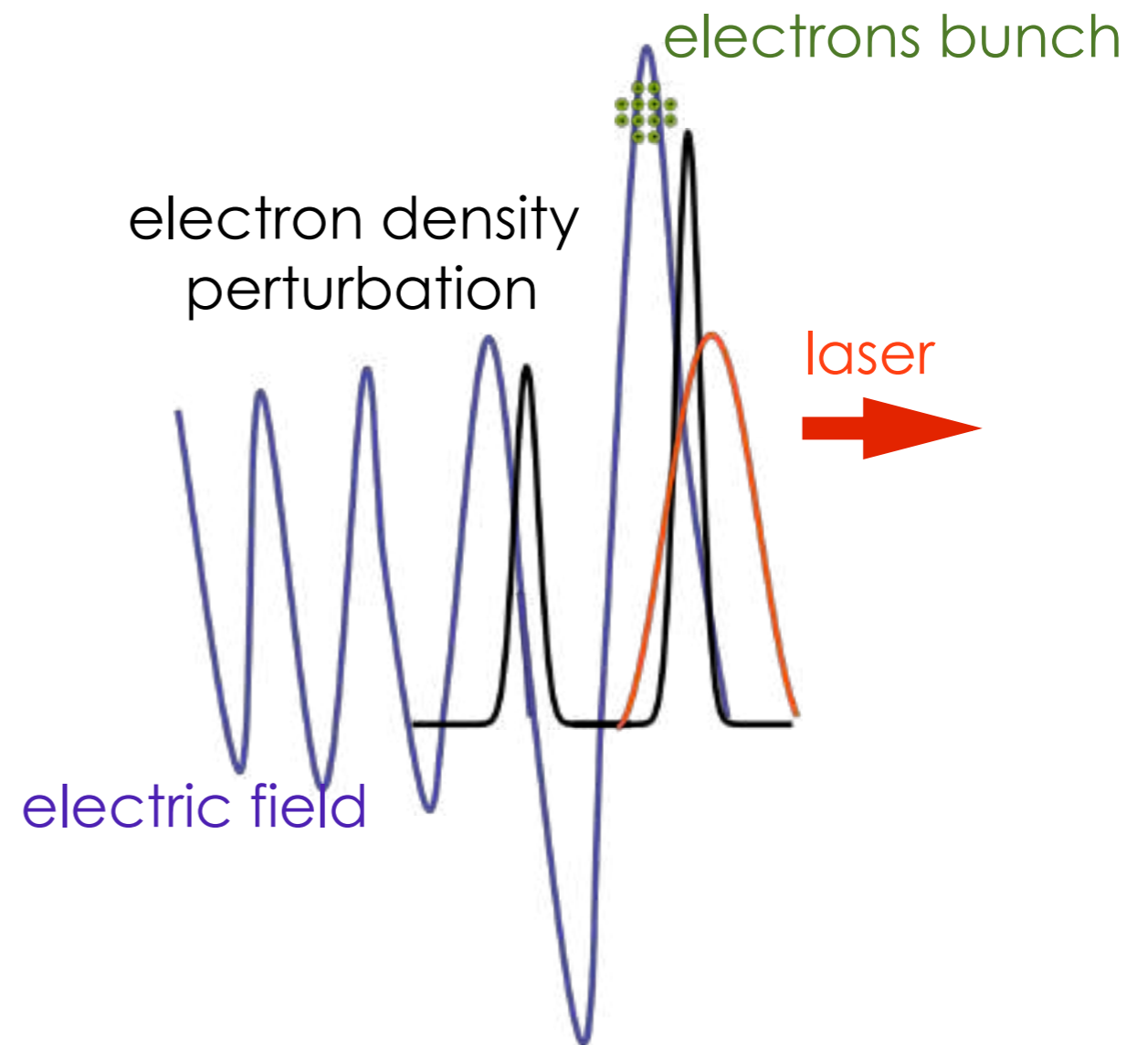
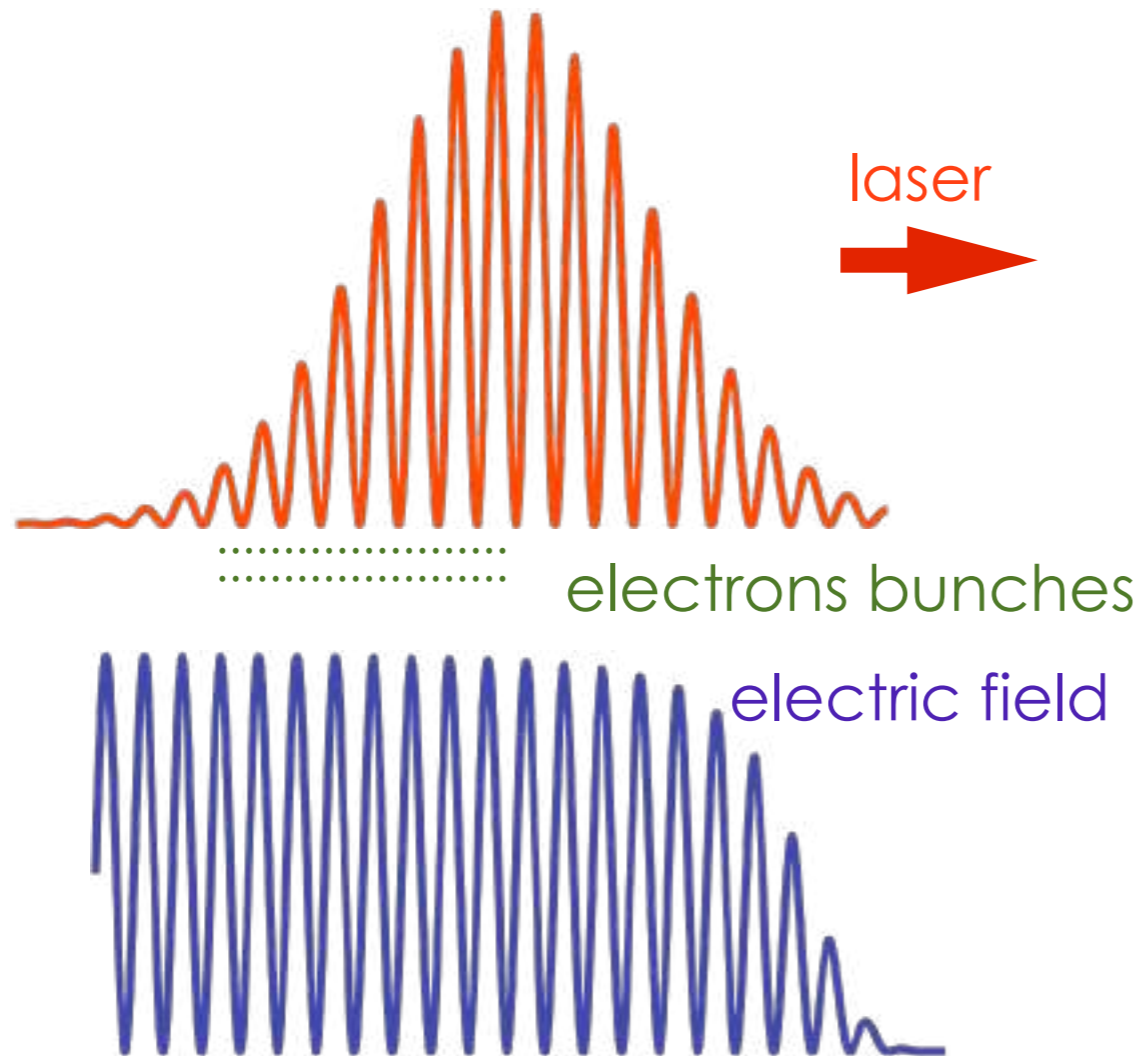
*CARE project

SMLWF / FLWF (ps/fs) : multiple/single bunch



SMLWF: $\omega_p \tau \gg 1$

FLWF: $\omega_p \tau \approx 1$

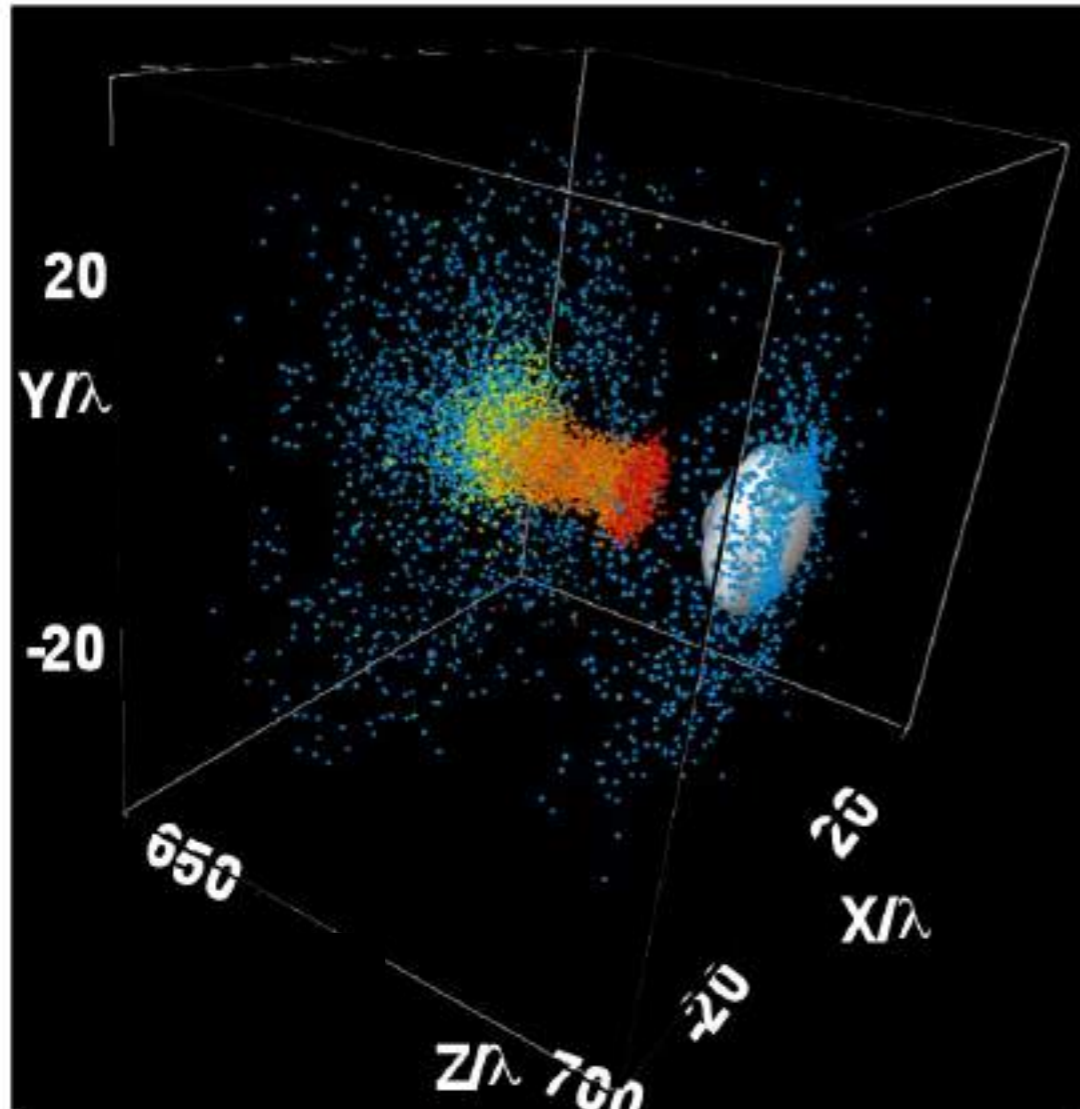


V. Malka, Europhysics News, April (2004)

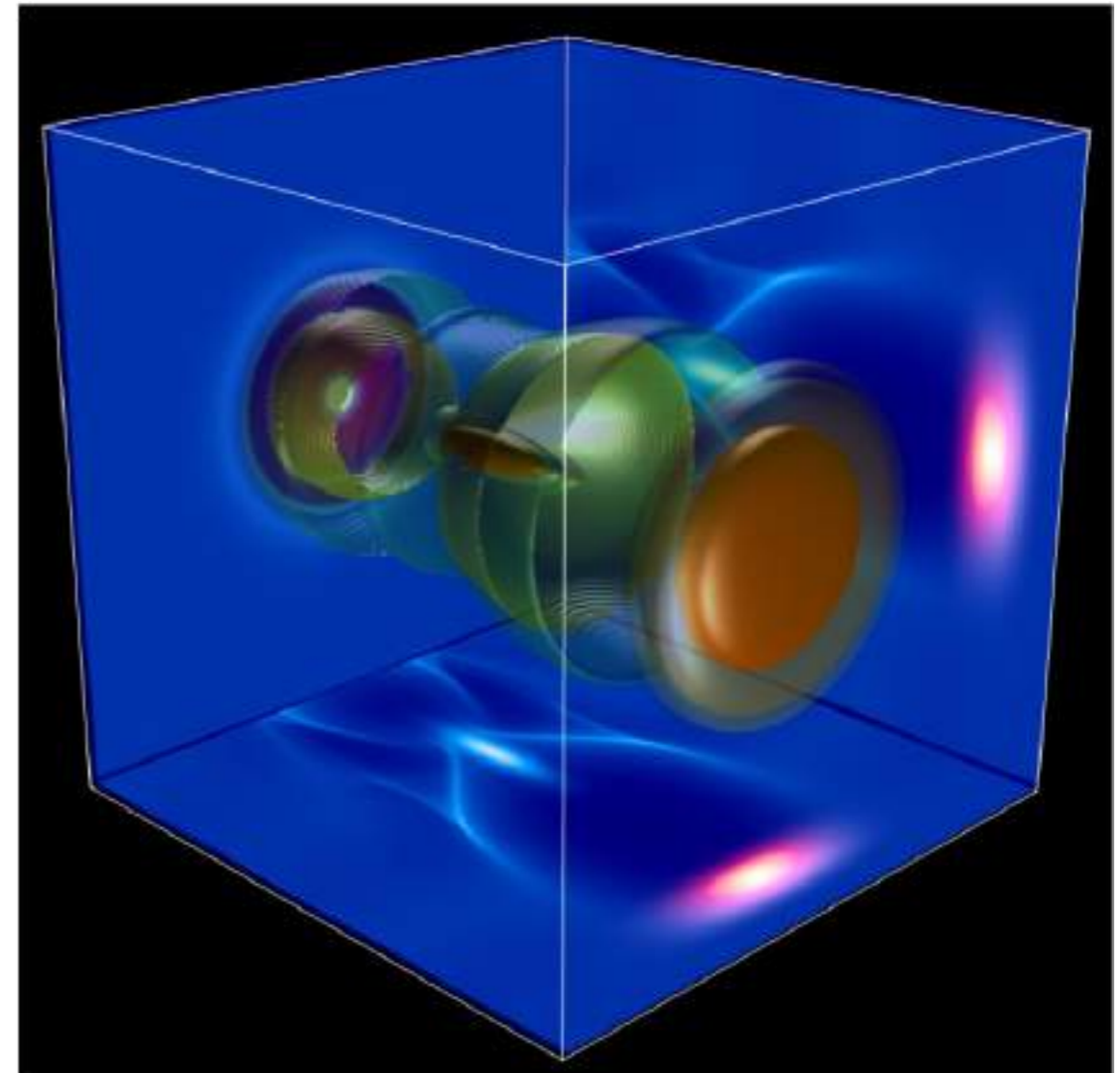
Part II : External and Self-Injection in LWF

- External injection : Laser wakefield and Beatwave experiments
- Self-injection : Self-Modulated Laser and Forced Wakefield
- Bubble regime
- Ionisation Injection, Gradient and Longitudinal injection

2002 The Bubble regime



VLPL, courtesy of A. Pukhov



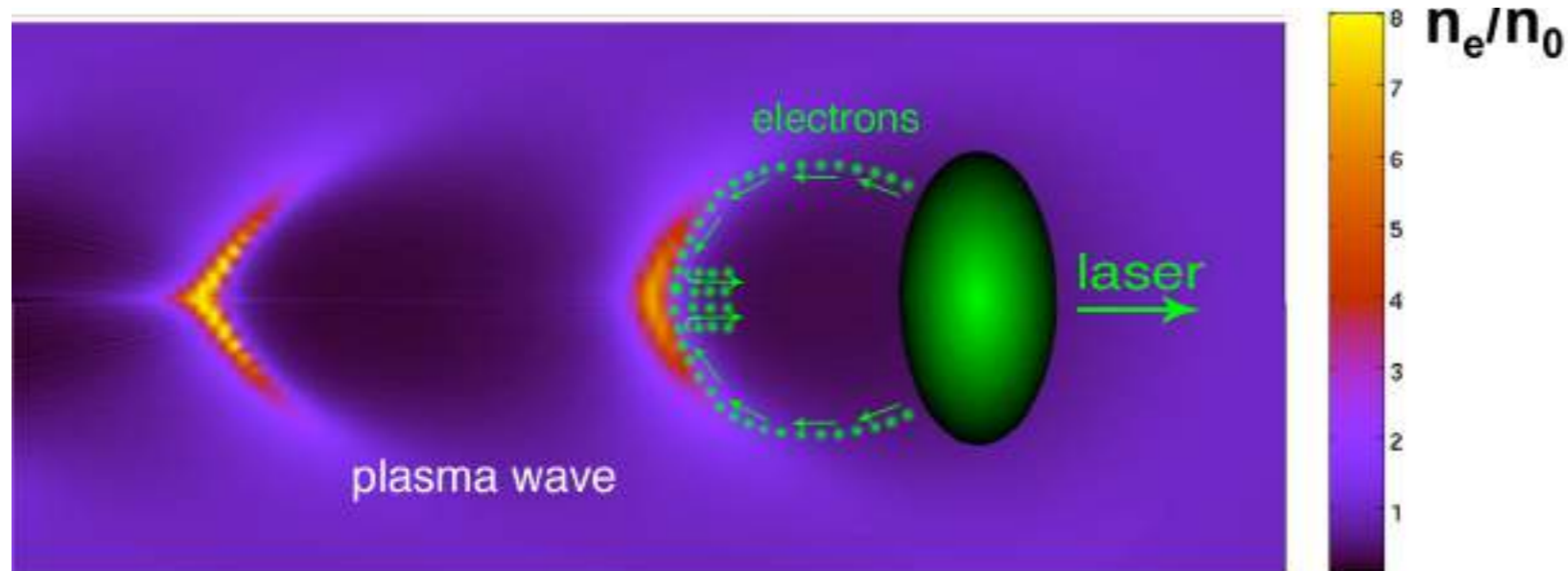
Golp, courtesy of L. Silva

A.Pukhov & J.Meyer-ter-Vehn, *Appl. Phys. B*, **74** (2002)

Bubble/blow-out regime : principle



Highly non-linear regime : self-injection

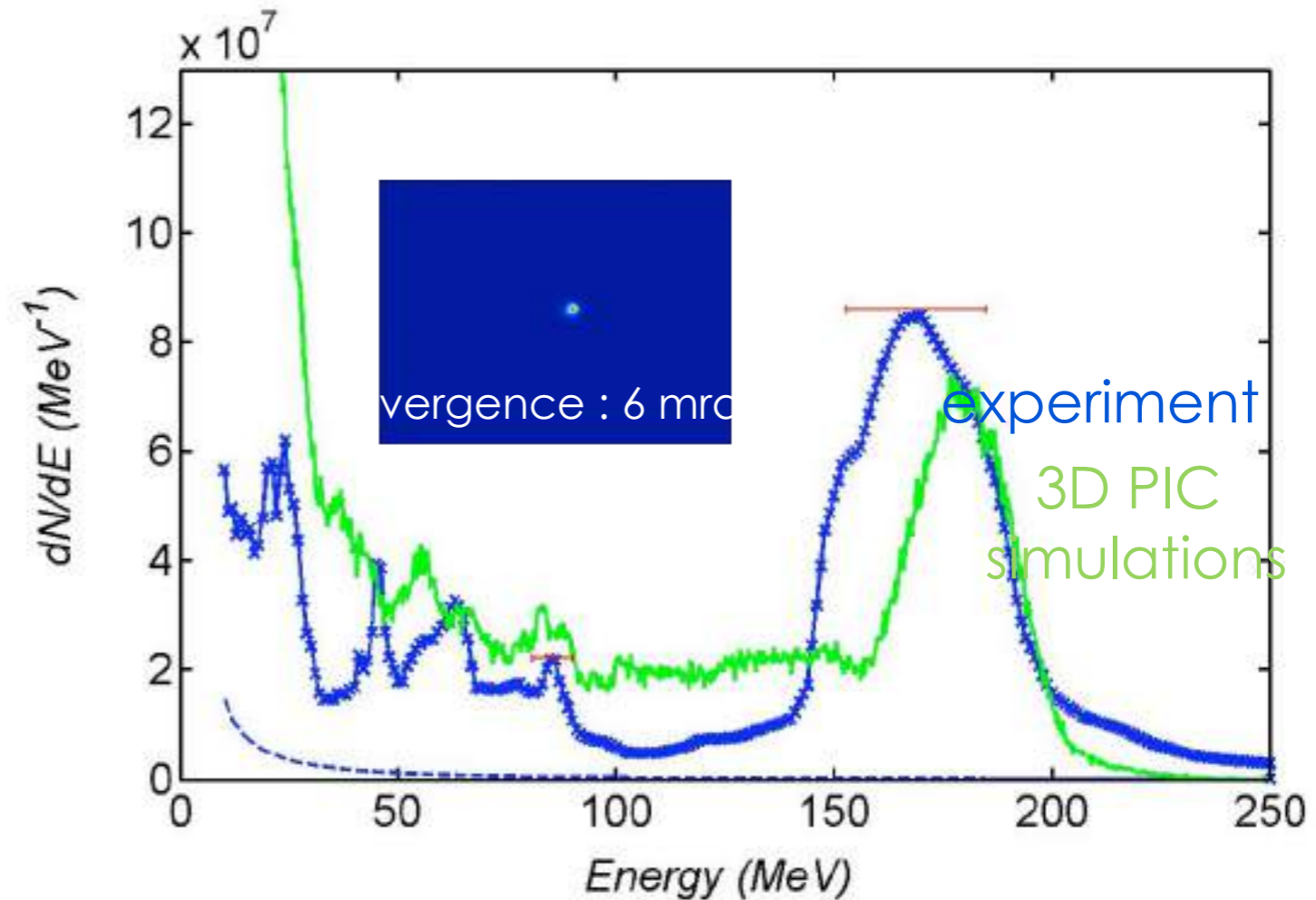
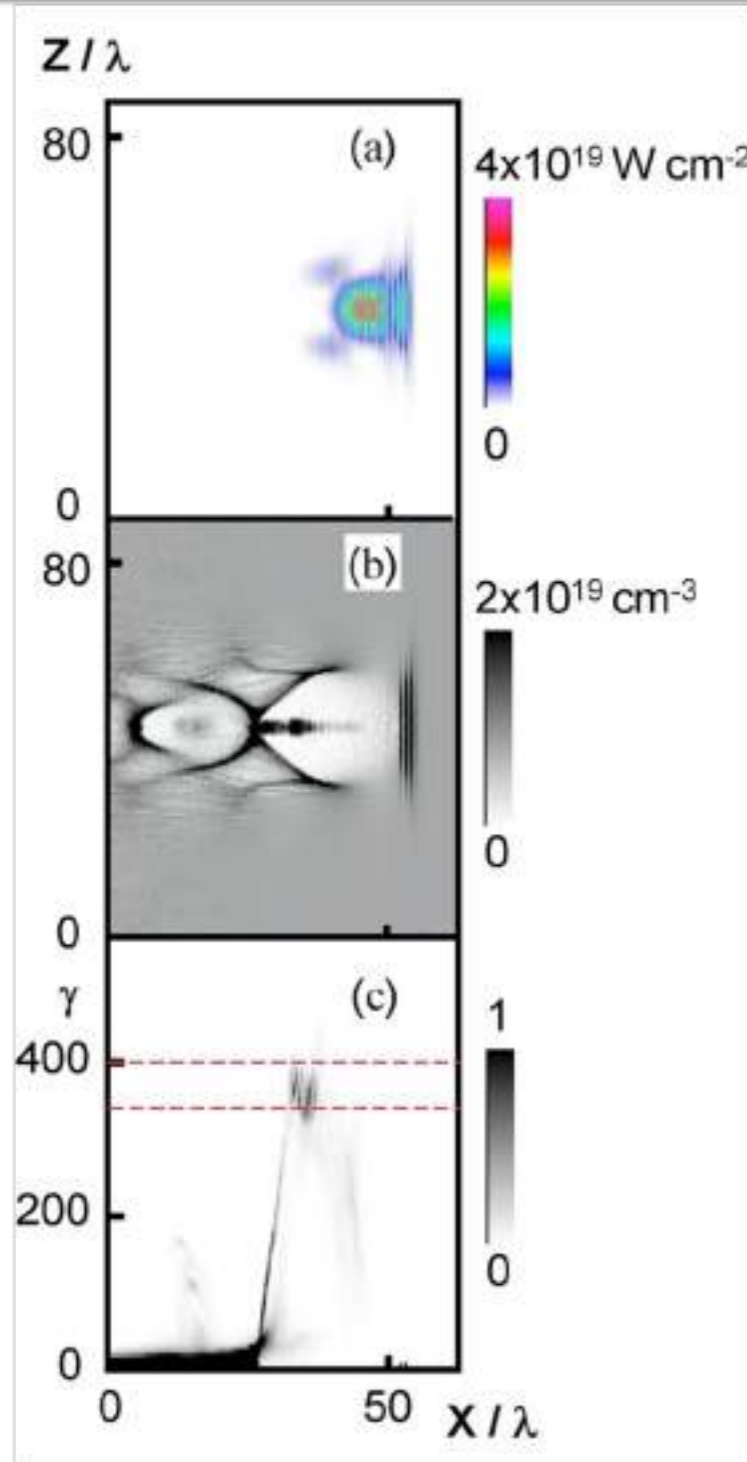


localized self injection in the
bubble/blow-out regime

surfing behind a wake boat

A. Pukhov & J. Meyer-ter-Vehn, *Appl. Phys. B* **74**, 355-361 (2002),

2005 The Bubble regime : theory/experiments



Experimental parameters : $E=1\text{J}$,
 $\tau_L=30\text{fs}$, $\lambda_L=0.8\mu\text{m}$, $I_L=3.2 \times 10^{19}\text{W/cm}^2$,
 $n_e=6 \times 10^{18}\text{cm}^{-3}$

J. Faure *et al.*, Nature **431**, 7008 (2004)



Monoenergetic beams of relativistic electrons from intense laser-plasma interactions

S. P. D. Mangles¹, C. D. Murphy^{1,2}, Z. Najmudin¹, A. G. R. Thomas¹, J. L. Collier², A. E. Dangor¹, E. J. Divall², P. S. Foster², J. G. Gallacher³, C. J. Hooker², D. A. Jaroszynski³, A. J. Langley², W. B. Mori⁴, P. A. Norreys², F. S. Tsung⁴, R. Viskup³, B. R. Walton¹ & K. Krushelnick¹

¹The Blackett Laboratory, Imperial College London, London SW7 2AZ, UK

²Central Laser Facility, Rutherford Appleton Laboratory, Chilton, Didcot, Oxon, OX11 0QX, UK

³Department of Physics, University of Strathclyde, Glasgow G4 0NG, UK

⁴Department of Physics and Astronomy, UCLA, Los Angeles, California 90095, USA

High-quality electron beams from a laser wakefield accelerator using plasma-channel guiding

C. G. R. Geddes^{1,2}, Cs. Toth¹, J. van Tilborg^{1,3}, E. Esarey¹, C. B. Schroeder¹, D. Bruhwiler⁴, C. Nieter⁴, J. Cary^{4,5} & W. P. Leemans¹

¹Lawrence Berkeley National Laboratory, 1 Cyclotron Road, Berkeley, California 94720, USA

²University of California, Berkeley, California 94720, USA

³Technische Universiteit Eindhoven, Postbus 513, 5600 MB Eindhoven, the Netherlands

⁴Tech-X Corporation, 5621 Arapahoe Ave. Suite A, Boulder, Colorado 80303, USA

⁵University of Colorado, Boulder, Colorado 80309, USA

A laser-plasma accelerator producing monoenergetic electron beams

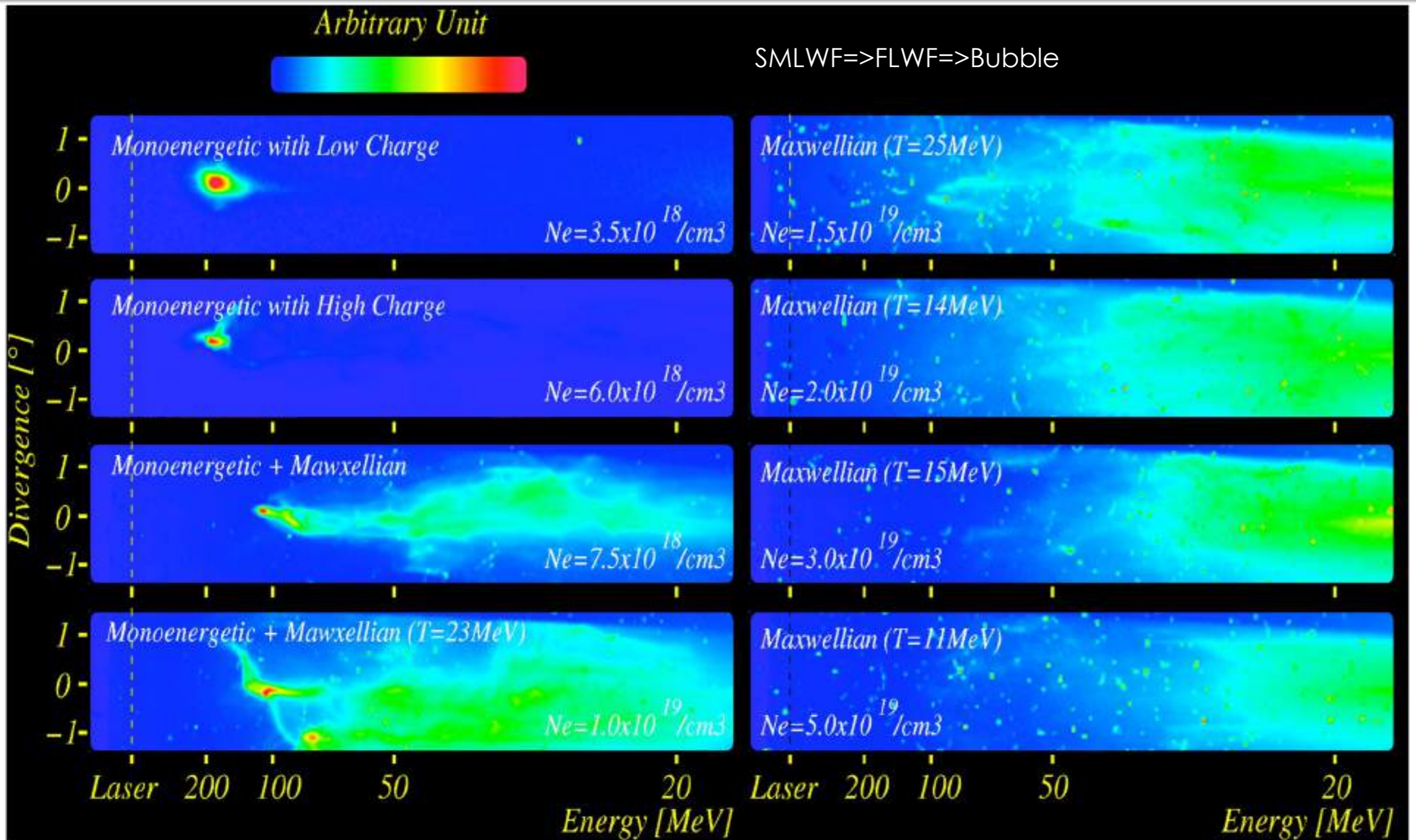
J. Faure¹, Y. Glinec¹, A. Pukhov², S. Kiselev², S. Gordienko², E. Lefebvre³, J.-P. Rousseau¹, F. Burgy¹ & V. Malka¹

¹Laboratoire d'Optique Appliquée, Ecole Polytechnique, ENSTA, CNRS, UMR 7639, 91761 Palaiseau, France

²Institut für Theoretische Physik 1, Heinrich-Heine-Universität Düsseldorf, 40225 Düsseldorf, Germany

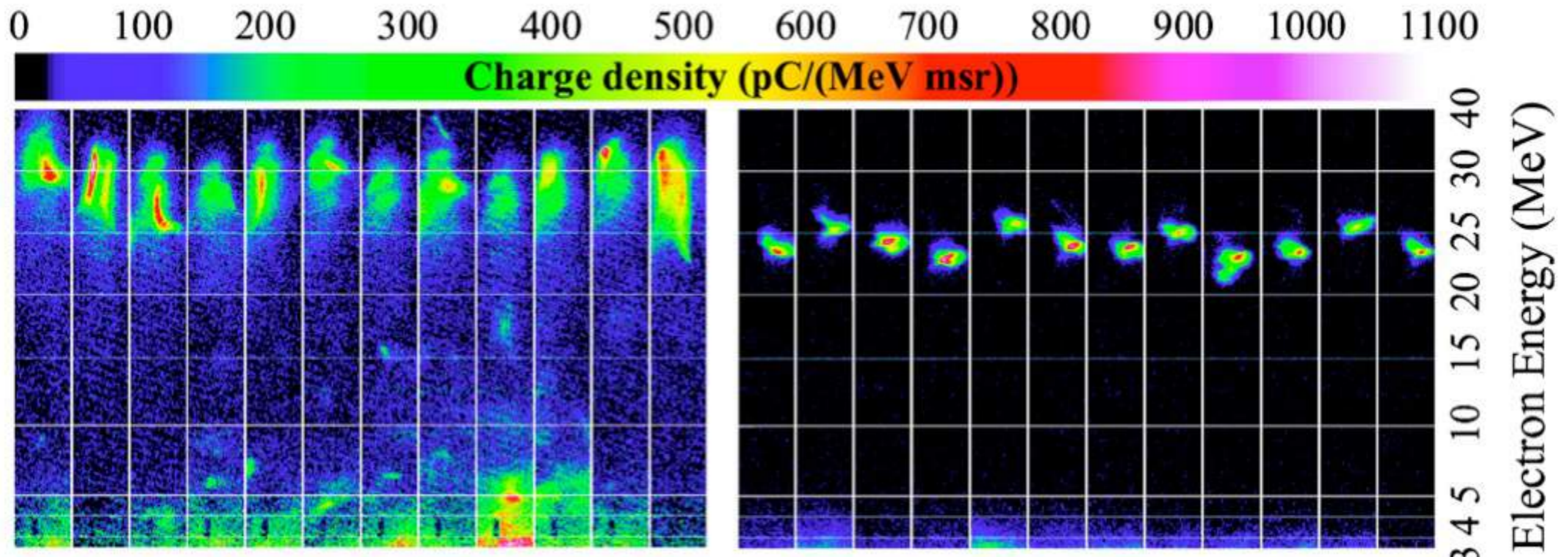
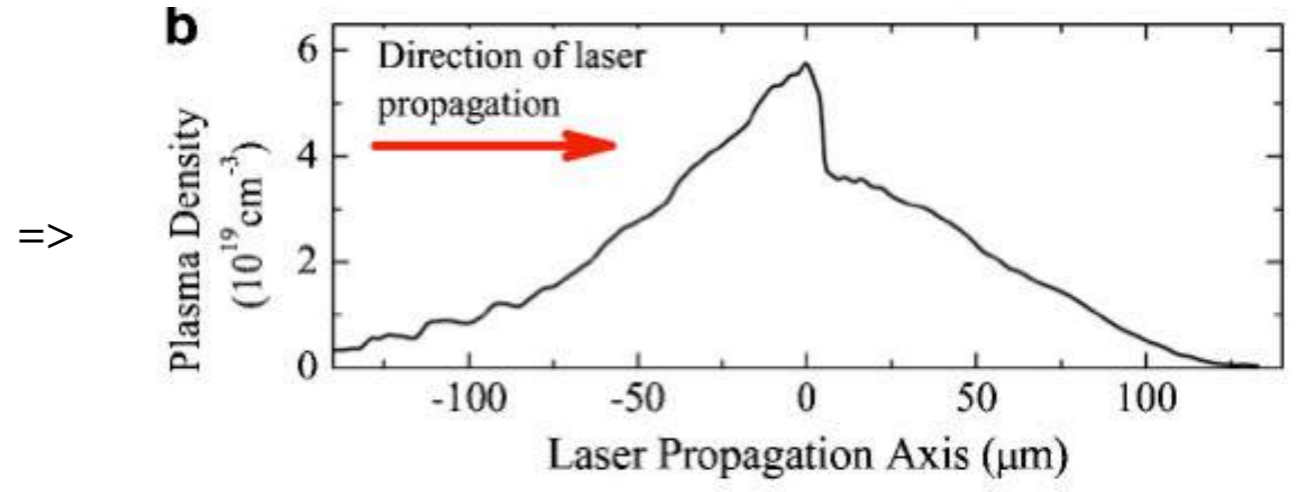
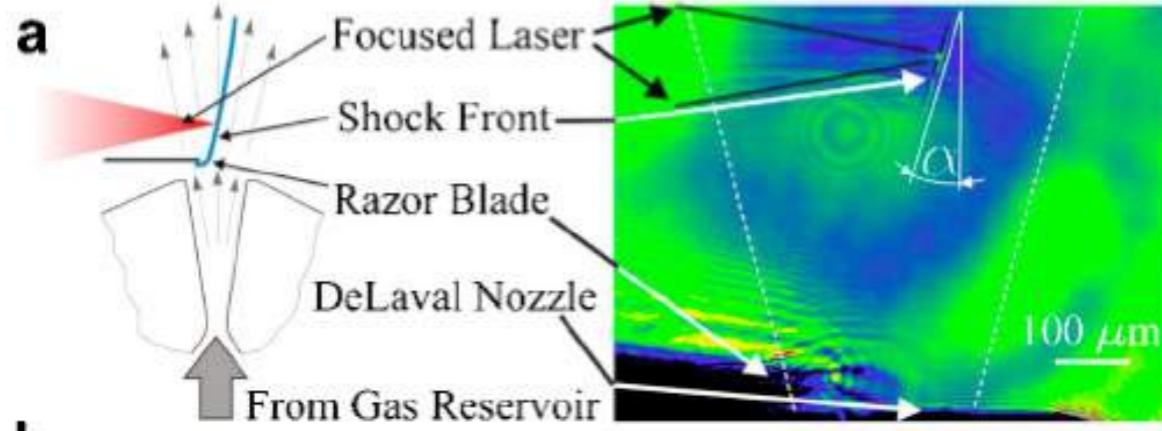
³Département de Physique Théorique et Appliquée, CEA/DAM Ile-de-France, 91680 Bruyères-le-Châtel, France

SMLWF => FLWF => Bubble regime



V. Malka et al., Phys. of Plasmas **12**, 5 (2005)

2010 Sharp density ramp injection

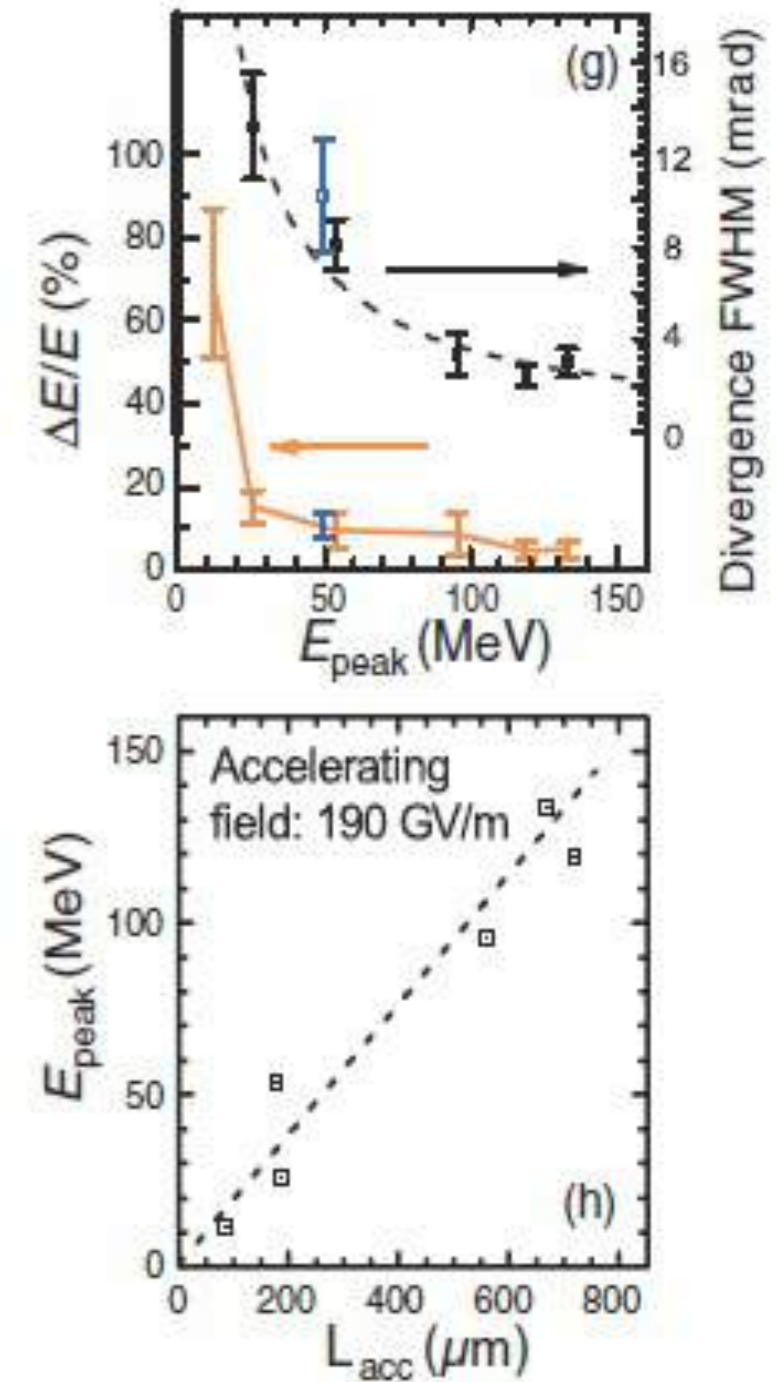
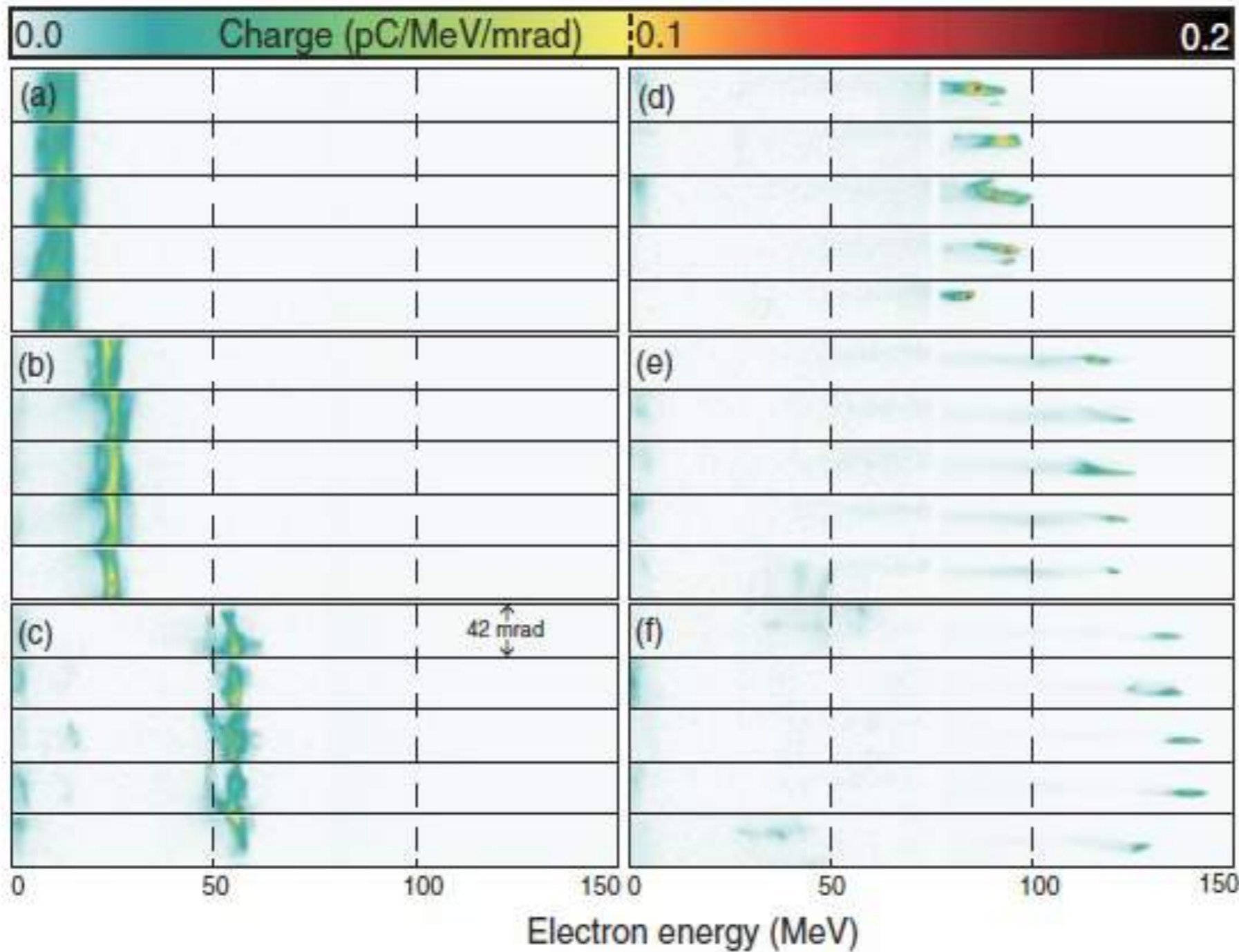


(a) Self injection

(b) Injection at density transition

K. Schmid et al., PRSTAB 13, 091301 (2010)

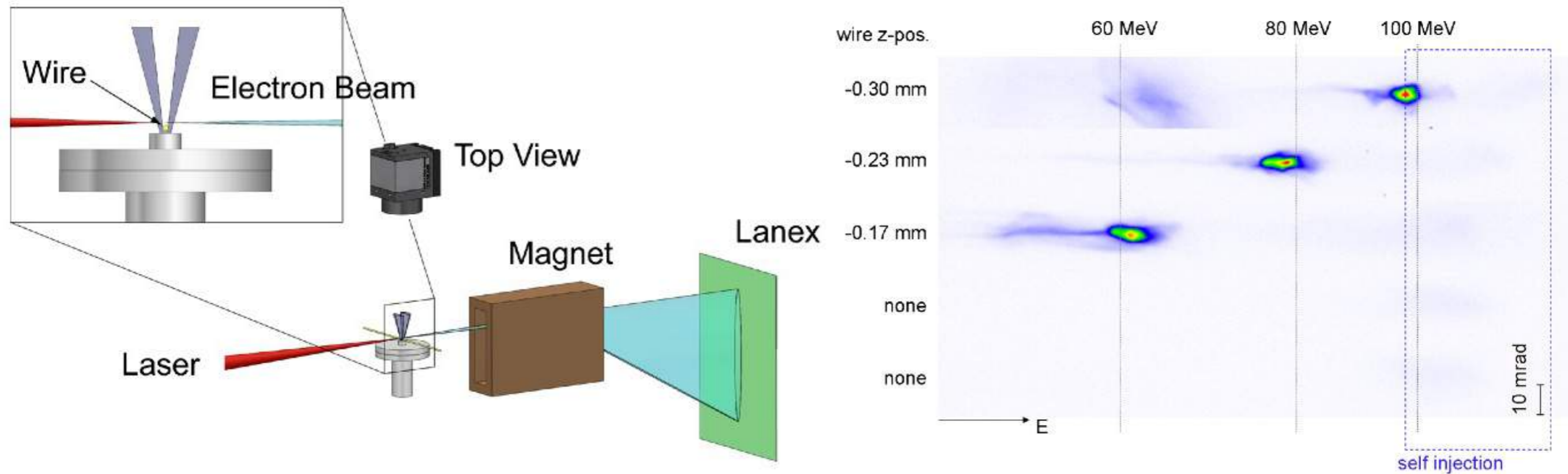
2013 Shock front injection



A. Buck *et al.*, PRSTAB 13, 091301 (2010)



Laser wakefield acceleration using wire produced double density ramps



M. Burza *et al.*, PRSTAB 16, 011301 (2013)

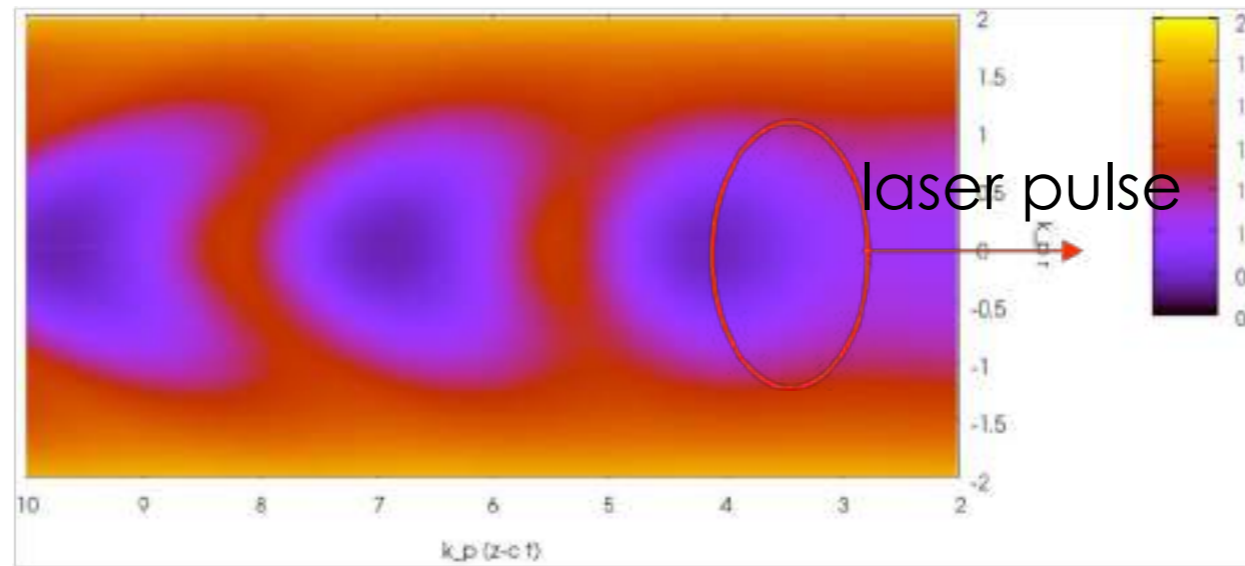
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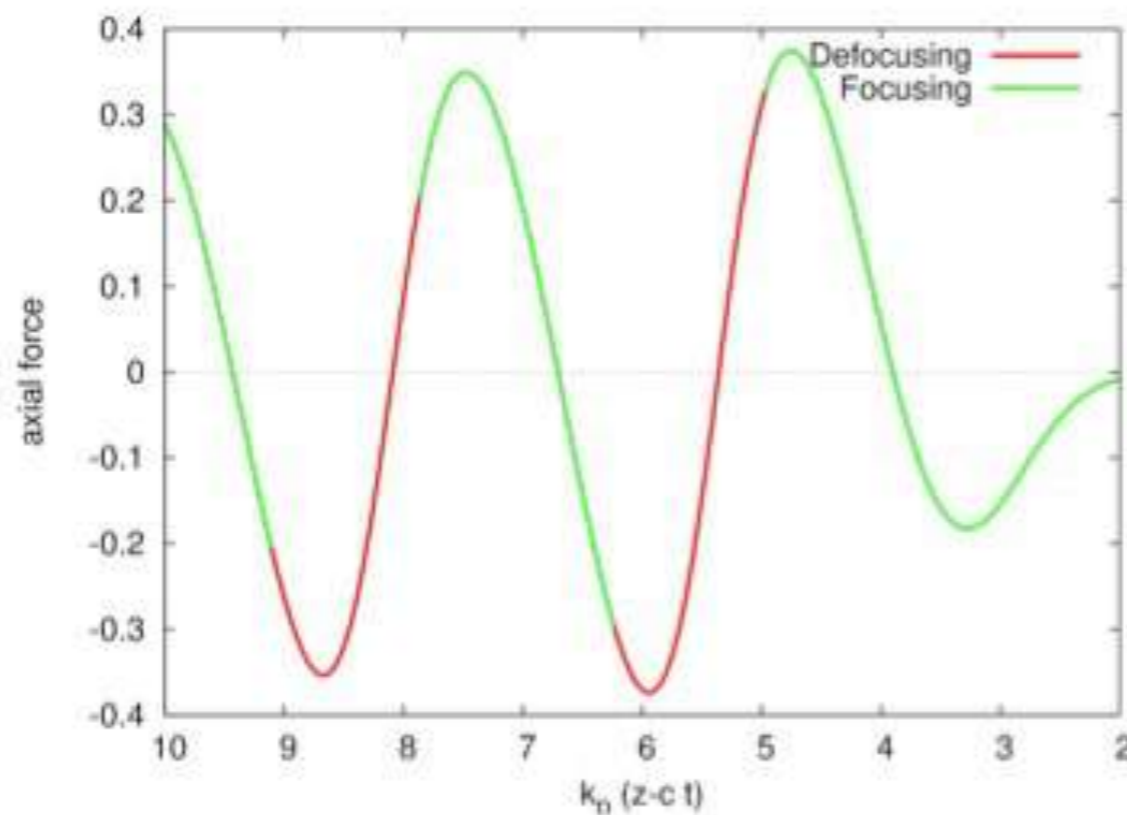
Towards a two stage plasma accelerator



Small Laser amplitude $a_0=0.5$ & Parabolic plasma channel

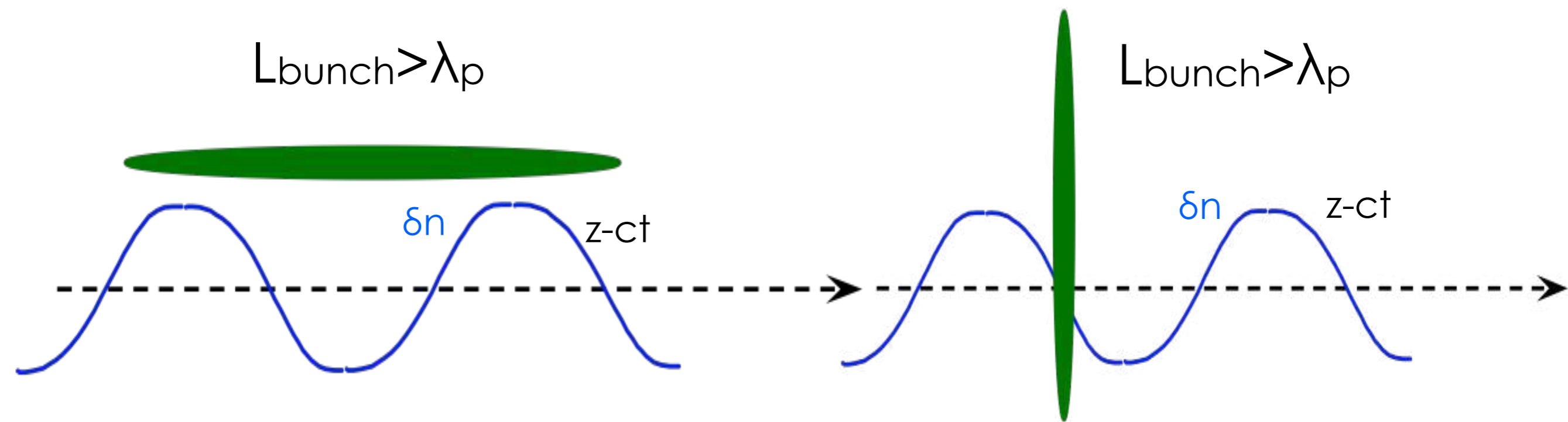


electron density



V. Malka et al., PRST-A 9, 9 (2006)

Towards a two stage plasma accelerator



Different phases =>
Different E field =>
100 % energy spread

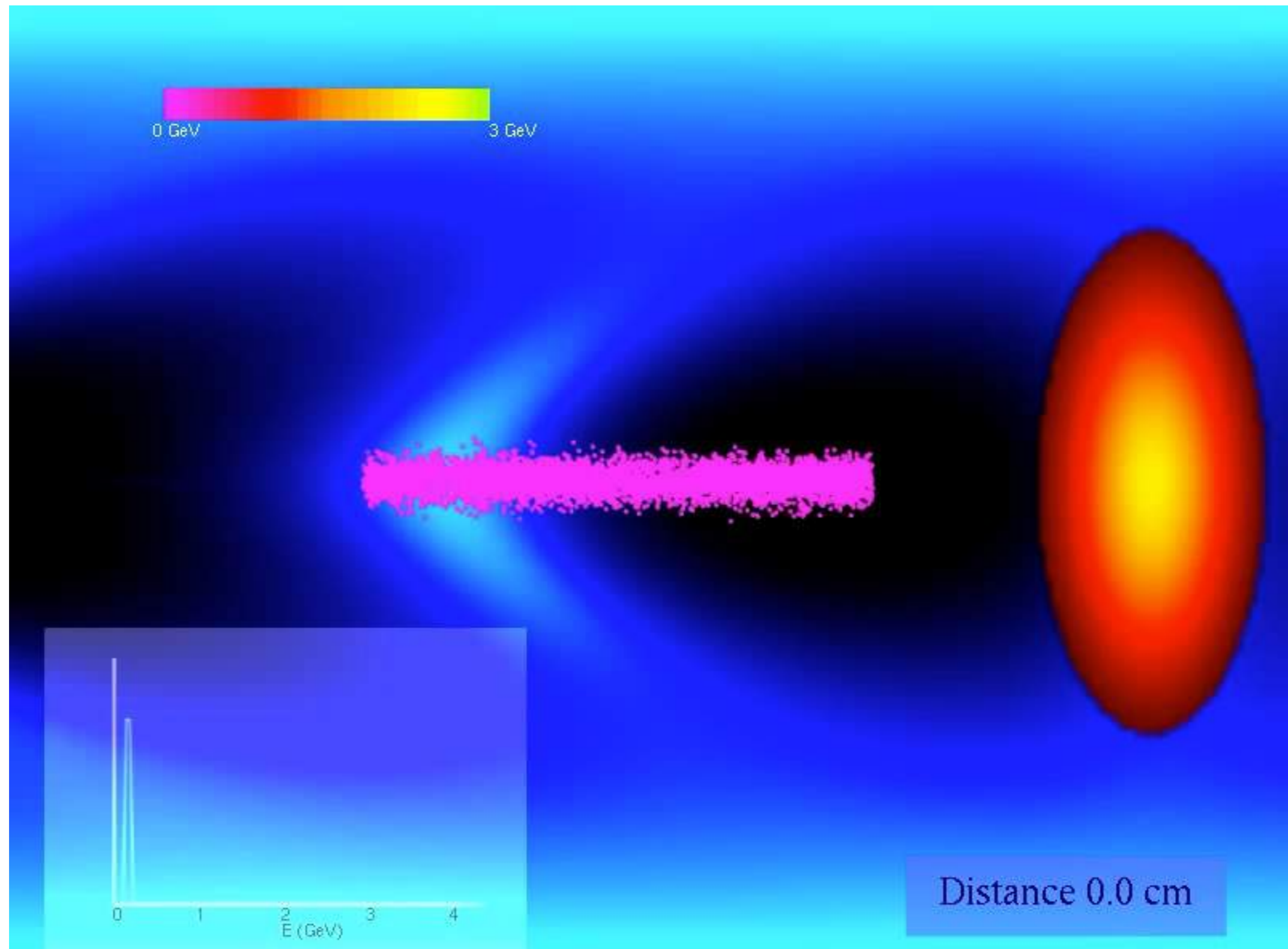
electrons “in phase” =>
same E field =>
low energy spread

One needs $L_{\text{bunch}} < 100$ fs
Challenge for RF technology

Wake simulations of injected 100 fs electrons bunch



E=170
MeV,
Laser :
9J, 150
TW, 60fs

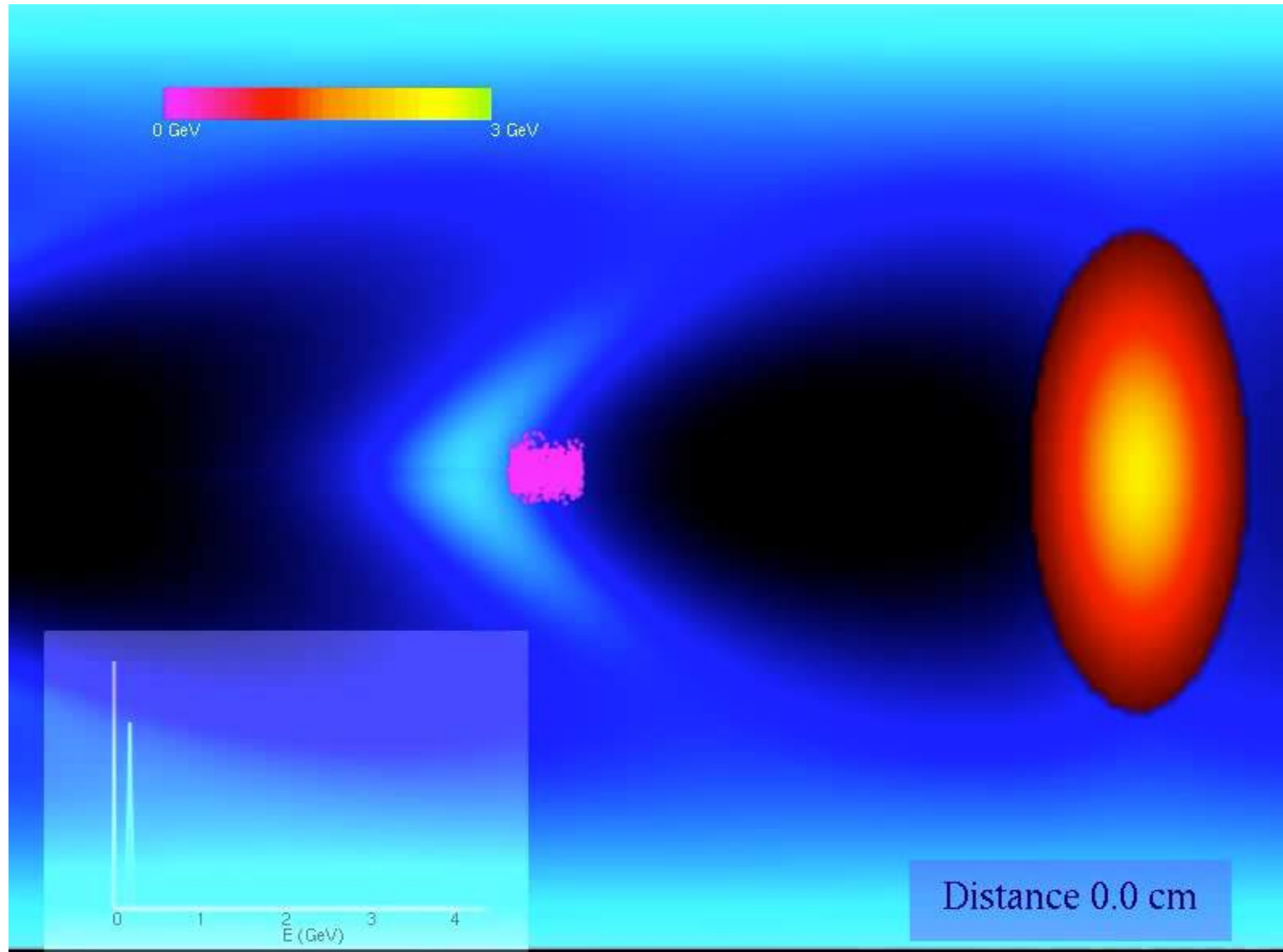


V. Malka *et al.*, PRST-A **9**, 9 (2006)

Wake simulations of injected 30 fs electrons bunch



E=170
MeV,
Laser :
9J, 150
TW, 60fs

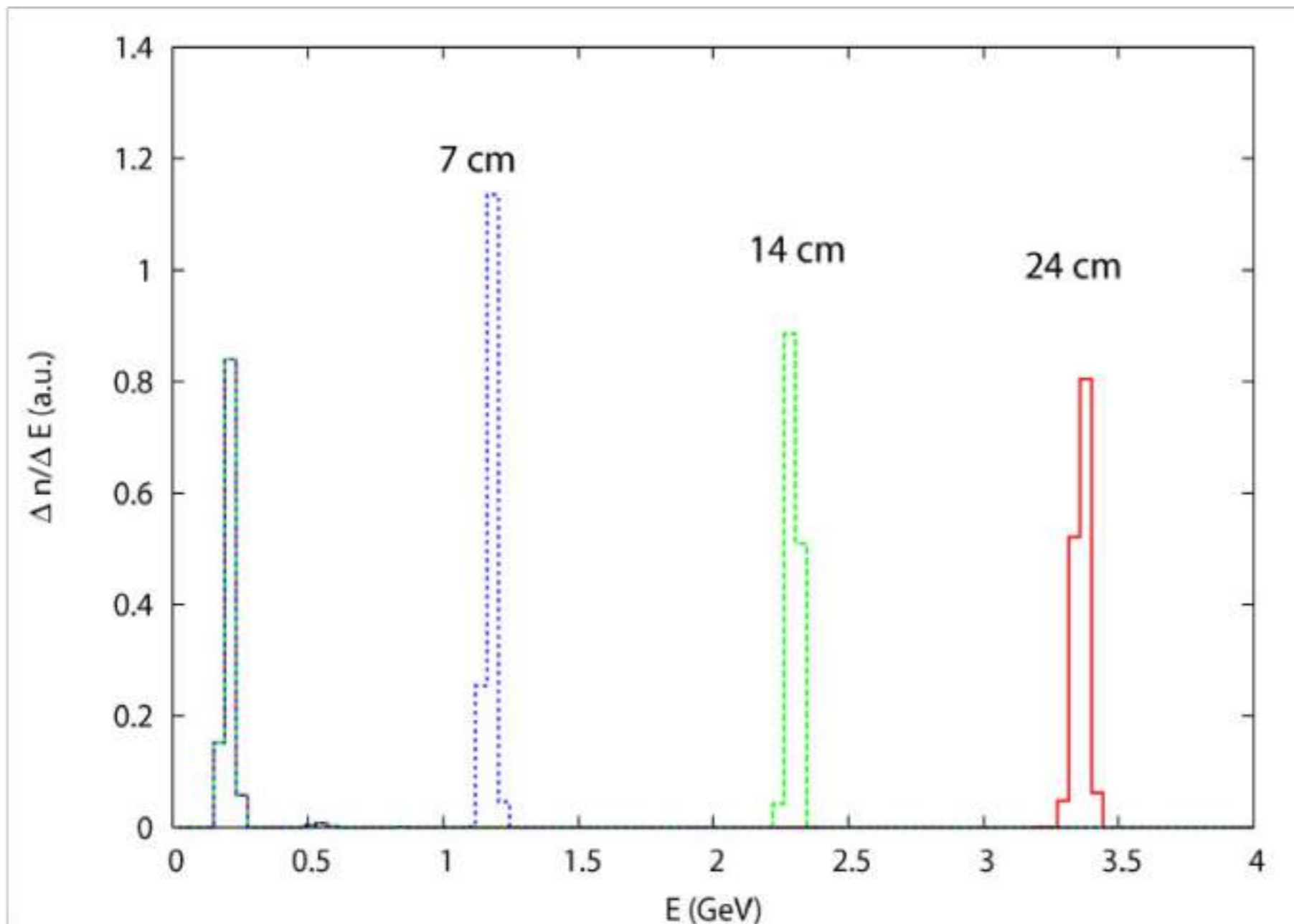


V. Malka *et al.*, PRST-A **9**, 9 (2006)

Wake simulations of injected 30 fs electrons bunch



$E=170$ MeV, Laser : 9J, 150 TW, 60fs



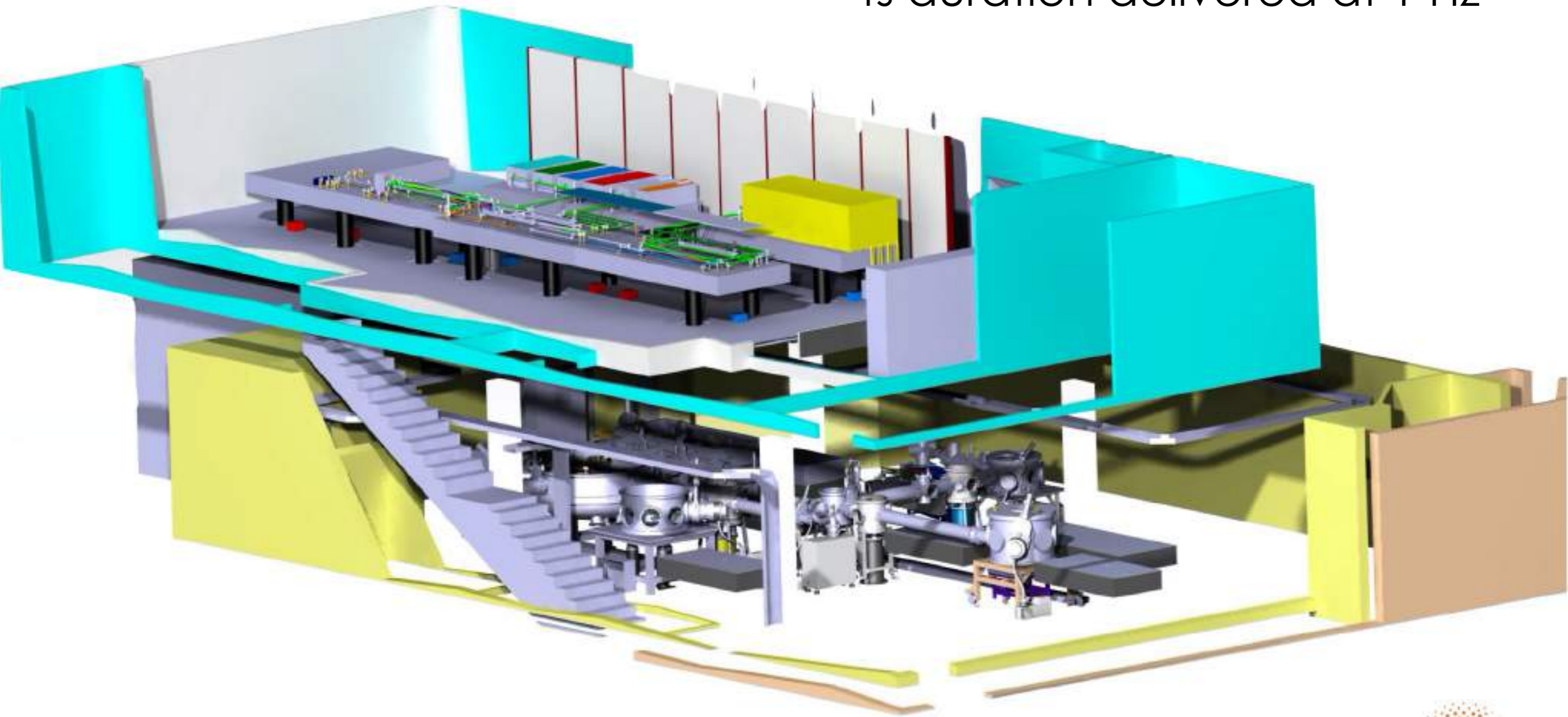
- $E=9$ J
- $P=0.15$ PW
- $a_0=1.5$
- Parabolic channel:
- $r_0=47$ μm ,
- $n(r)=n_0 (1+0.585 r/r_0)$
- $n_0 = 1.1 \times 10^{17}$ cm^{-3}

3.5 GeV, with a relative energy spread FWHM of 1% and an un-normalized emittance of 0.006 mm

« Salle Jaune Laser » : Home made laser



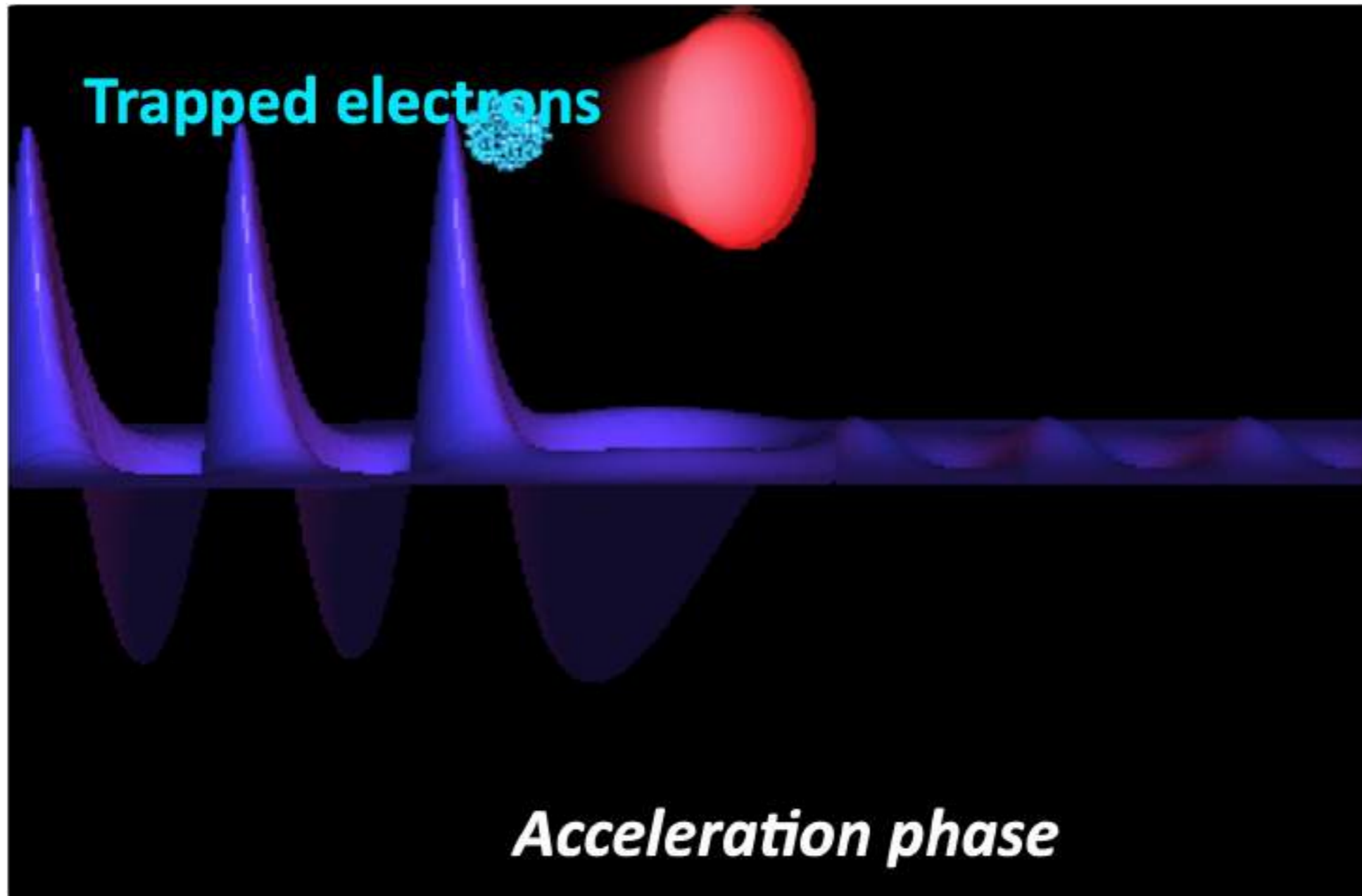
2 Joules in 2 laser beams of 30 fs duration delivered at 1 Hz



R. Lehe

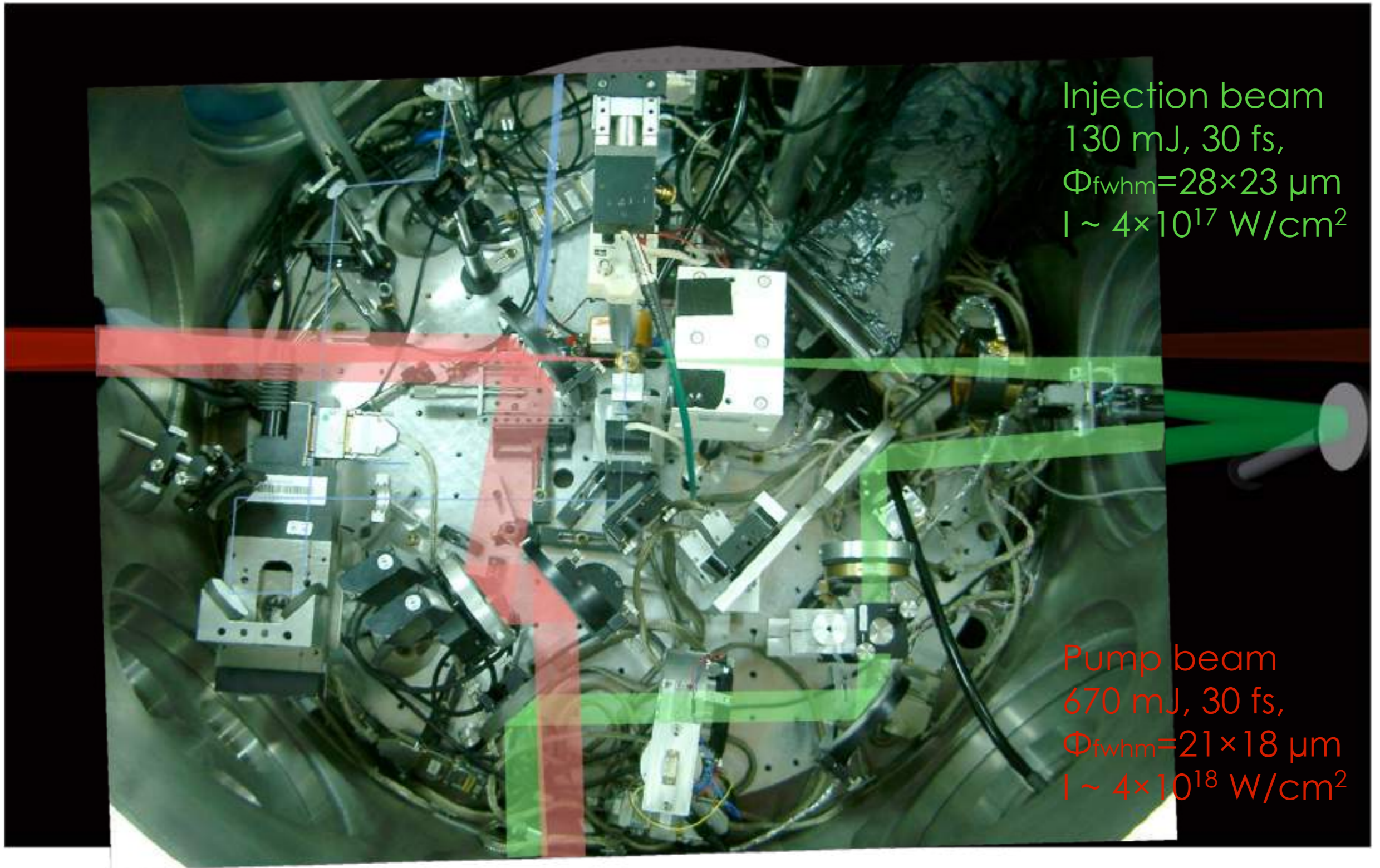


Colliding Laser Pulses Scheme



The first laser creates the accelerating structure
A second laser beam is used to heat electrons

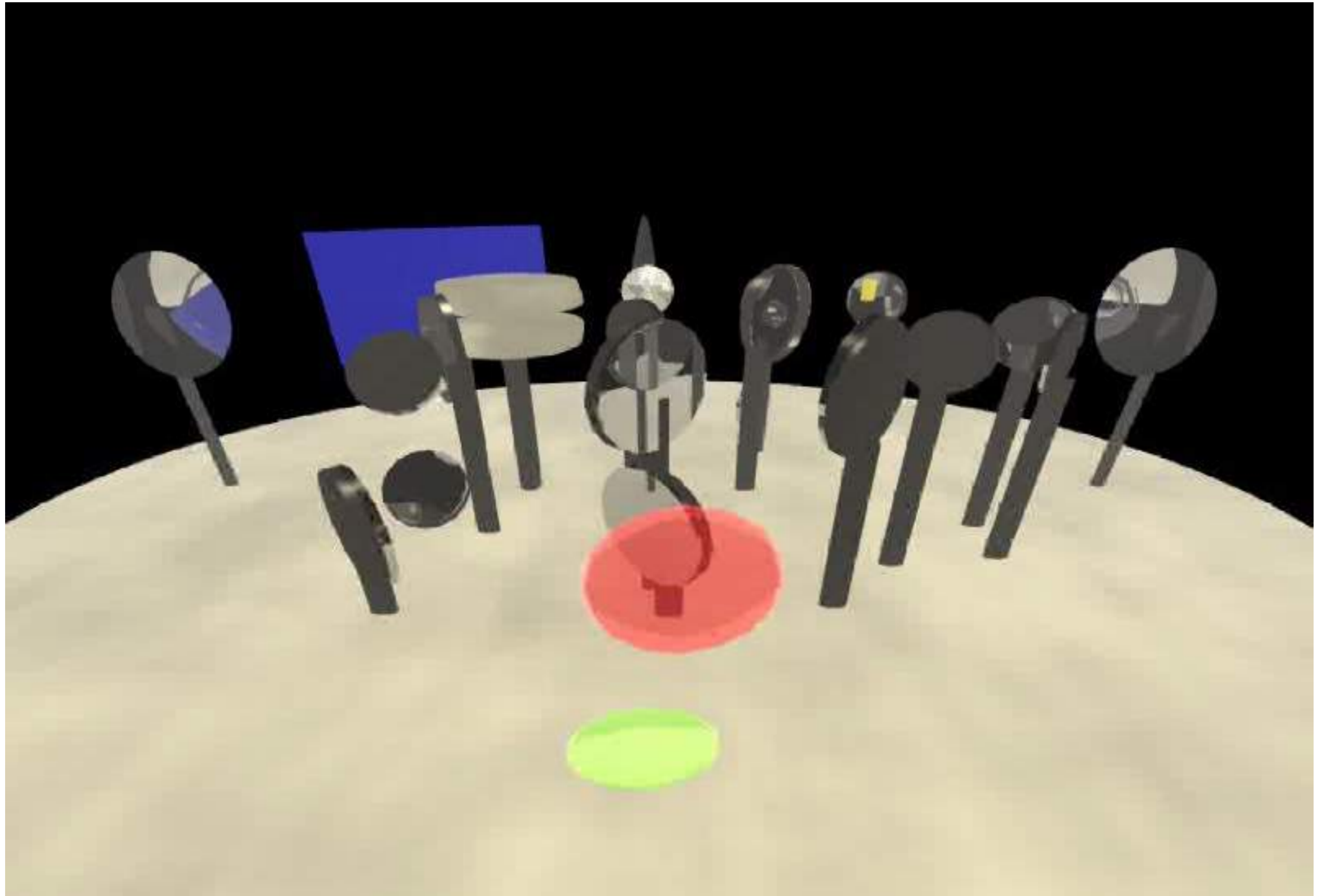
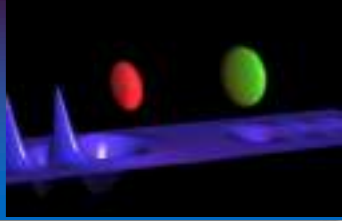
Set-up for colliding pulses experiment



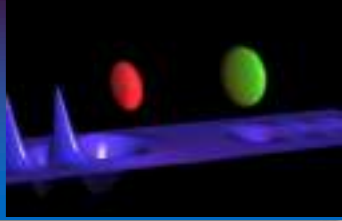
Injection beam
130 mJ, 30 fs,
 $\Phi_{\text{fwhm}}=28 \times 23 \mu\text{m}$
 $I \sim 4 \times 10^{17} \text{ W/cm}^2$

Pump beam
670 mJ, 30 fs,
 $\Phi_{\text{fwhm}}=21 \times 18 \mu\text{m}$
 $I \sim 4 \times 10^{18} \text{ W/cm}^2$

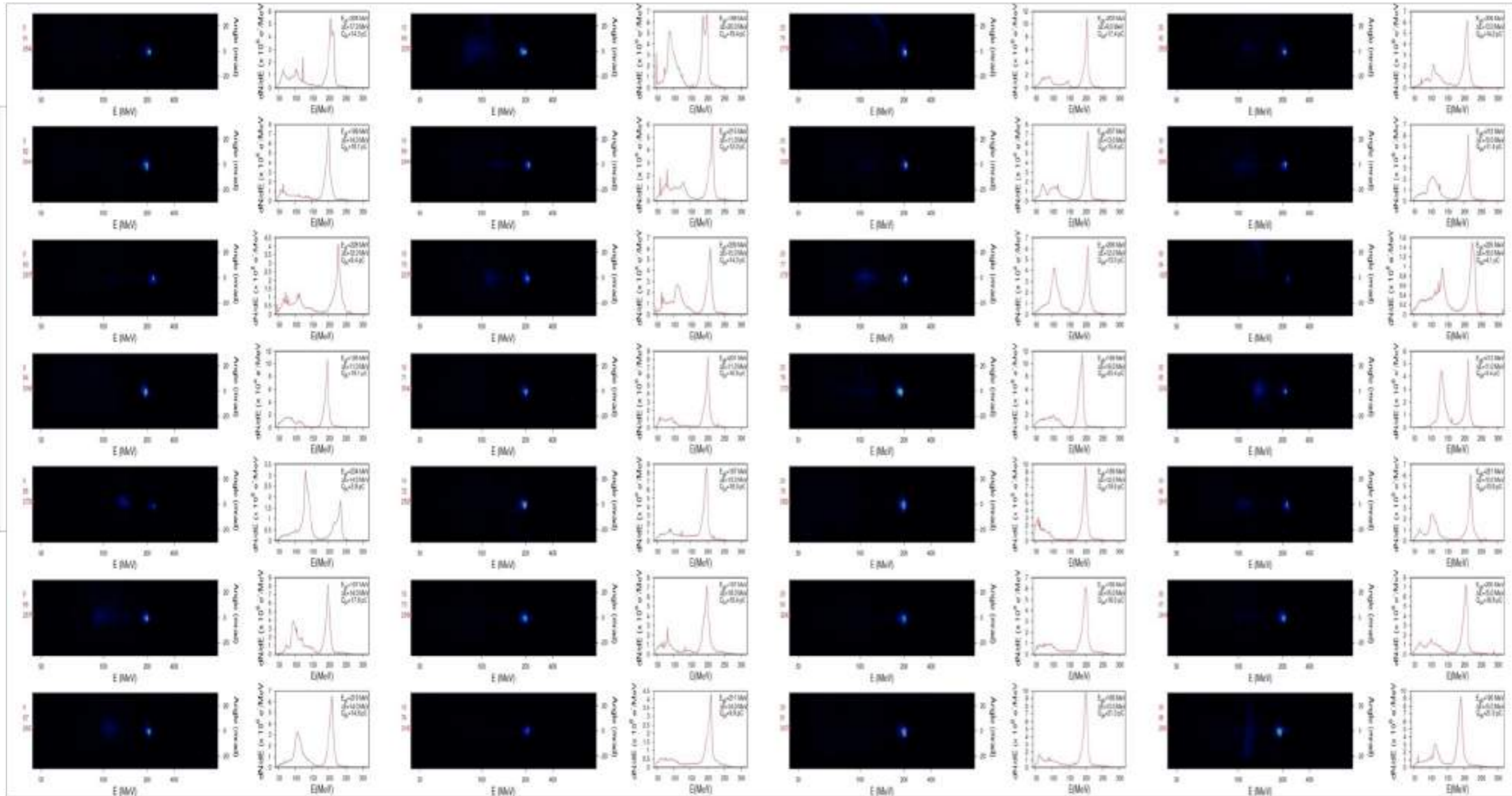
The colliding of two laser pulses scheme



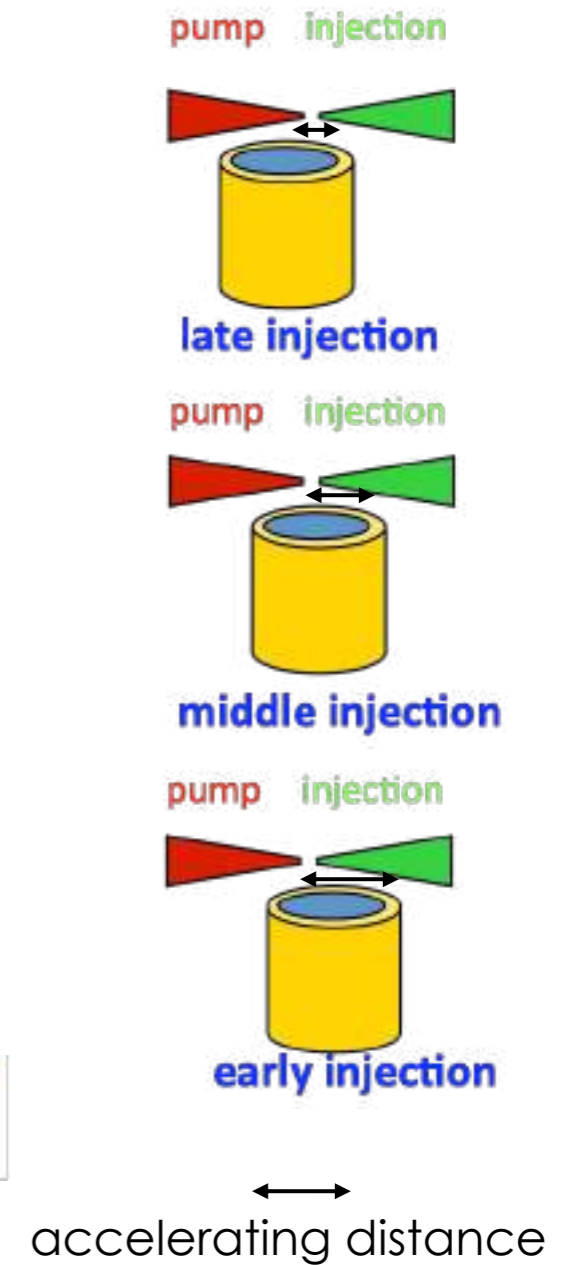
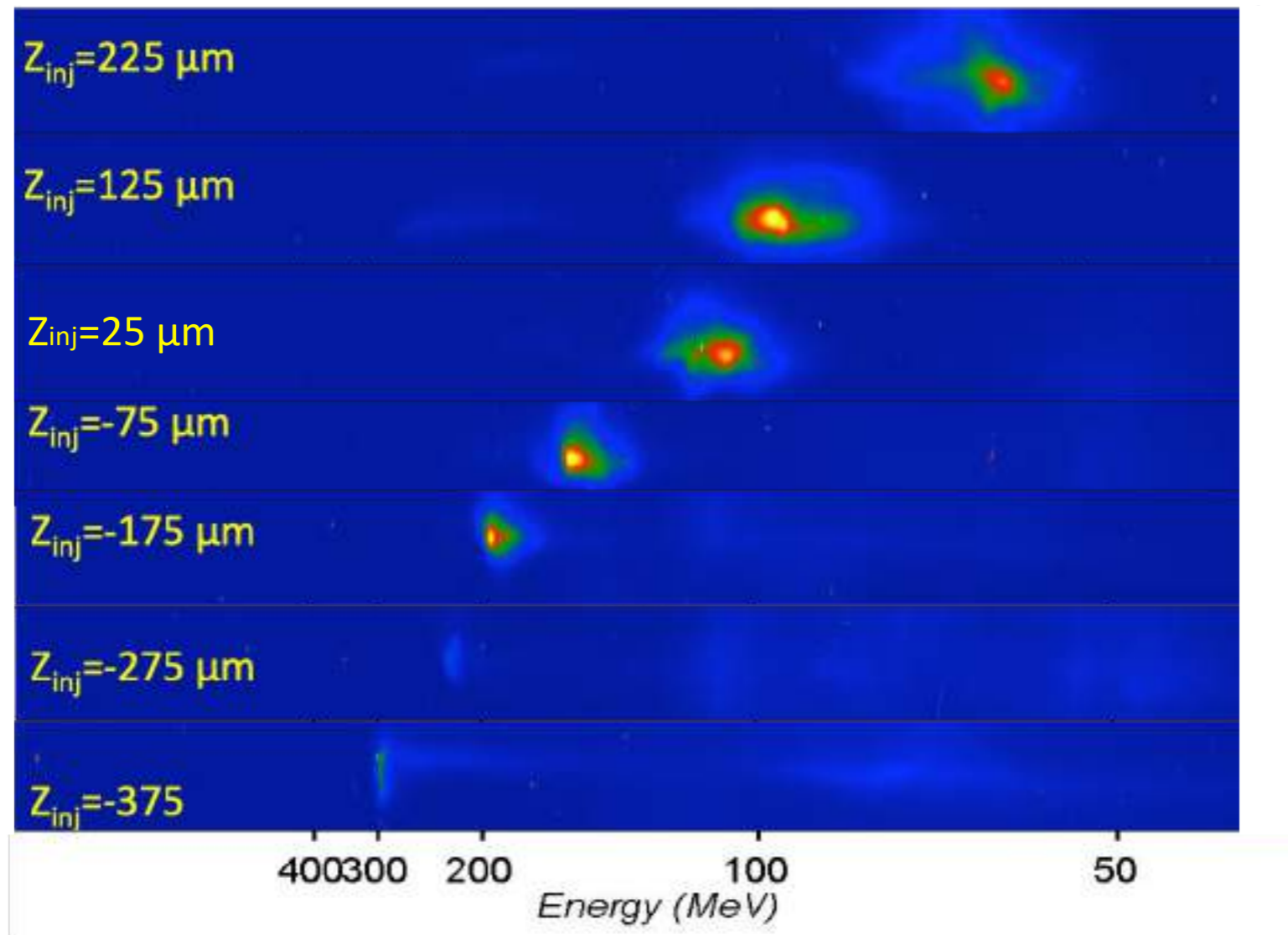
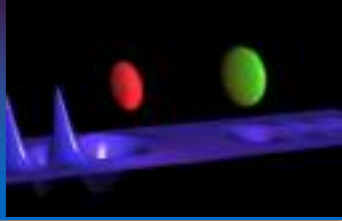
Towards a Stable Laser Plasma Accelerators



Series of 28 consecutive shots with : $a_0=1.5$, $a_1=0.4$, $n_e=5.7 \times 10^{18} \text{cm}^{-3}$

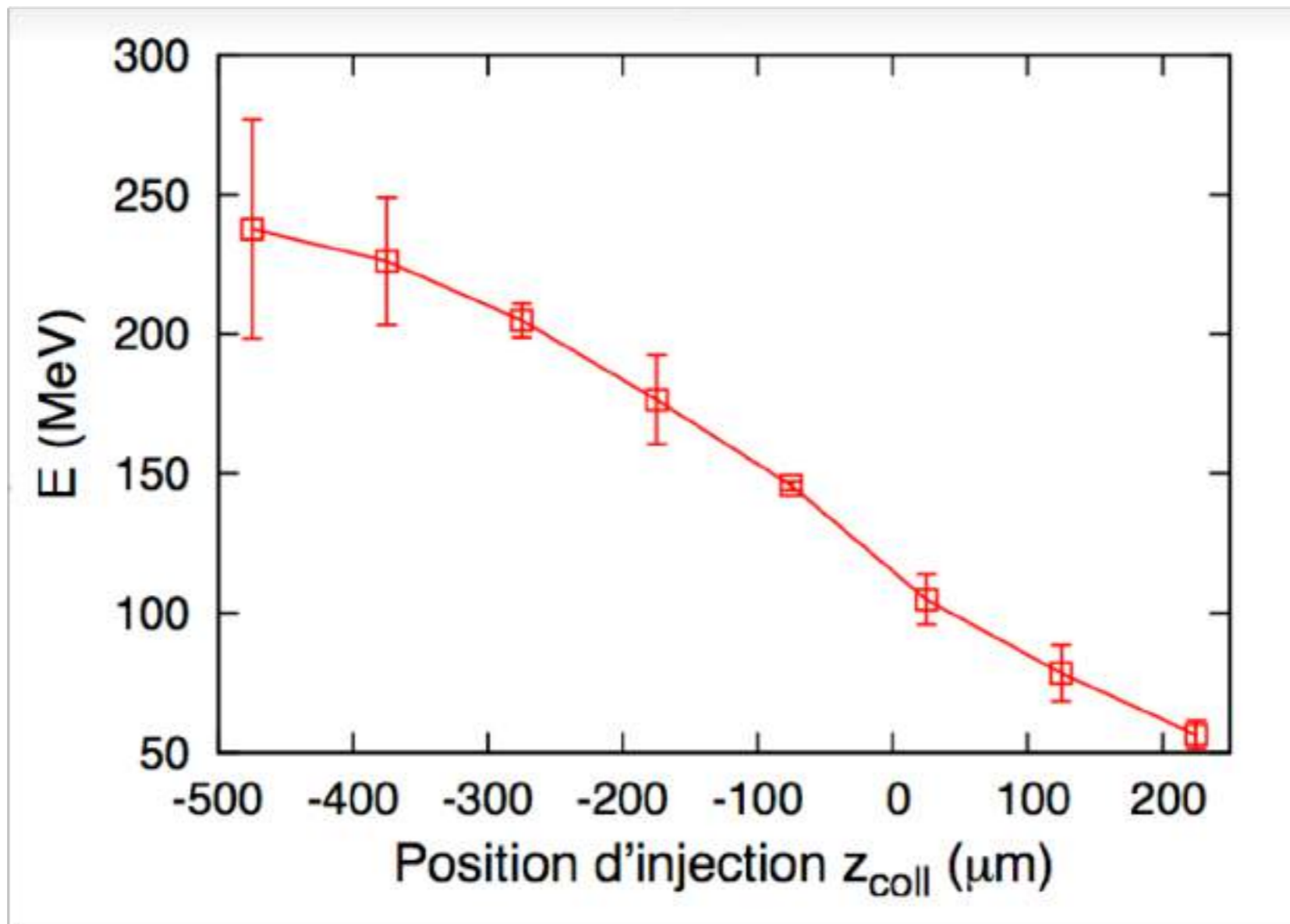
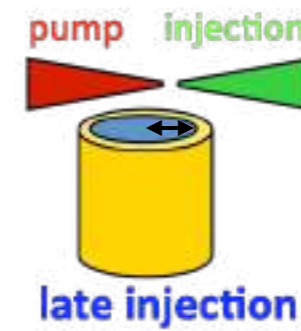


Tunability of the electrons energy

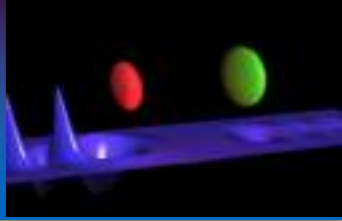


J. Faure et al., Nature **444**, 737 (2006)

Tunability of the electrons energy

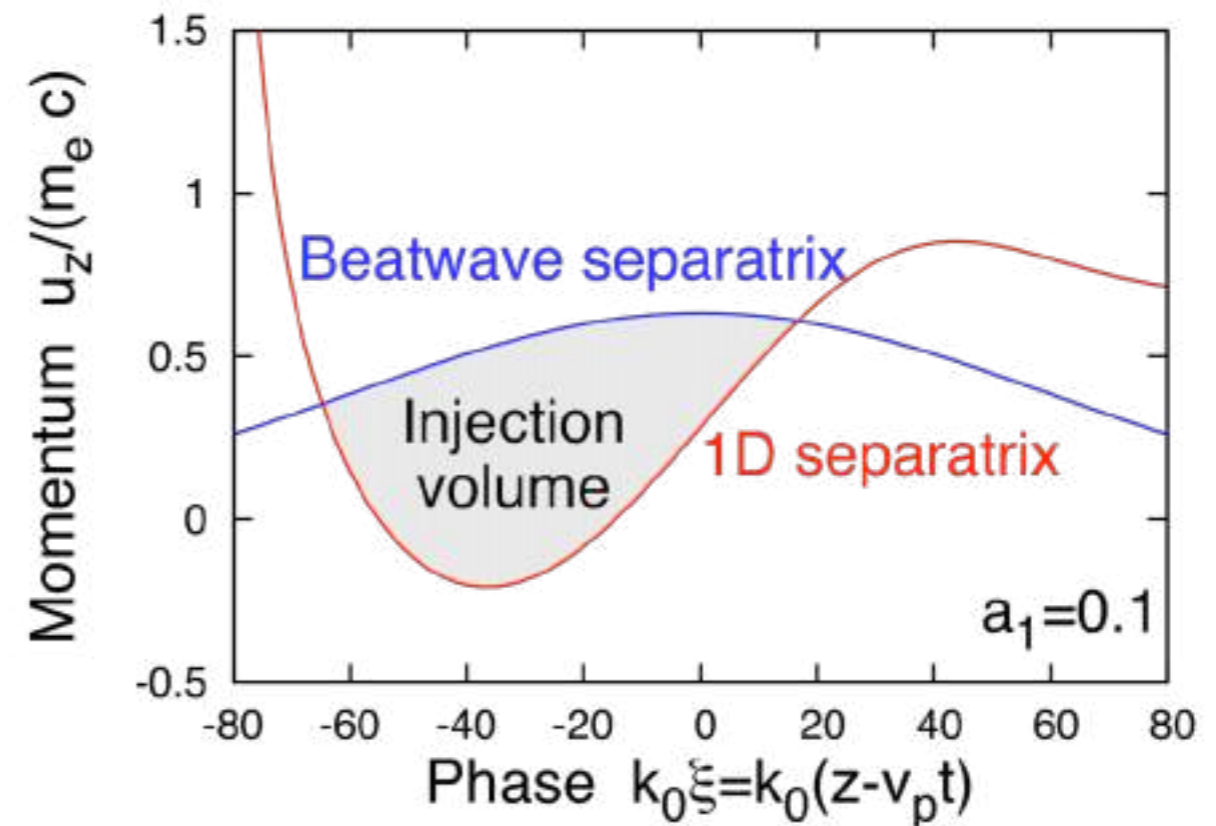
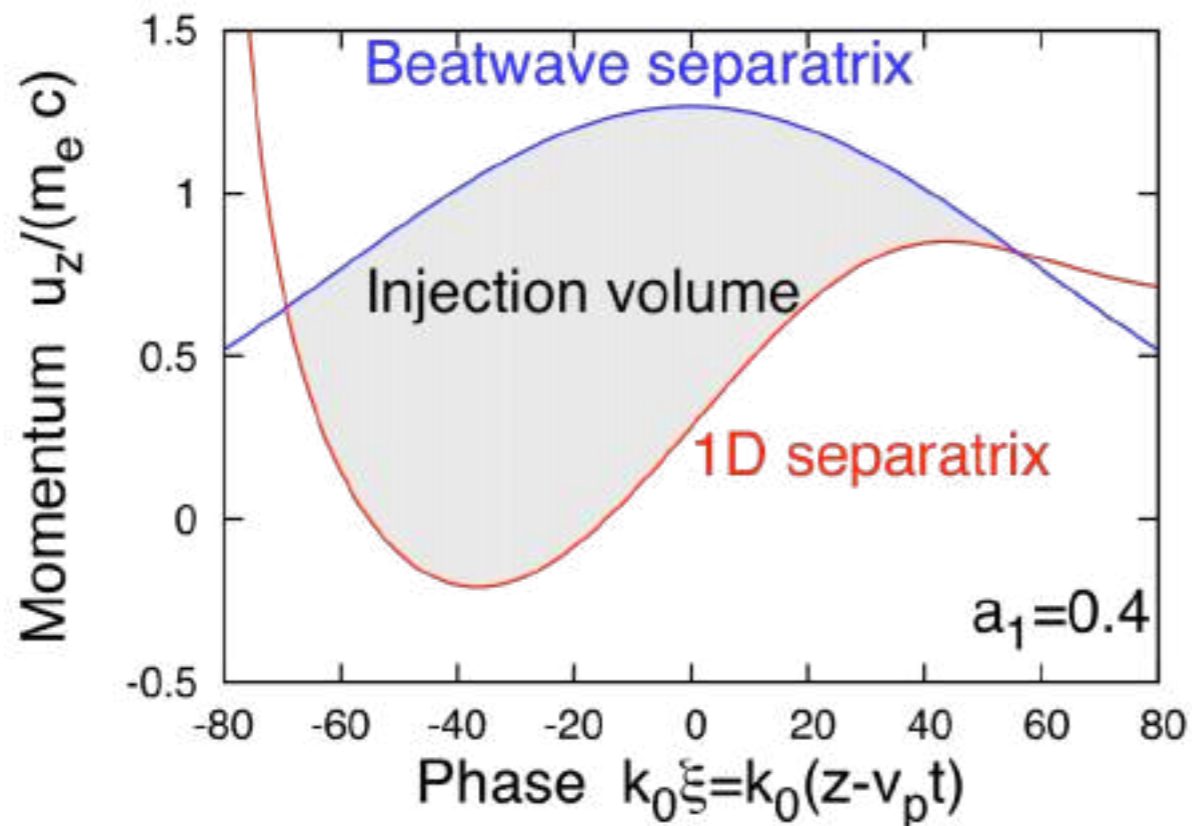


Tunability of charge & energy spread



Charge : controlling electrons heating processes => smaller a_{inj} . means less heating and less trapping

Energy spread : Decreasing the phase space volume V_{trap} of trapped electrons by reducing a_{inj} . or by reducing $c\tau/\lambda_p$ by changing n_e (i.e λ_p)

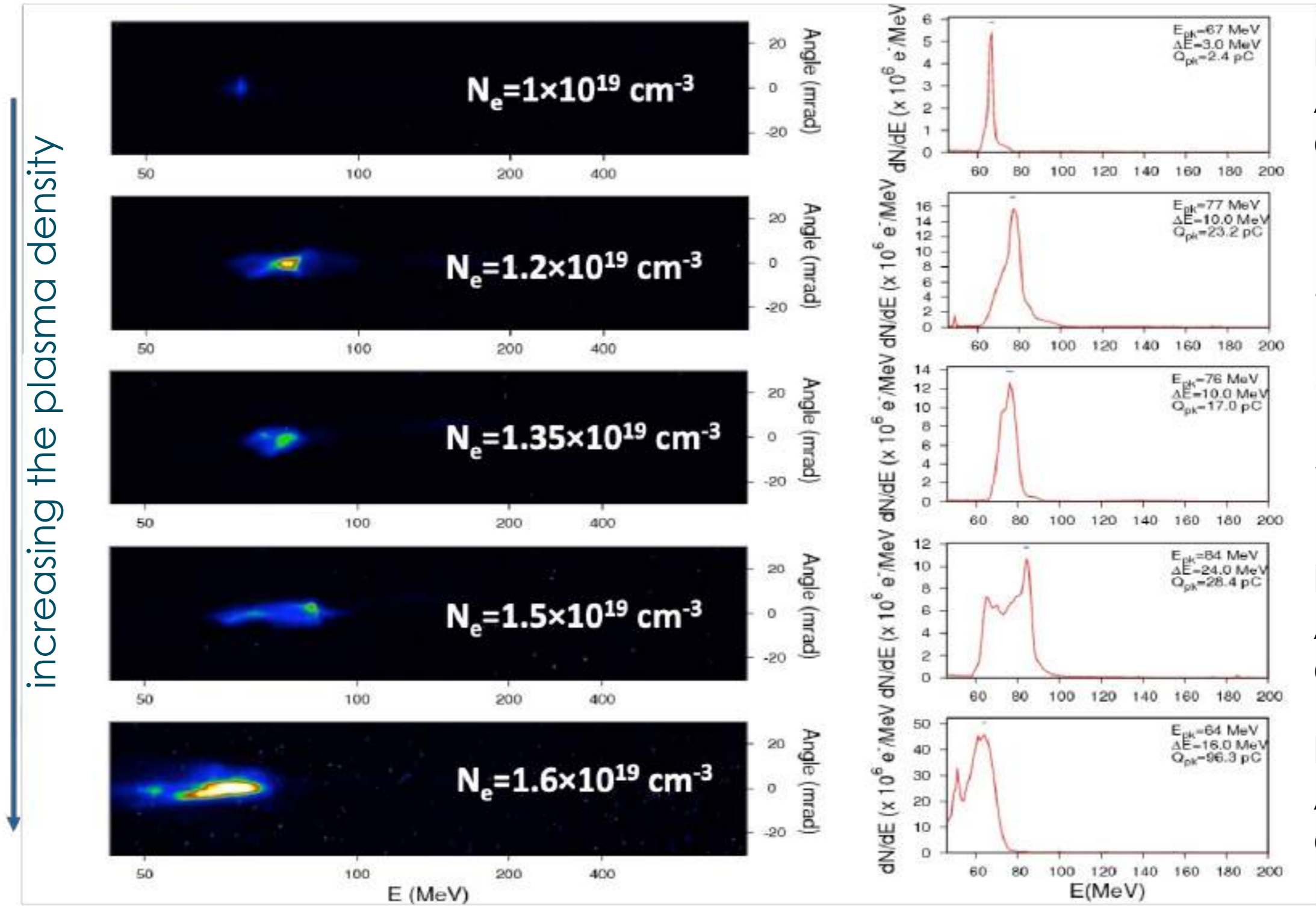
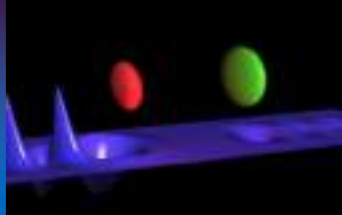


Evolution of injection volume with a_1 for $a_0 = 2$, $n_e = 7 \times 10^{18} \text{cm}^{-3}$.

Fields are computed for the 1D case and the beatwave separatrix corresponds to the circular polarization case.

In practice, energy spread and charge are correlated: Decreasing a_1 decreases the charge but also V_{trap} , and in consequence the energy spread

Tuning the charge & energy spread with the plasma density



$E=67$ MeV
 $\Delta E=3$ MeV
 $Q_{pk}=2.4$ pC

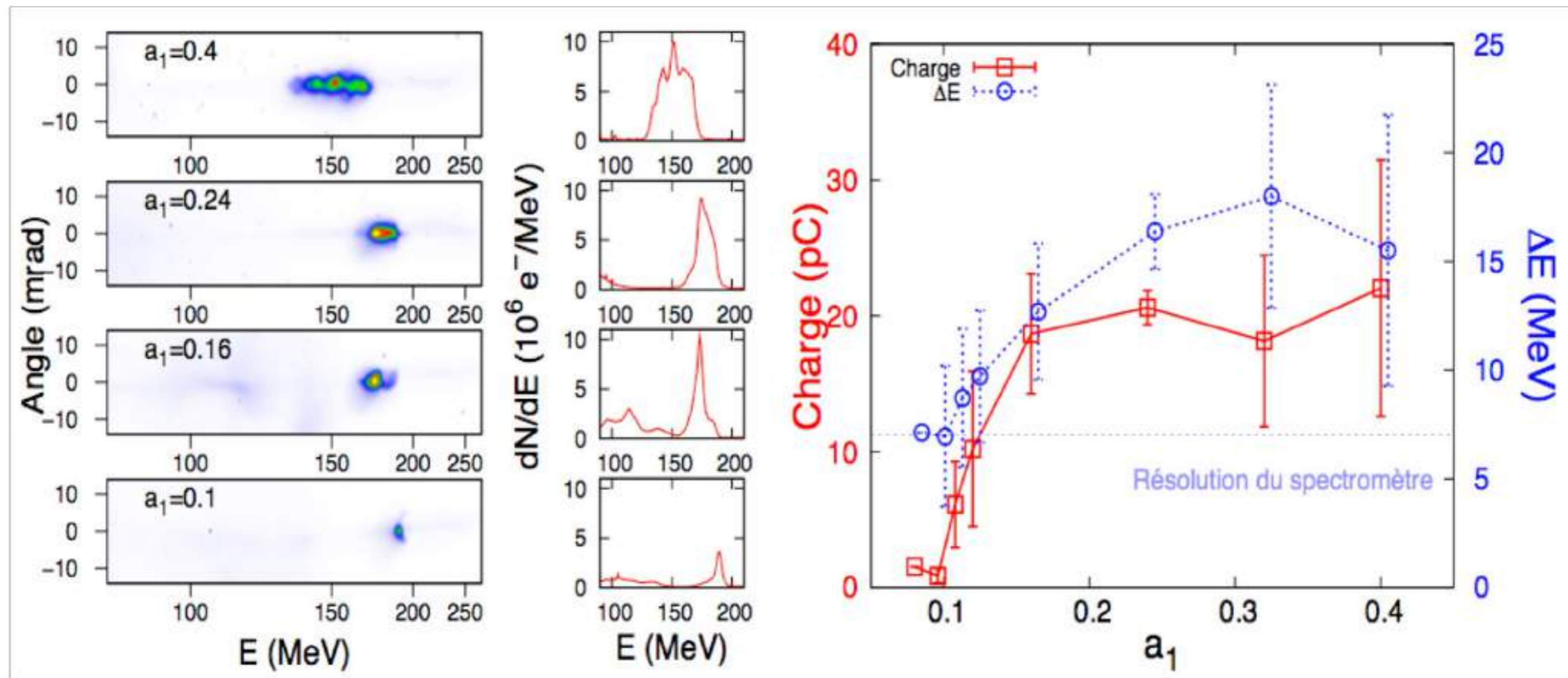
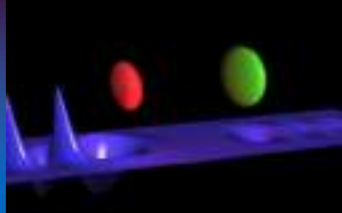
$E=77$ MeV
 $\Delta E=10$ MeV
 $Q_{pk}=23.2$ pC

$E=76$ MeV
 $\Delta E=10.0$ MeV
 $Q_{pk}=17$ pC

$E=84$ MeV
 $\Delta E=24$ MeV
 $Q_{pk}=25.4$ pC

$E=64$ MeV
 $\Delta E=16$ MeV
 $Q_{pk}=96$ pC

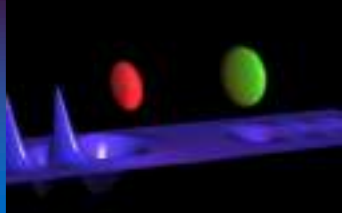
Tuning charge & energy spread with the inj. laser intensity



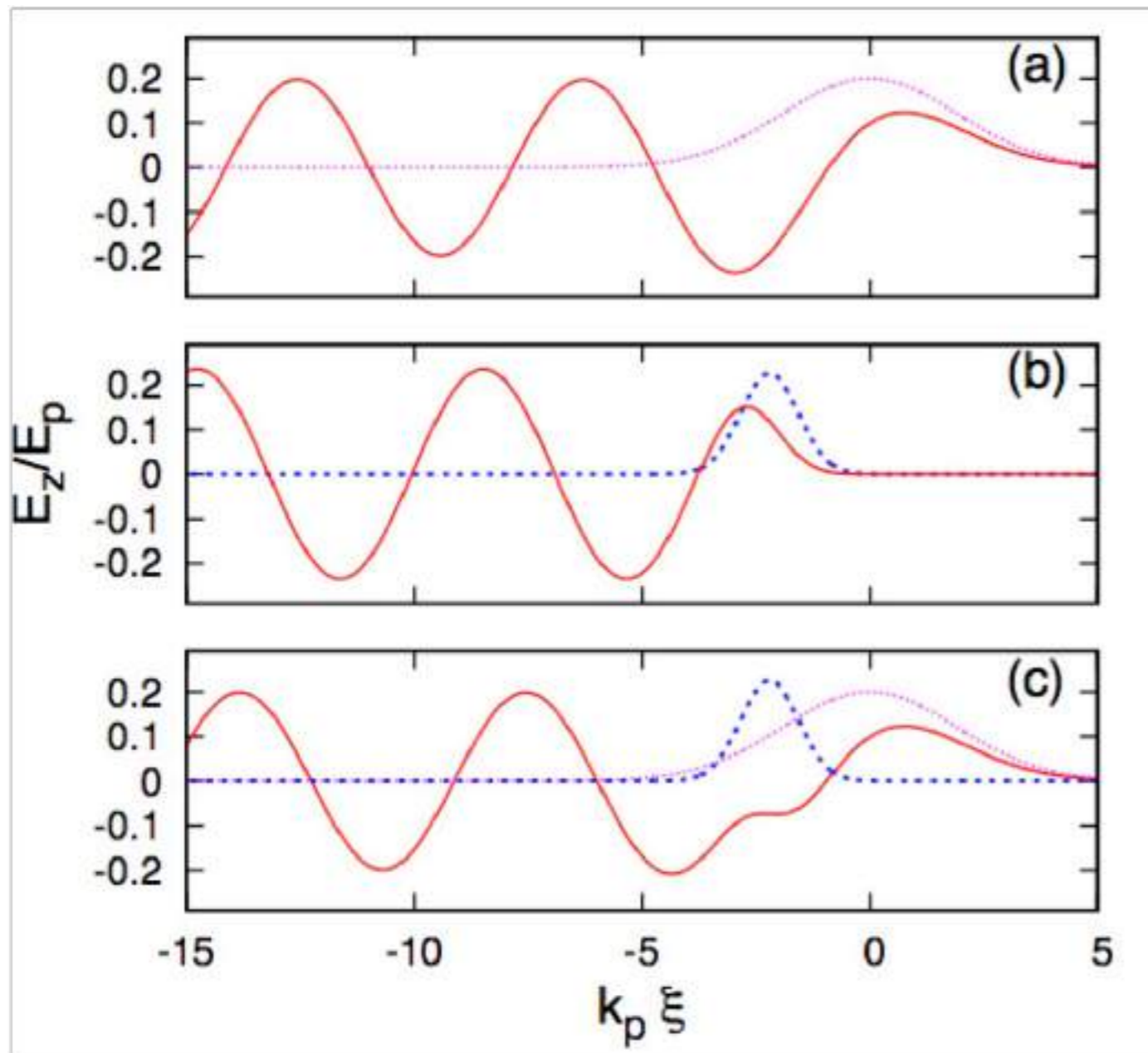
Charge from 60 pC to 5 pC, ΔE from 20 to 5 MeV

C. Rechatin *et al.*, Phys. Rev. Lett. **102**, 164801 (2009)

e- beam dynamics in plasma wave: beam loading



Parameters: $n_e=1.5 \cdot 10^{19} \text{cm}^{-3}$, $\tau = 35 \text{fs}$, $E=0.6 \text{J}$, $I=2 \cdot 10^{18} \text{W/cm}^2$



Laser wakefield

$n_e=7 \cdot 10^{18} \text{cm}^{-3}$, $\tau = 30 \text{fs}$, $a_0 = 0.5$

E-beam wakefield

$n_b/n_e=0.11$, $\tau = 10 \text{fs}$, $d_{\text{FWHM}}=4 \mu\text{m}$
($Q=7 \text{pC}$)

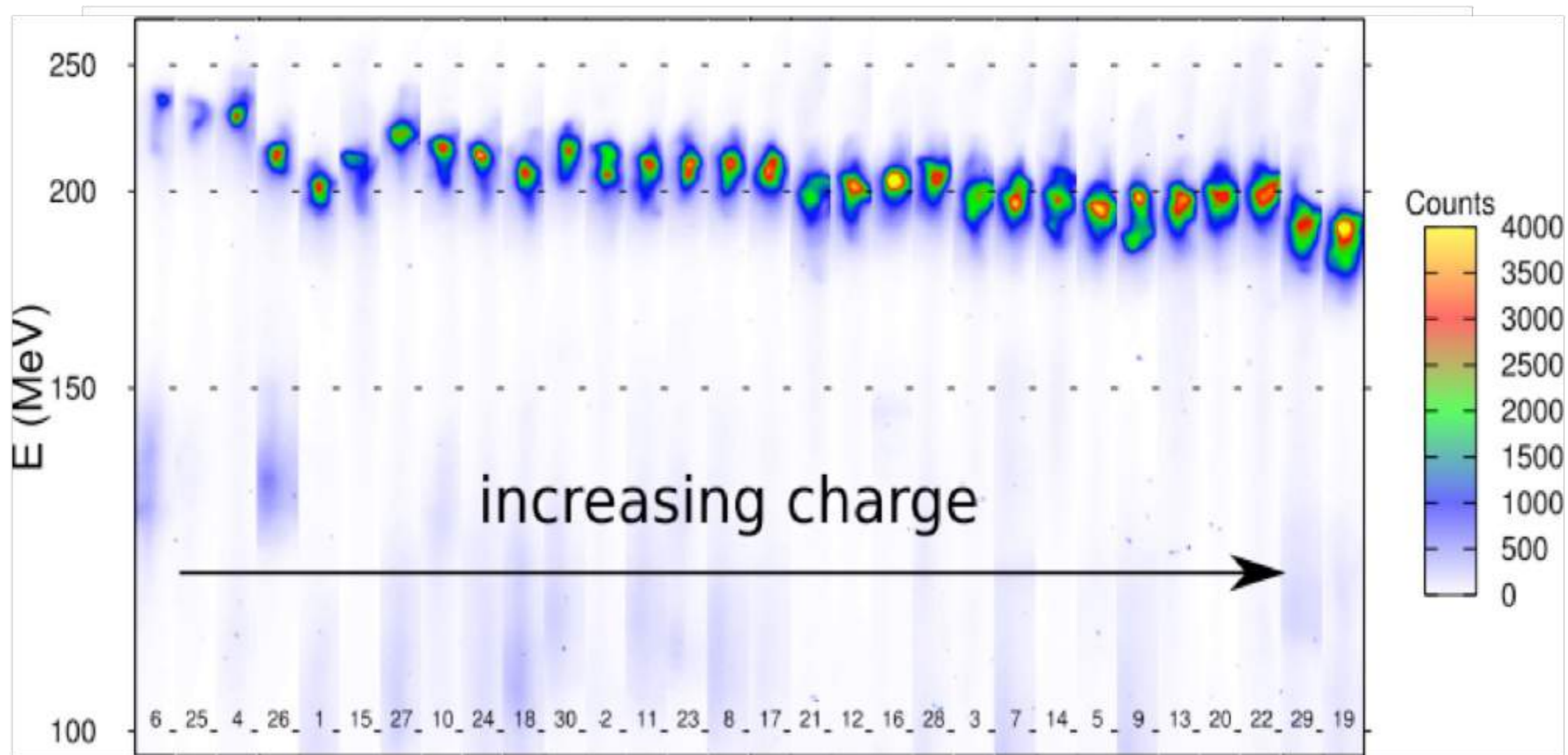
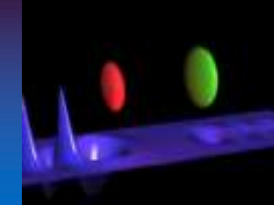
The end of the bunch
experiments a modified
wakefield

Limitation of the accelerated charge
Influence on energy and energy spread

Observables : correlation charge/energy spread/energy

T. Katsouleas *et al.*, (1987), M. Tzoufras *et al.*, *Phys. Rev. Lett.*, **101** (2008)

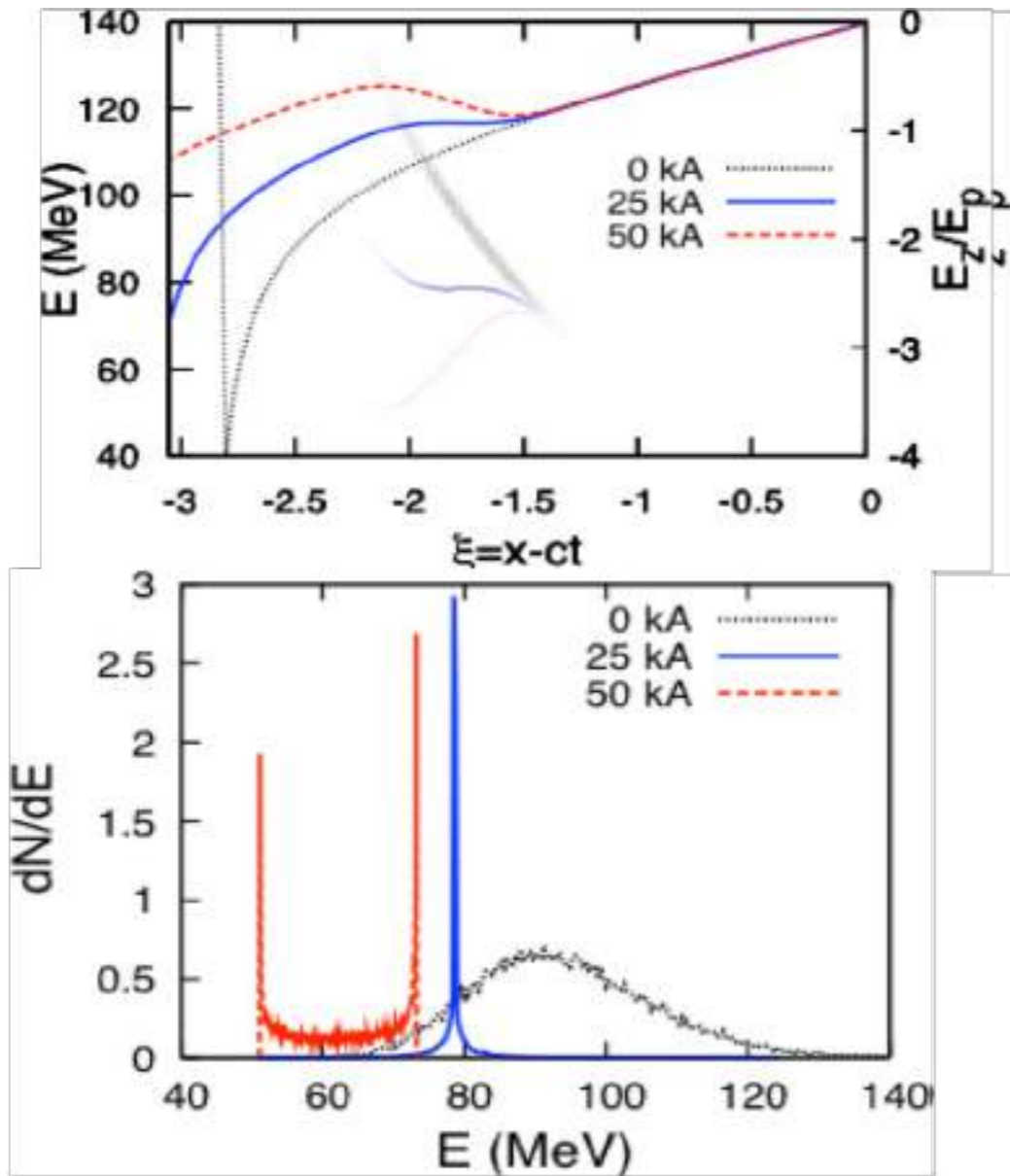
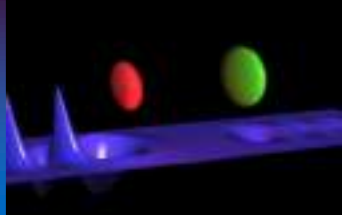
e⁻ beam dynamics in plasma waves: beam loading



Clear correlation !

Nb: very few electrons at low energy
 $\delta E/E=5\%$ limited by the spectrometer

e- beam dynamics in plasma wave: beam loading



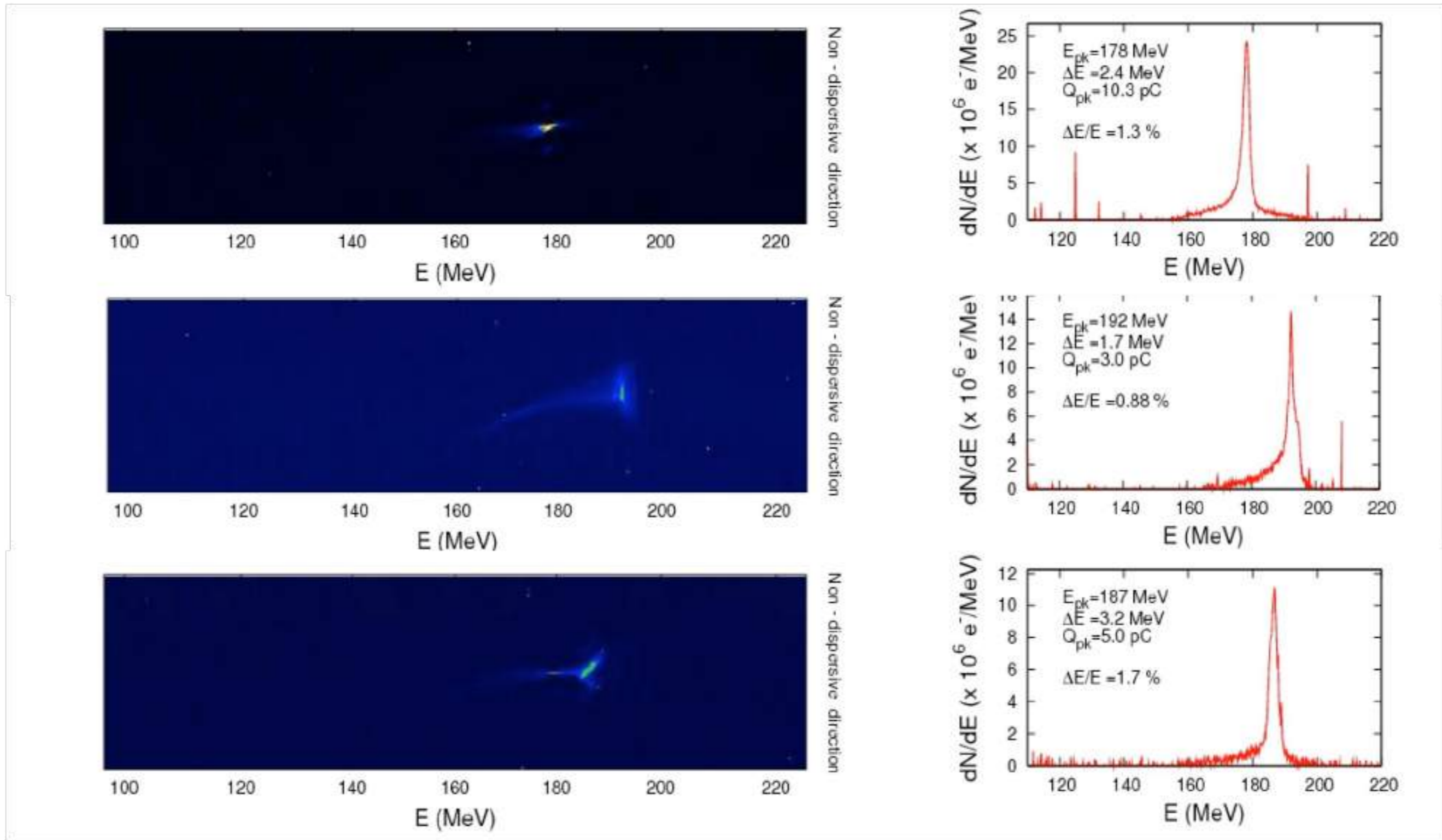
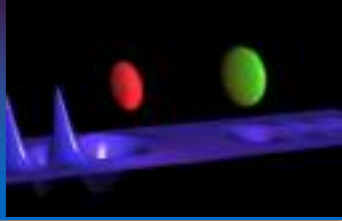
Low charge
=> large energy spread

Optimal charge
=> flat E field
=> low energy spread

High charge
=> End of the beam decelerated
=> high energy spread

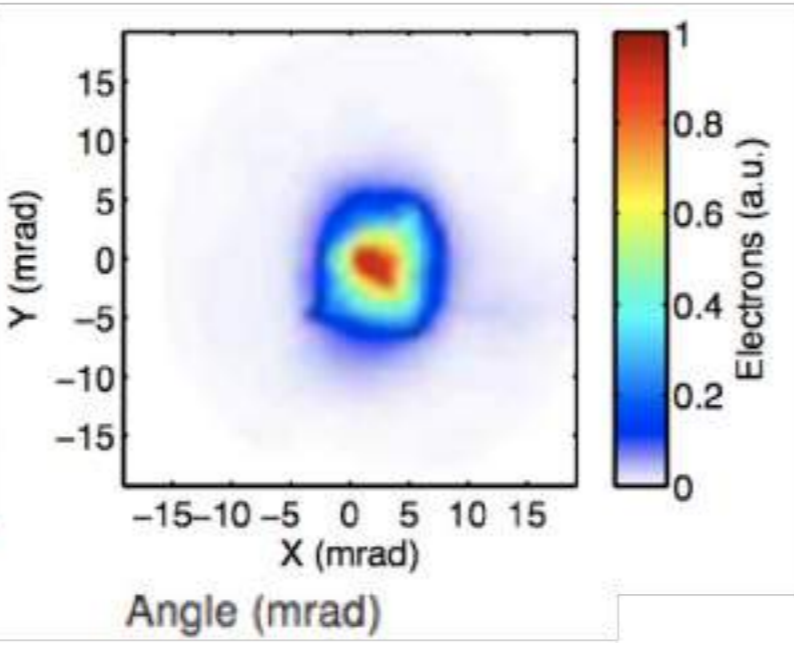
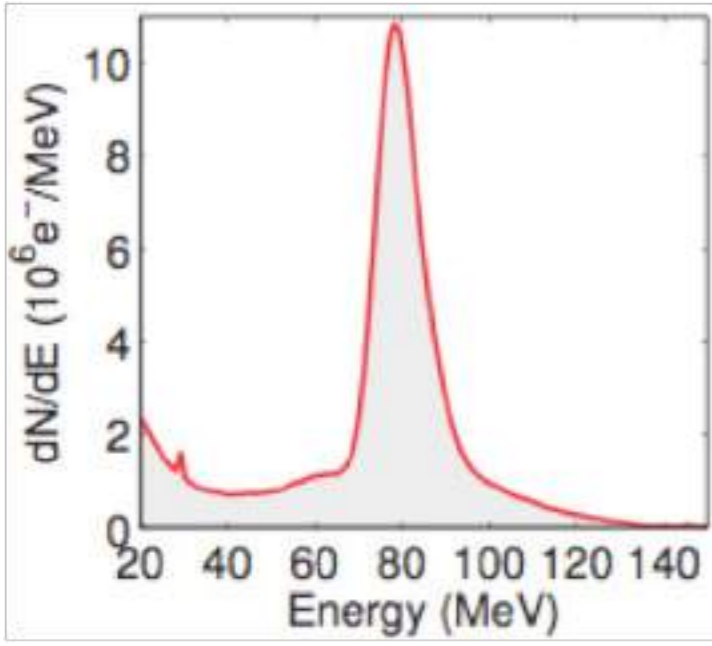
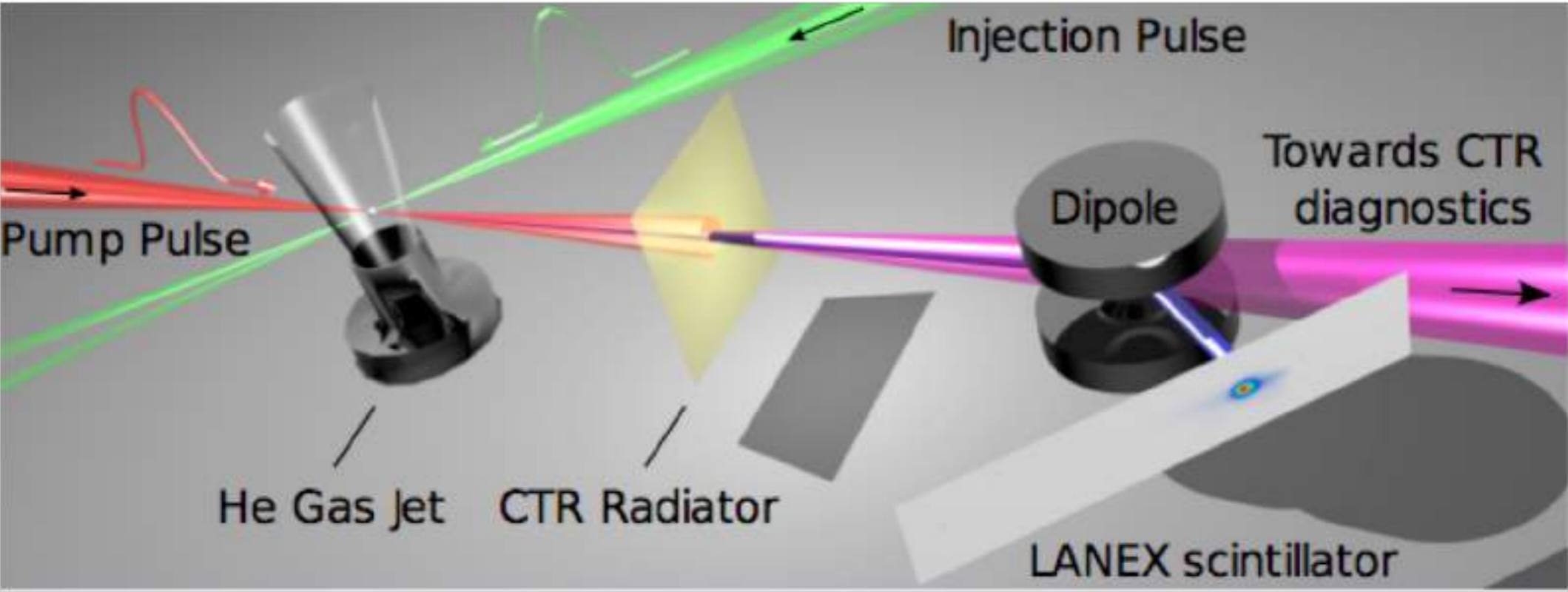
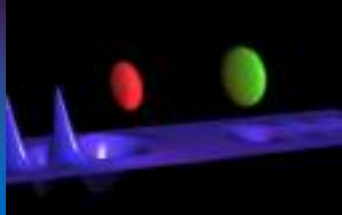
Observables : correlation charge/energy spread/energy

1% relative energy spread !



C. Rechatin *et al.*, Phys. Rev. Lett. **102**, 194804 (2009)

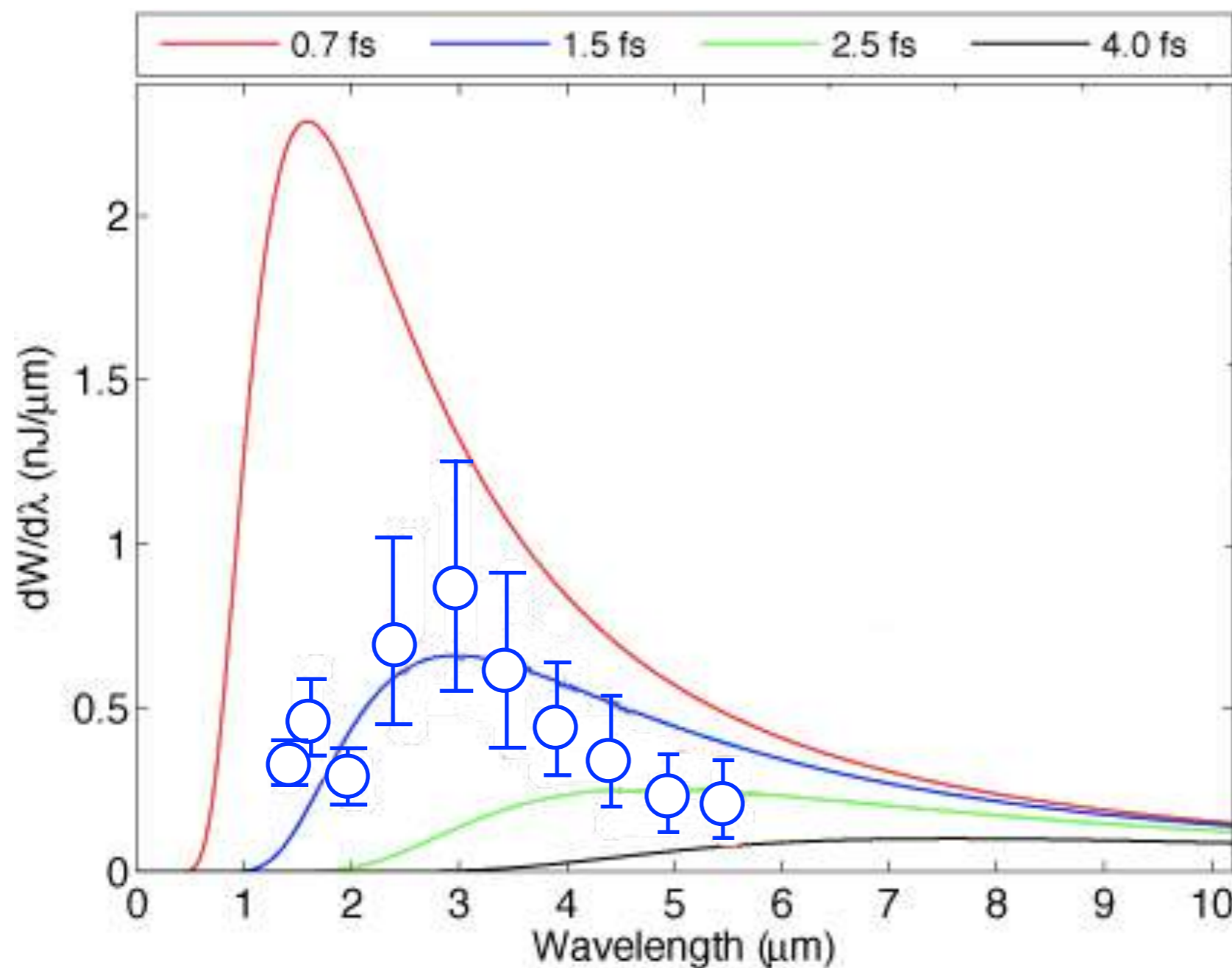
Bunch length measurement : CTR diagnostic



$E=84 (\pm 21)$ MeV, $\Delta E^*=20(\pm 17)$ MeV
 *after the foil

$Q=15(\pm 7)$ pC and $\Delta\theta=6 (\pm 1.6)$ mrad

1.5 fs RMS duration : Peak current of 4 kA



Analytic CTR model

Gaussian pulse shape

Measured e-beam :

Charge

Energy

Divergence

Bunch duration

Peak wavelength

Peak intensity

Spectral features

Peak at 3 μm

Coherent

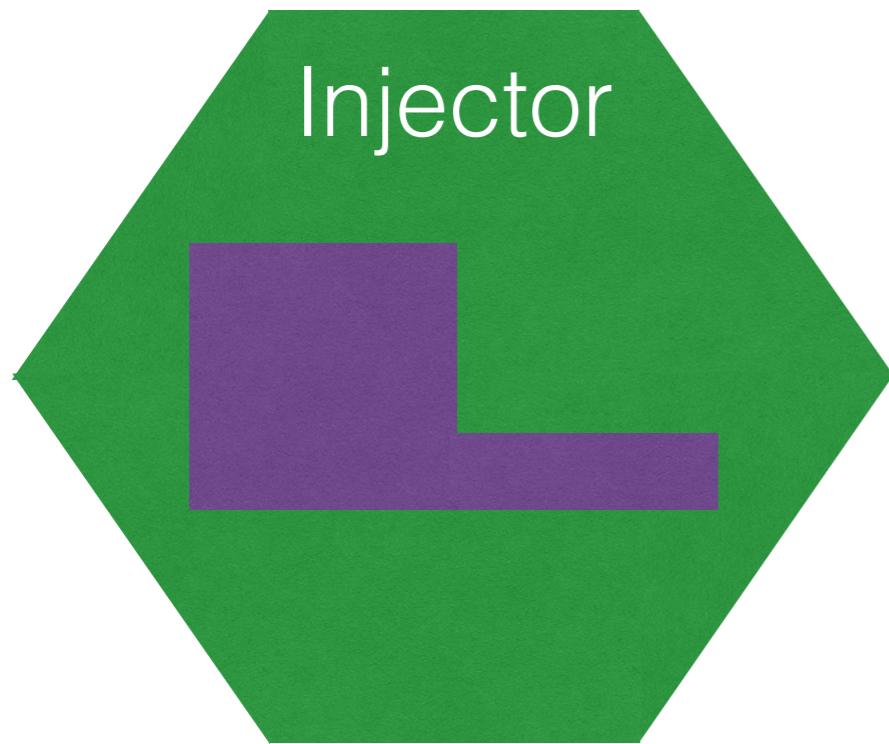
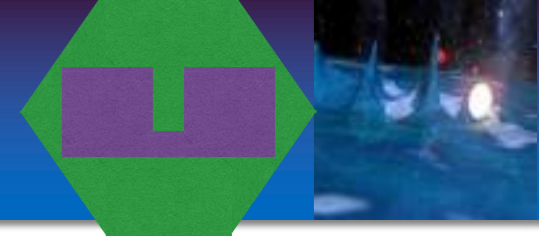
1.5 fs RMS duration : Peak current of 4 kA



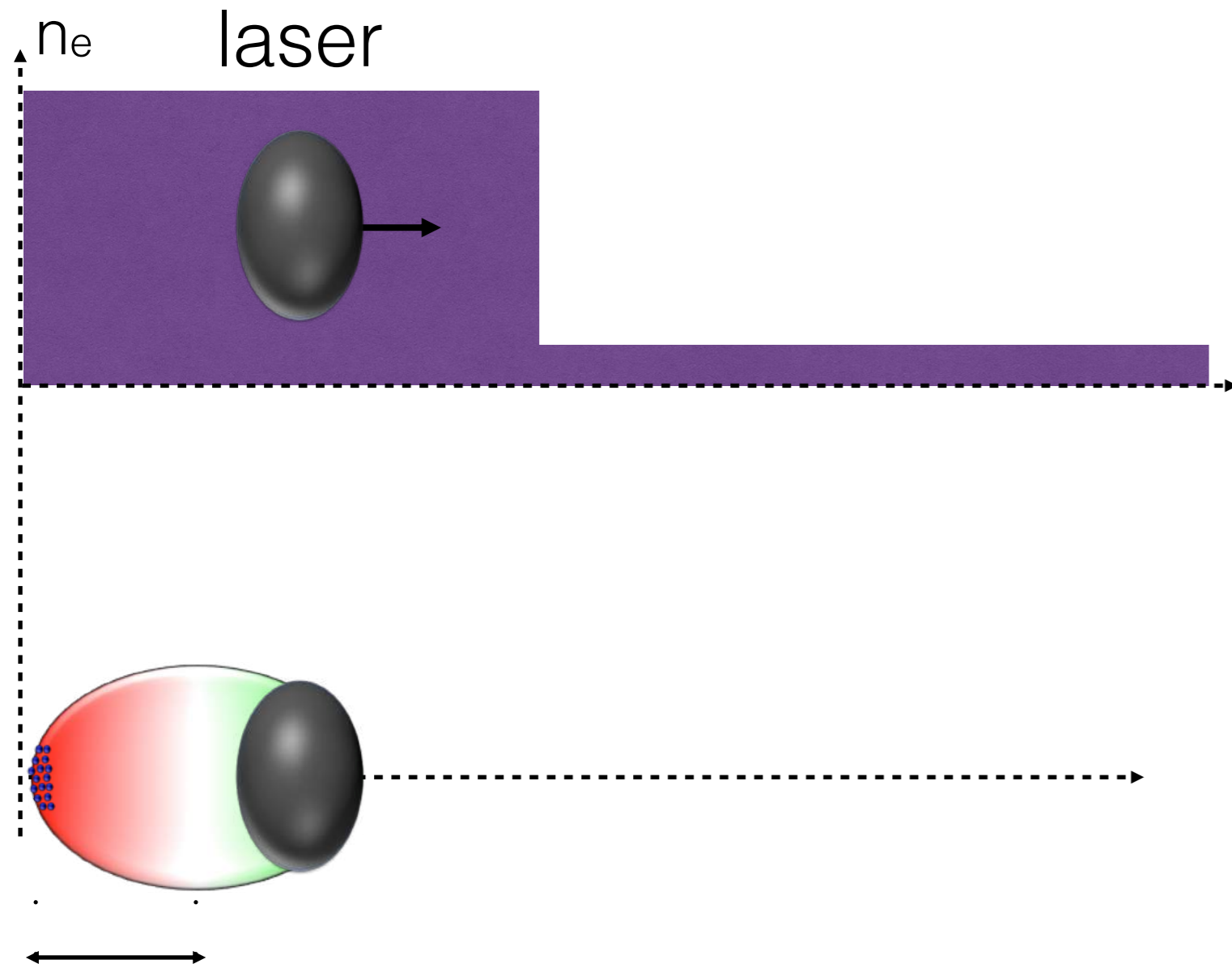
O. Lundh et al., Nature Physics, **7** (2011)

Laser Plasma Accelerators : Outline

- Introduction : context and motivations
- Colliding laser pulses scheme
- Injection in a density gradient
- Manipulating the longitudinal momentum
- Manipulating the transverse momentum
- Applications
- Conclusion and perspectives



Injection in a sharp density gradient



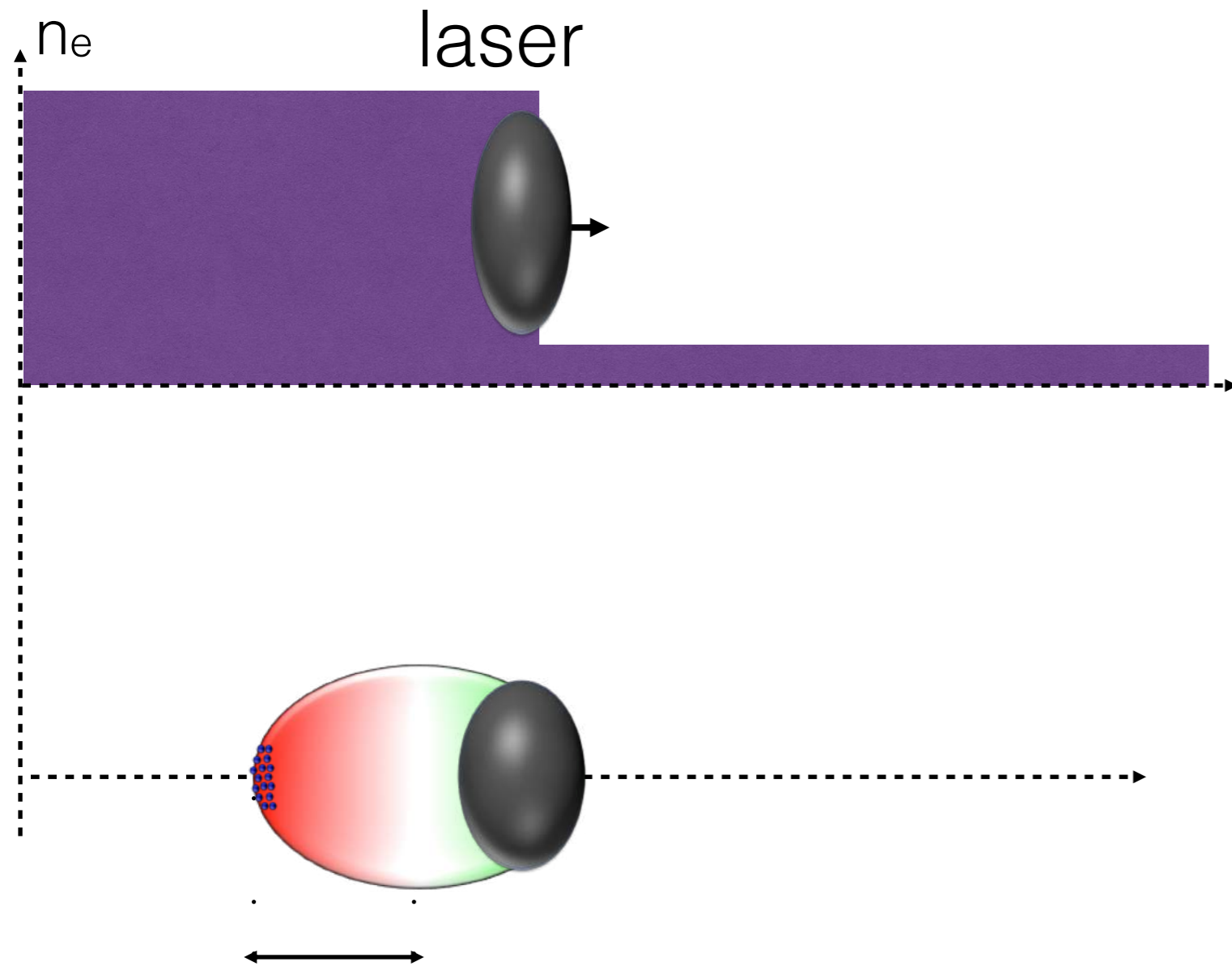
Density drop => increase of the cavity length

the bubble expansion allows electrons injection and energy gain.

Sharp density ramp is required to localize the injection and reduce the energy spread !

[Schmid et al., 2010; Buck et al., 2013]

Injection in a sharp density gradient

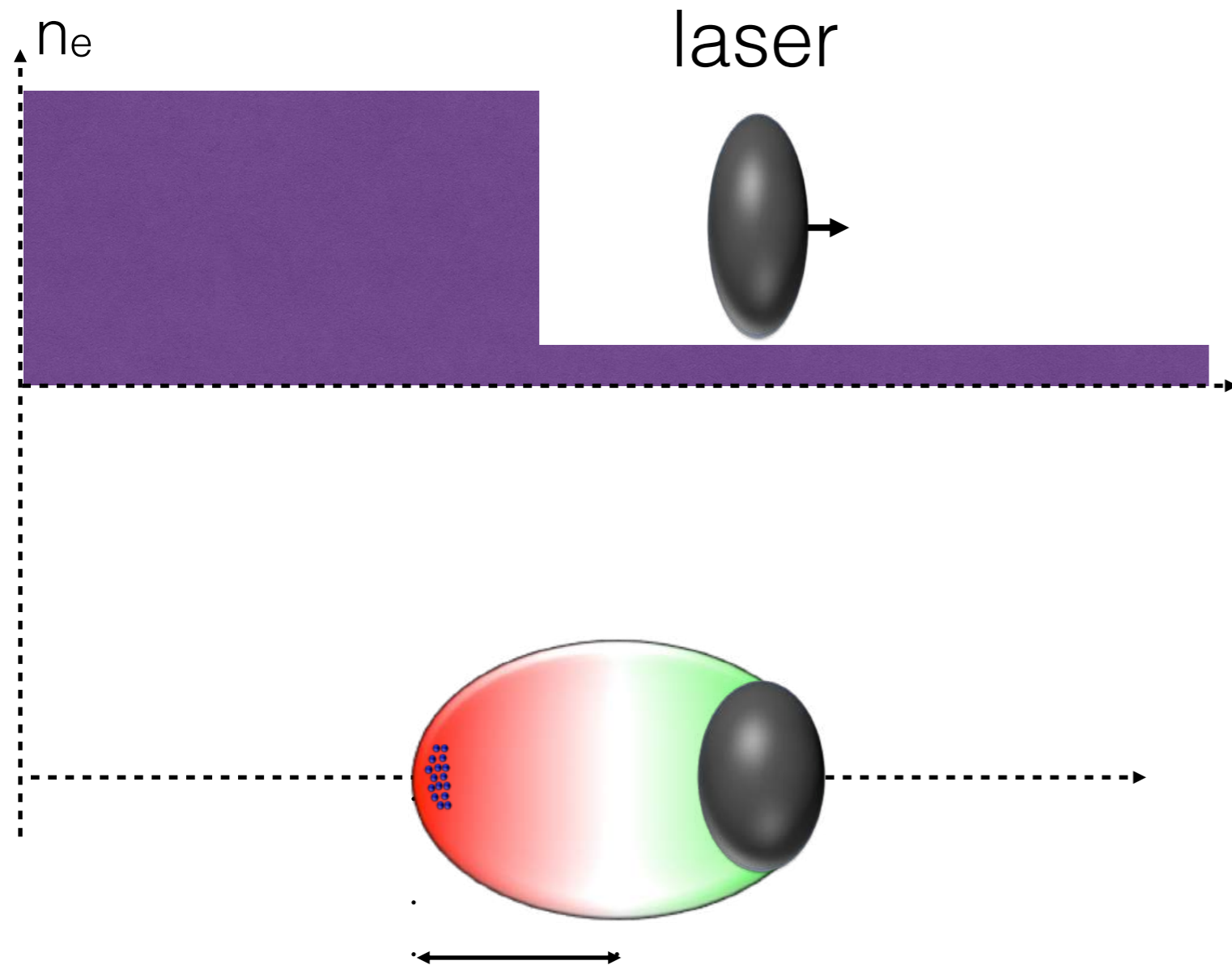


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Injection in a sharp density gradient

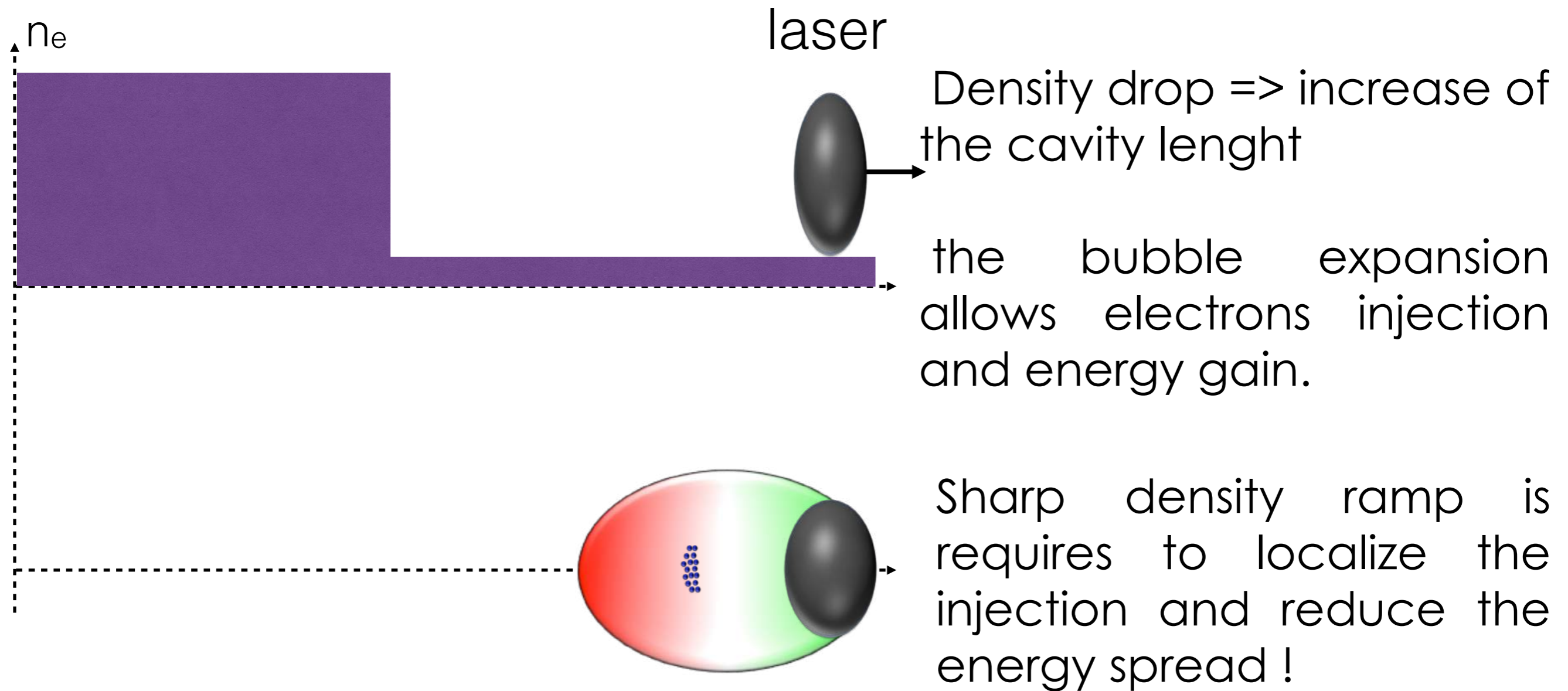


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Sharp density ramp is required to localize the injection and reduce the energy spread !

Injection in a sharp density gradient

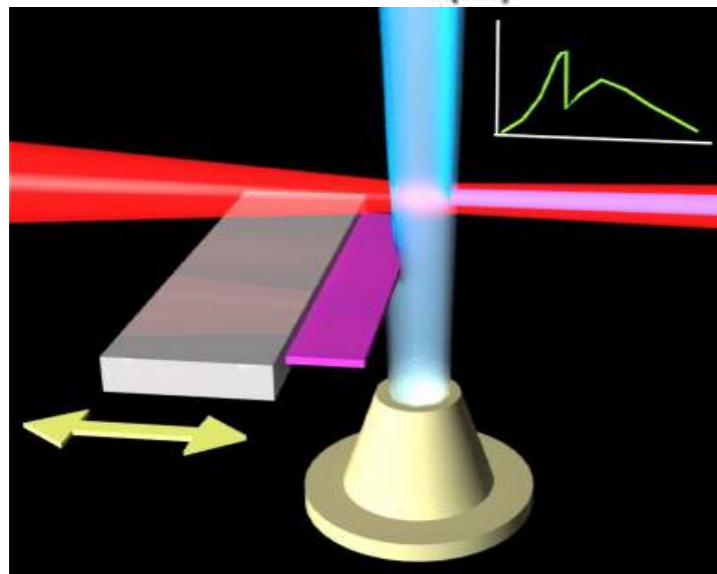
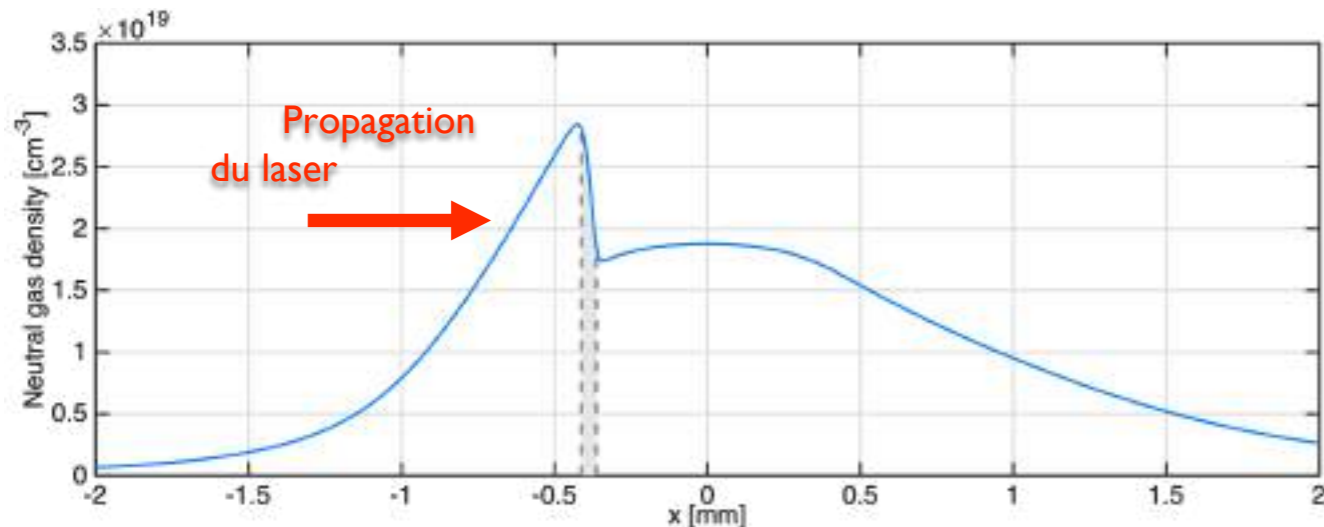
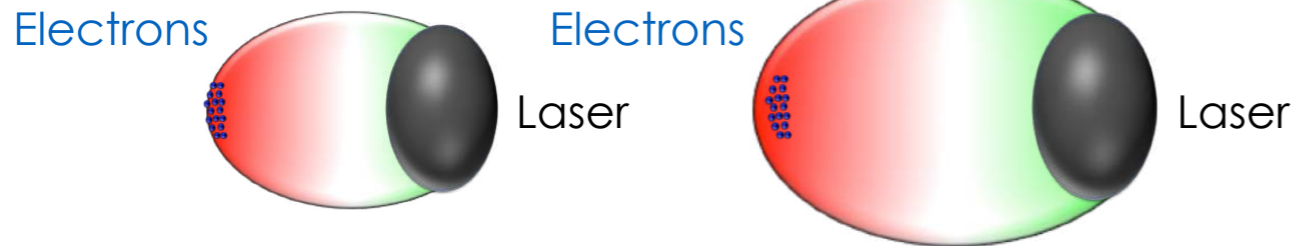


Injection in a shock front : principle

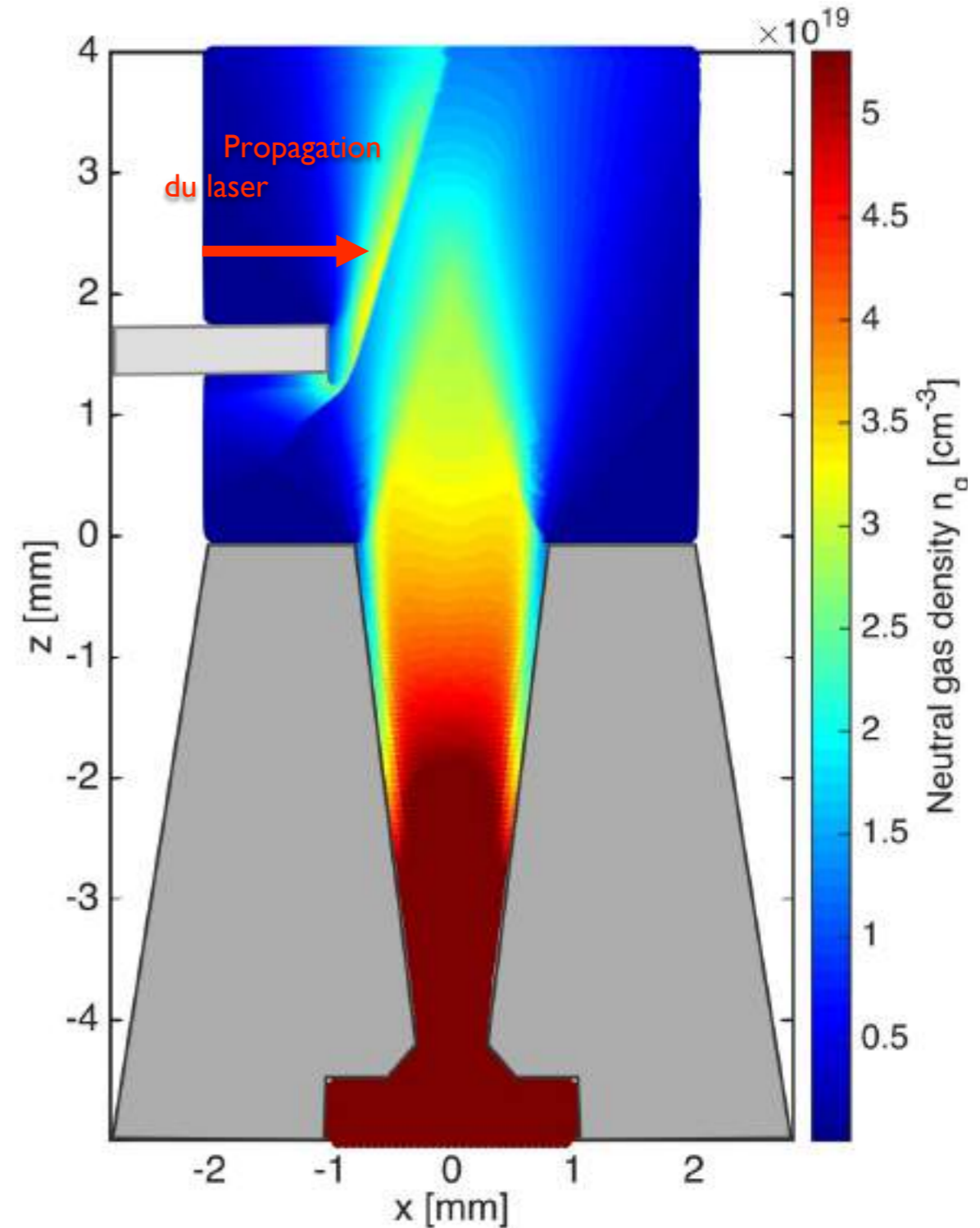


Plasma cavity before the shock front

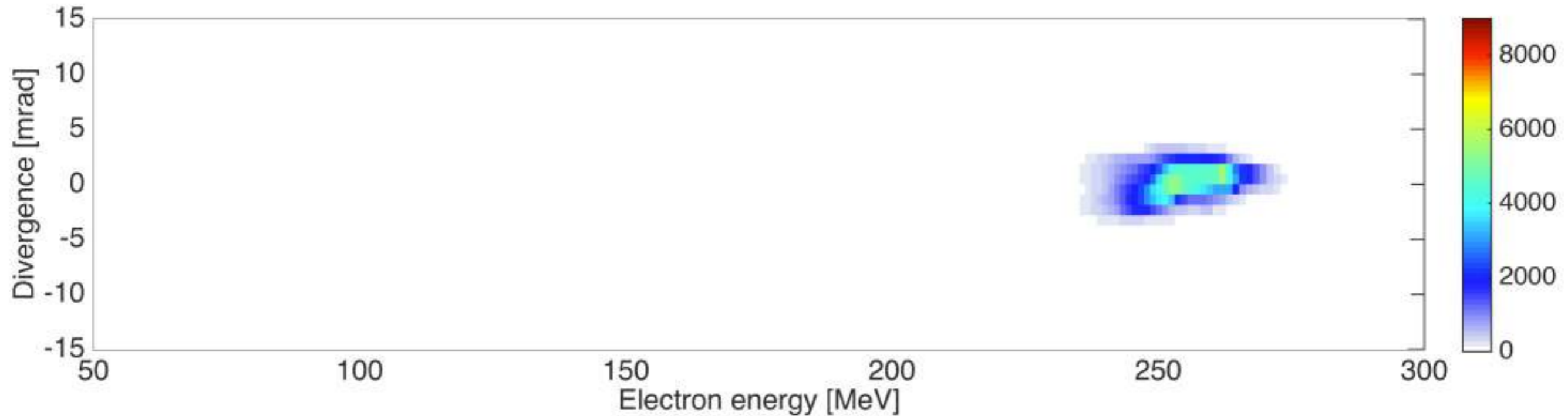
Plasma cavity after the shock front



Simulations ANSYS Fluent



Injection in a shock front : pur helium gas



Generation of a stable e-beam ($n_2 = 7.5 \times 10^{18} \text{ cm}^{-3}$) :

$$E_{peak} = 256.5 \pm 4 \text{ MeV}$$

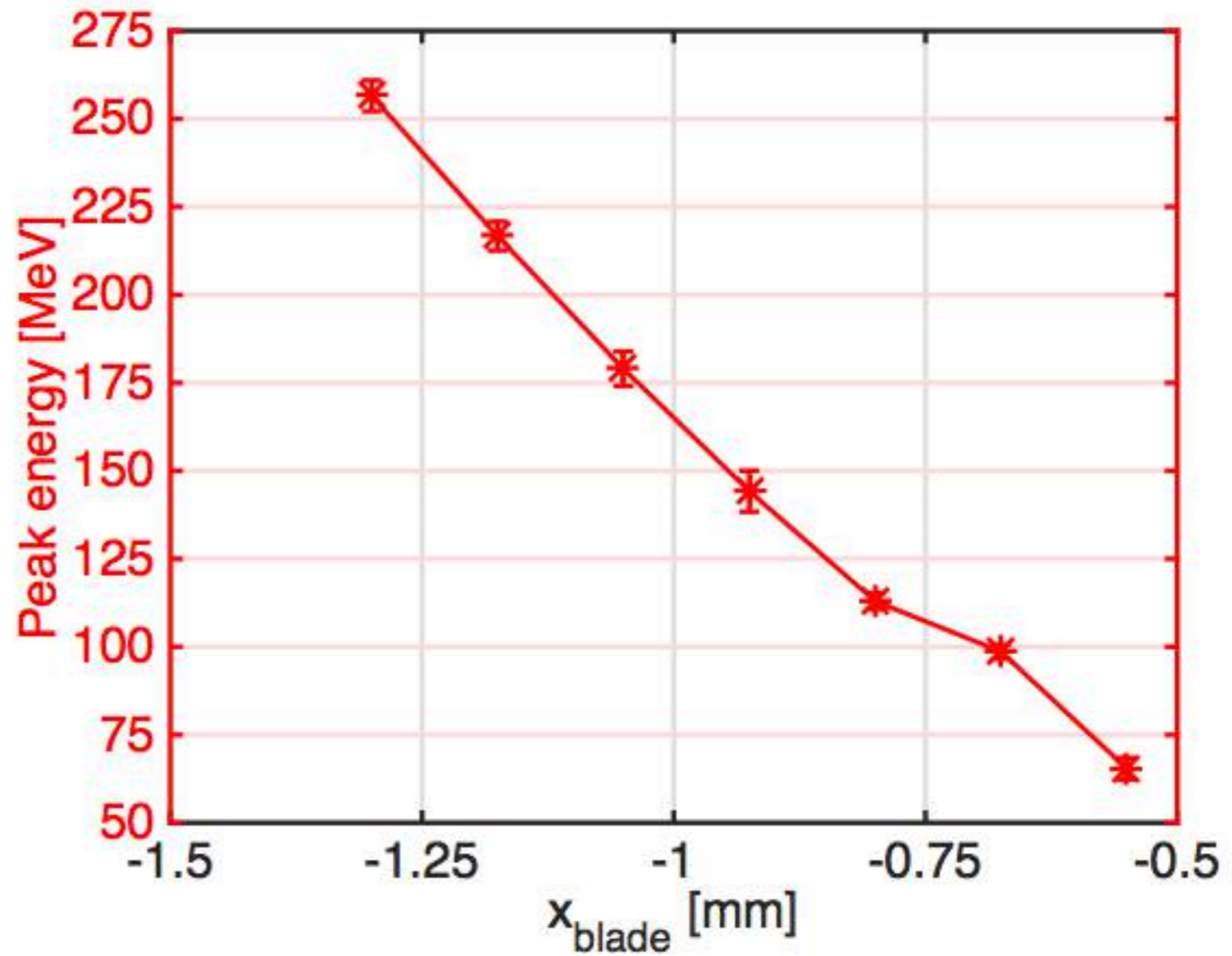
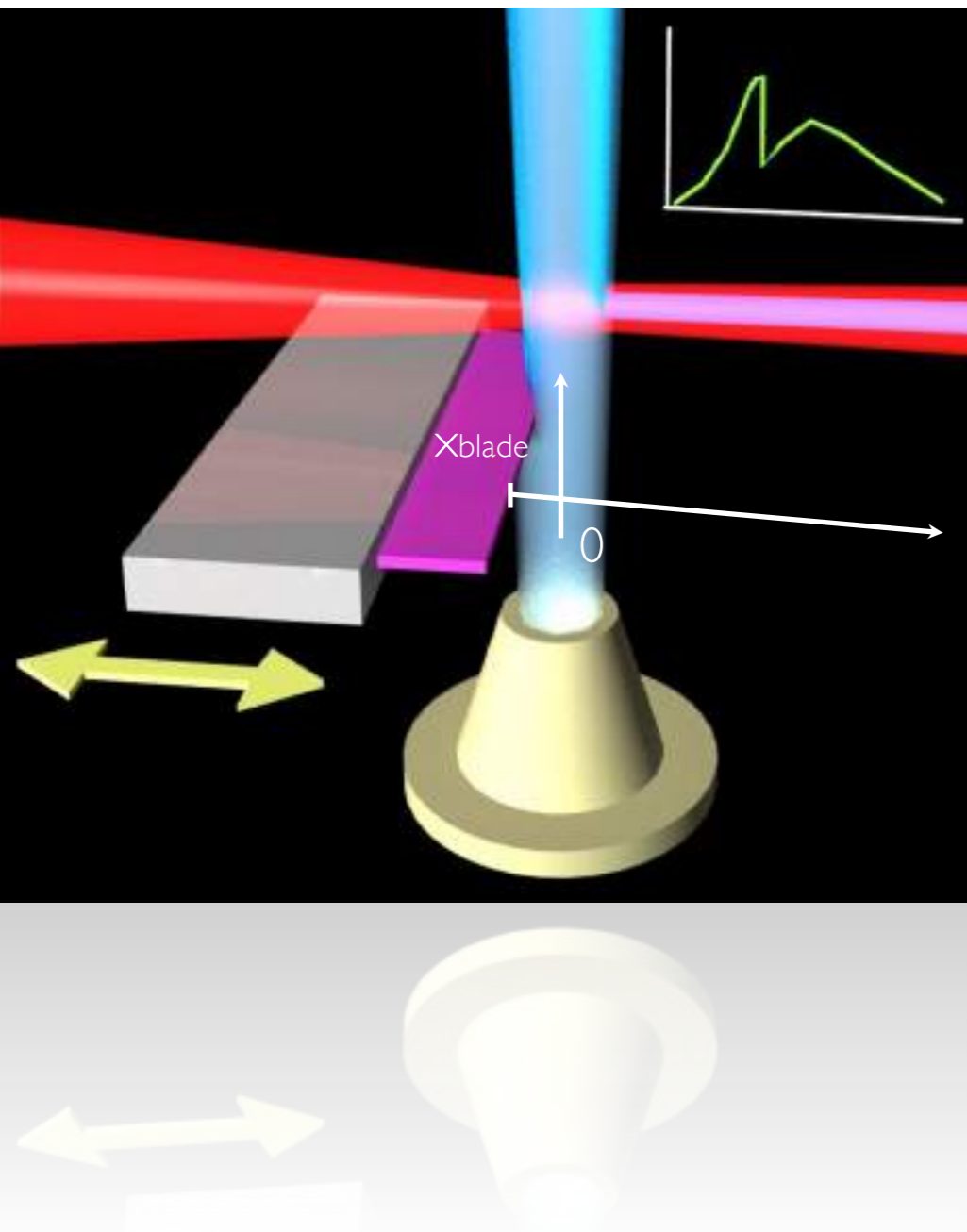
$$\Delta E = 15.5 \pm 2 \text{ MeV}$$

$$\Delta E / E = 6 \pm 1\%$$

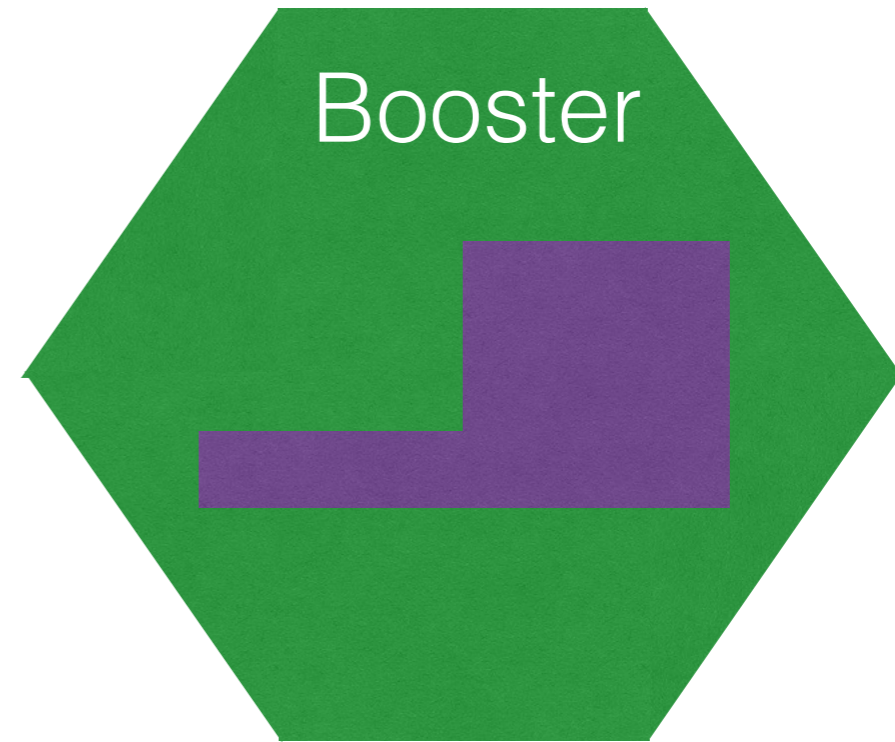
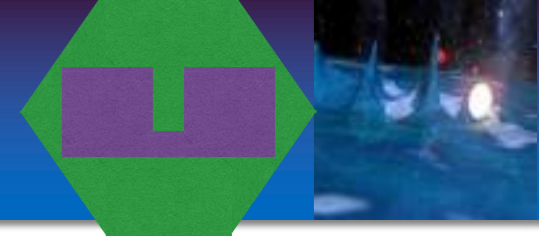
$$Q_{peak} = 3.2 \pm 0.4 \text{ pC}$$

$$\text{Divergence} = 2.0 \pm 0.3 \text{ mrad}$$

Injection in a shock front : pur helium gas



Electron energies is controlled by the position of the blade

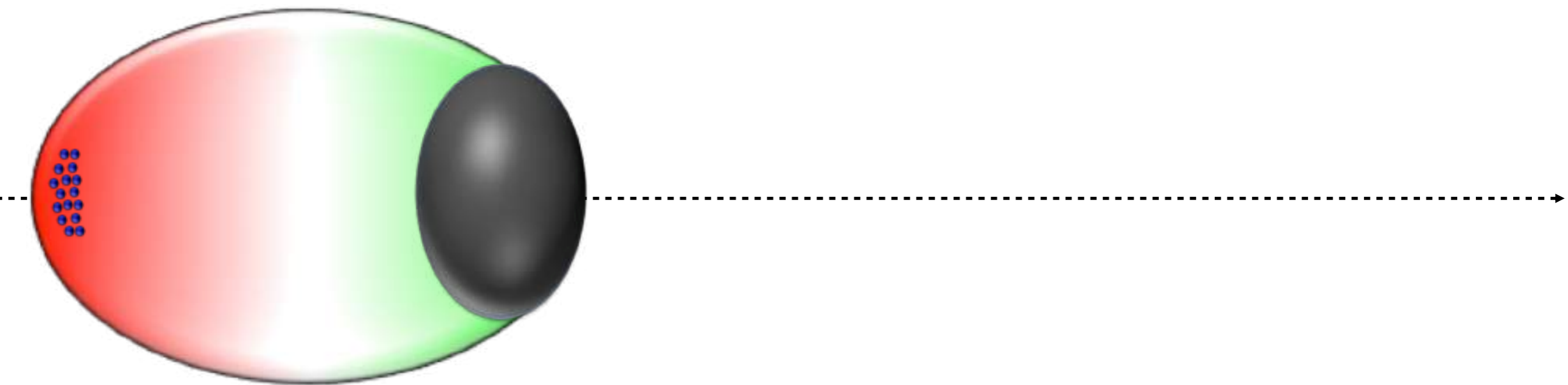


Overcoming the dephasing limit



Since the laser group velocity is $< c$, when electrons energy is getting $\sim c$ they dephase

→ electrons reach the center of the cavity and start to be decelerated



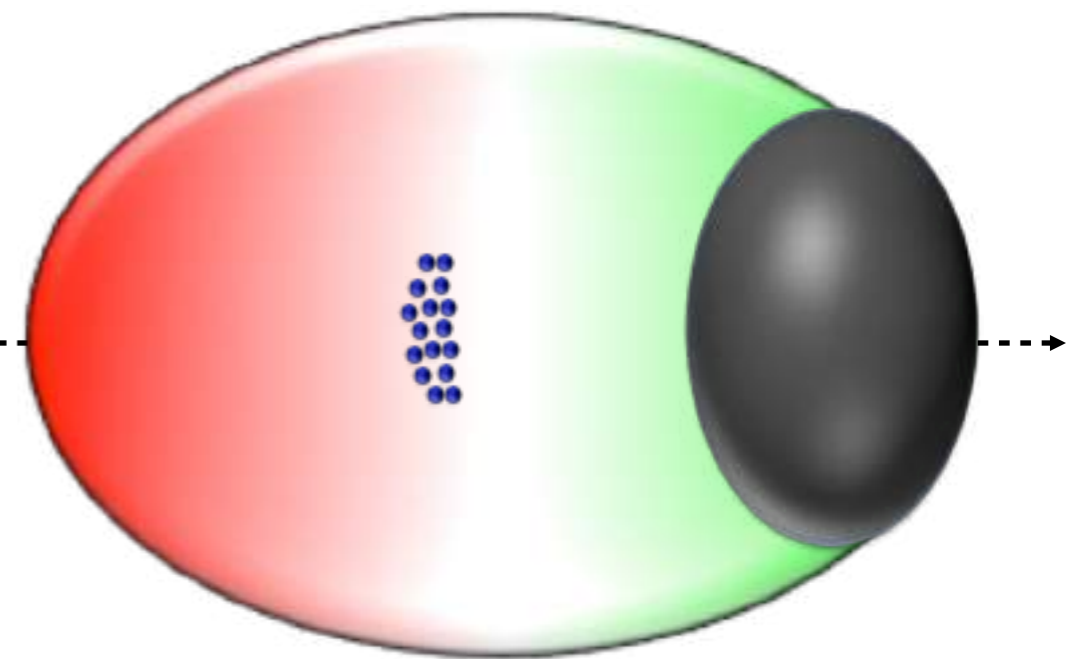
R. Lehe

Overcoming the dephasing limit



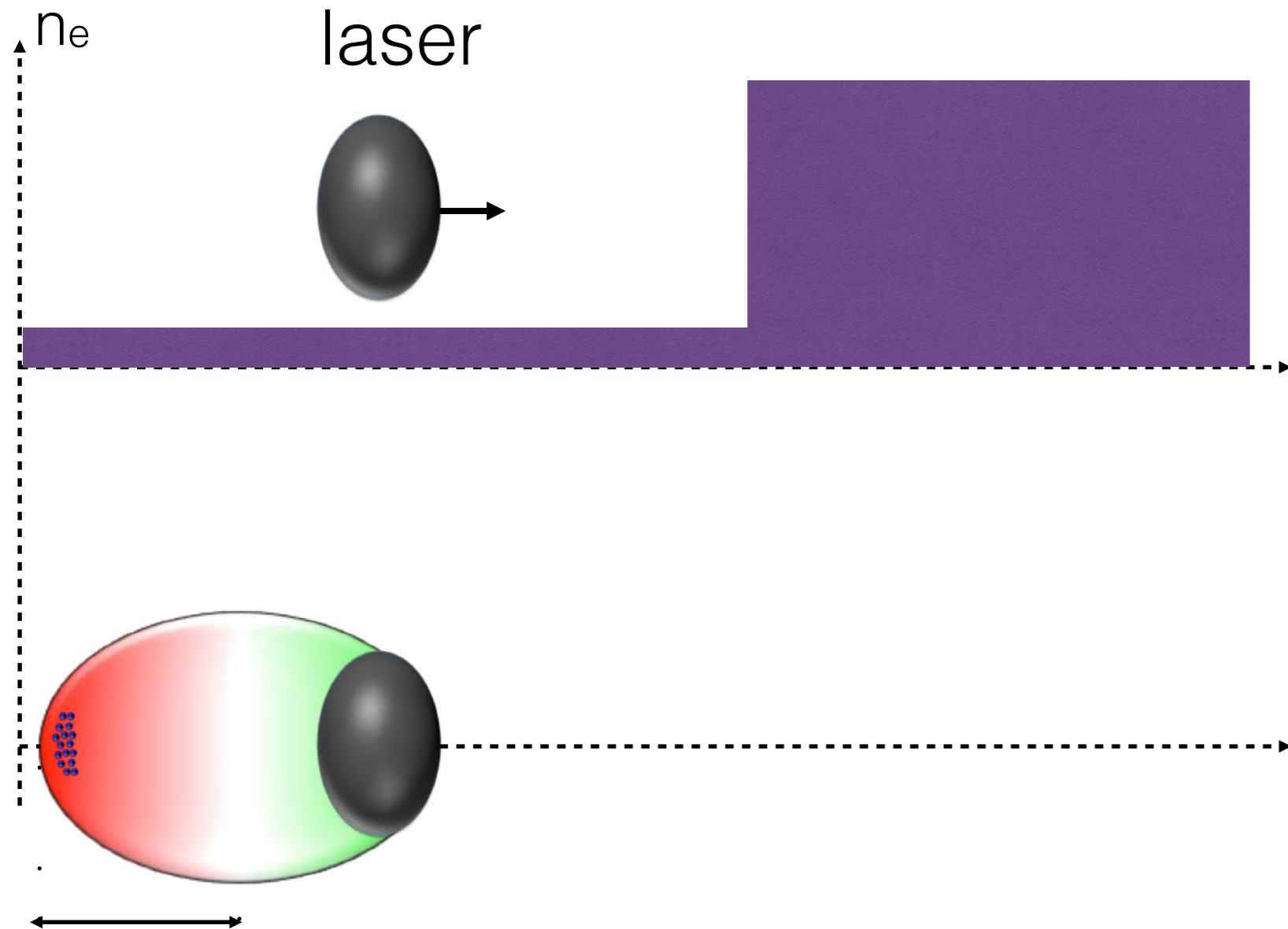
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R. Lehe

Overcoming the dephasing limit



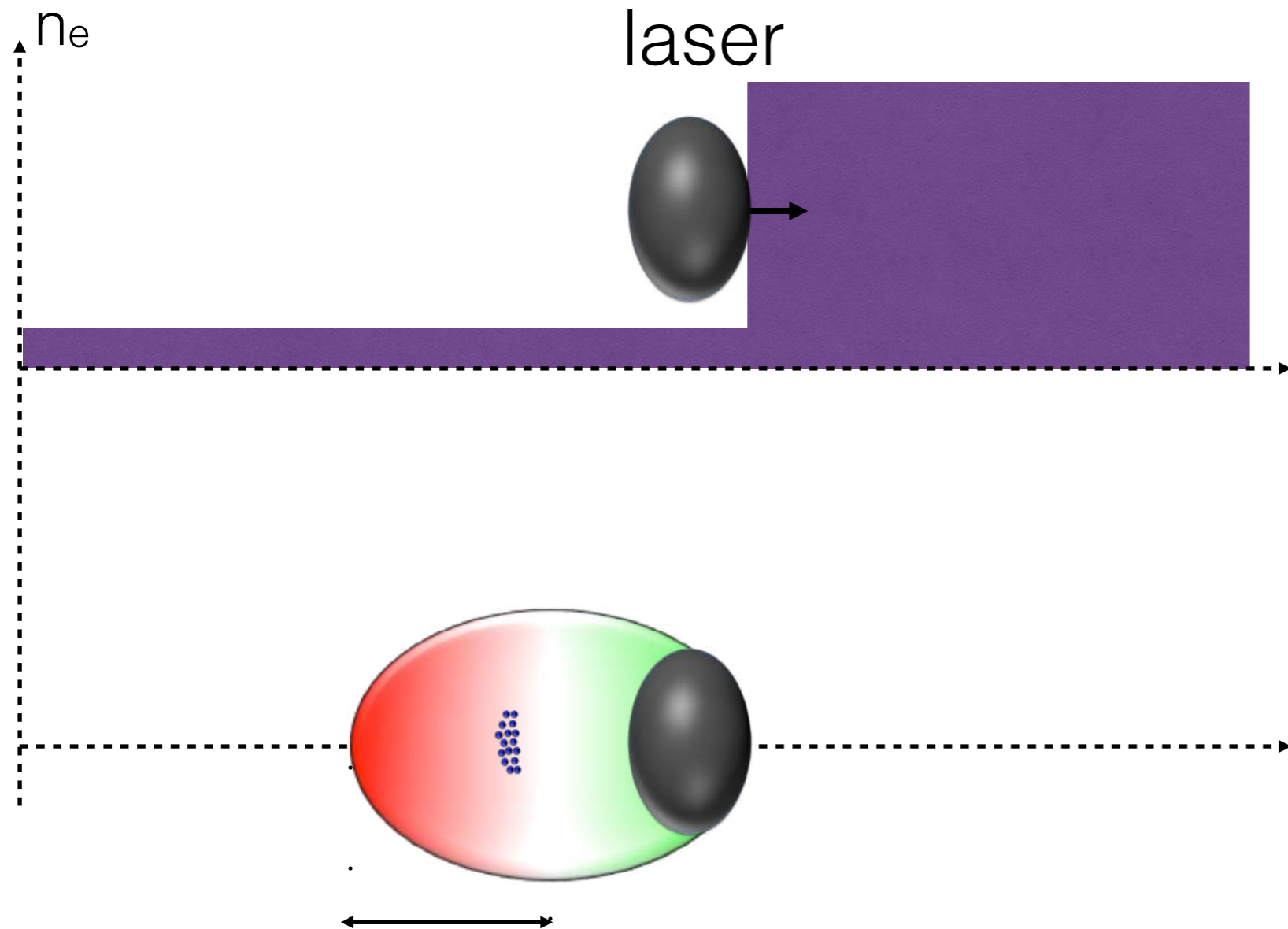
The reduction of the bubble size at the right position by increasing suddenly the density resets the electrons phase.

Electrons can start again to gain energy.

R. Lehe

[Katsouleas et al., 1986; Sprangle et al., 2001]

Overcoming the dephasing limit

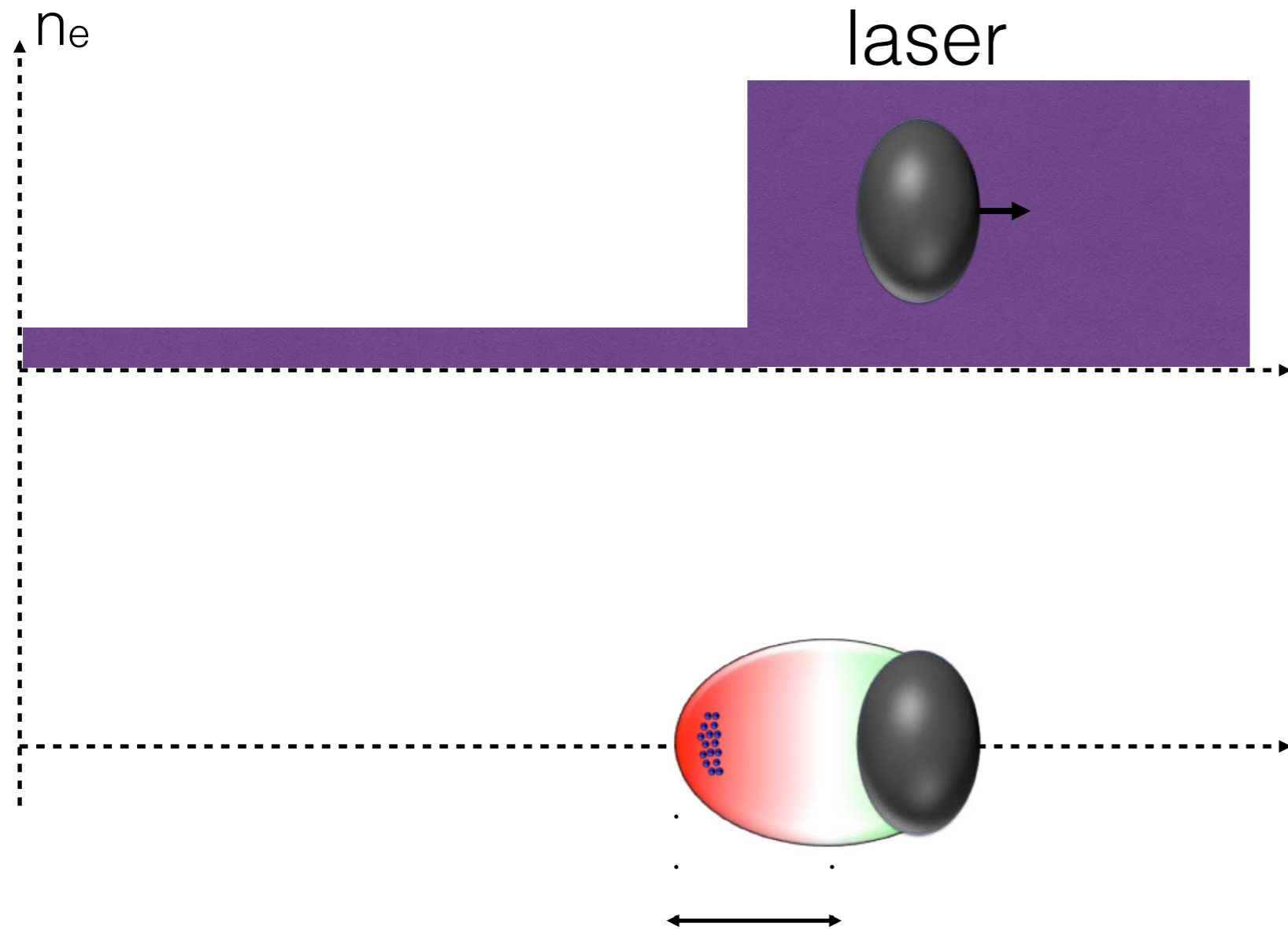


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Overcoming the dephasing limit

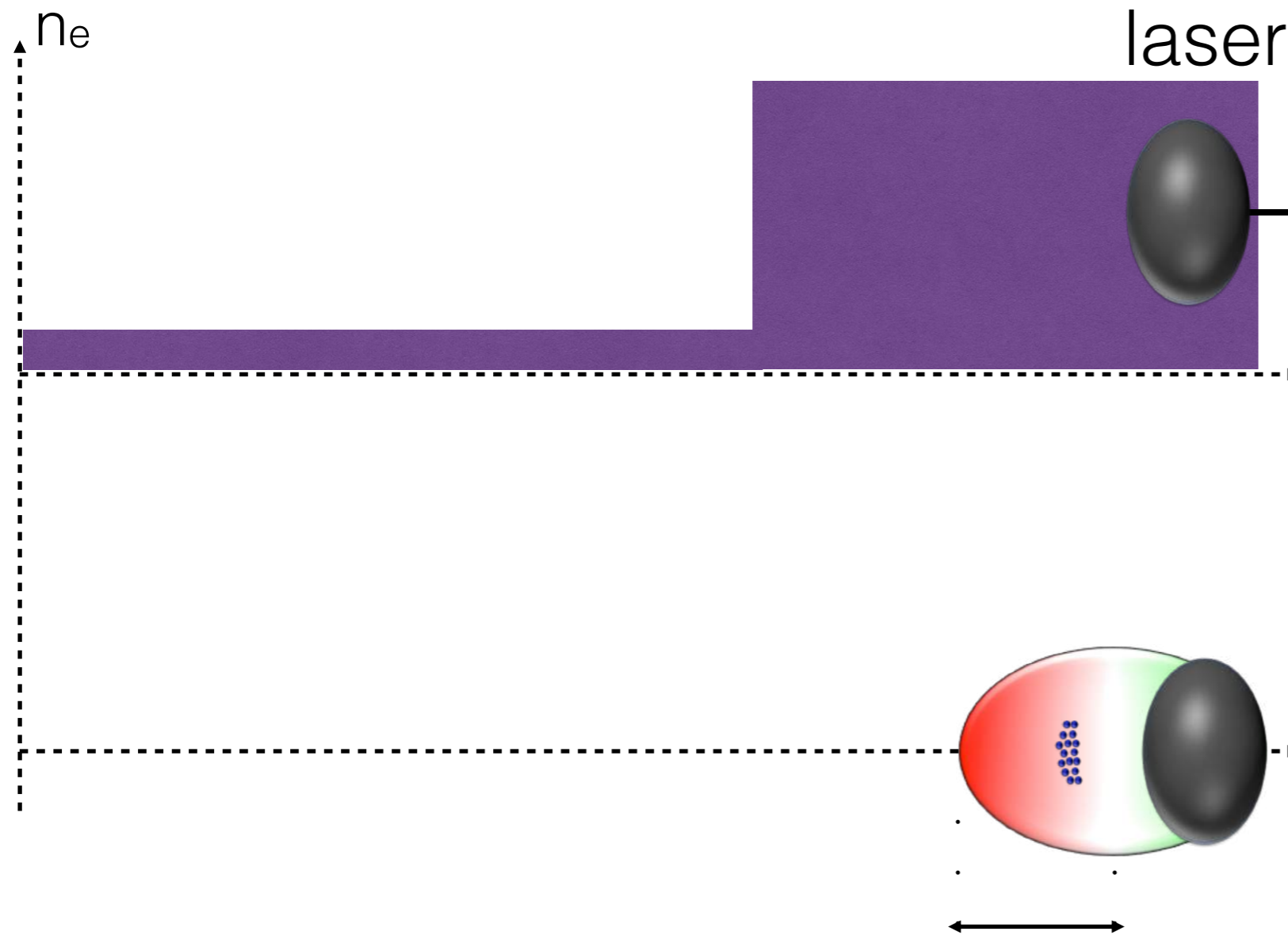


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Overcoming the dephasing limit

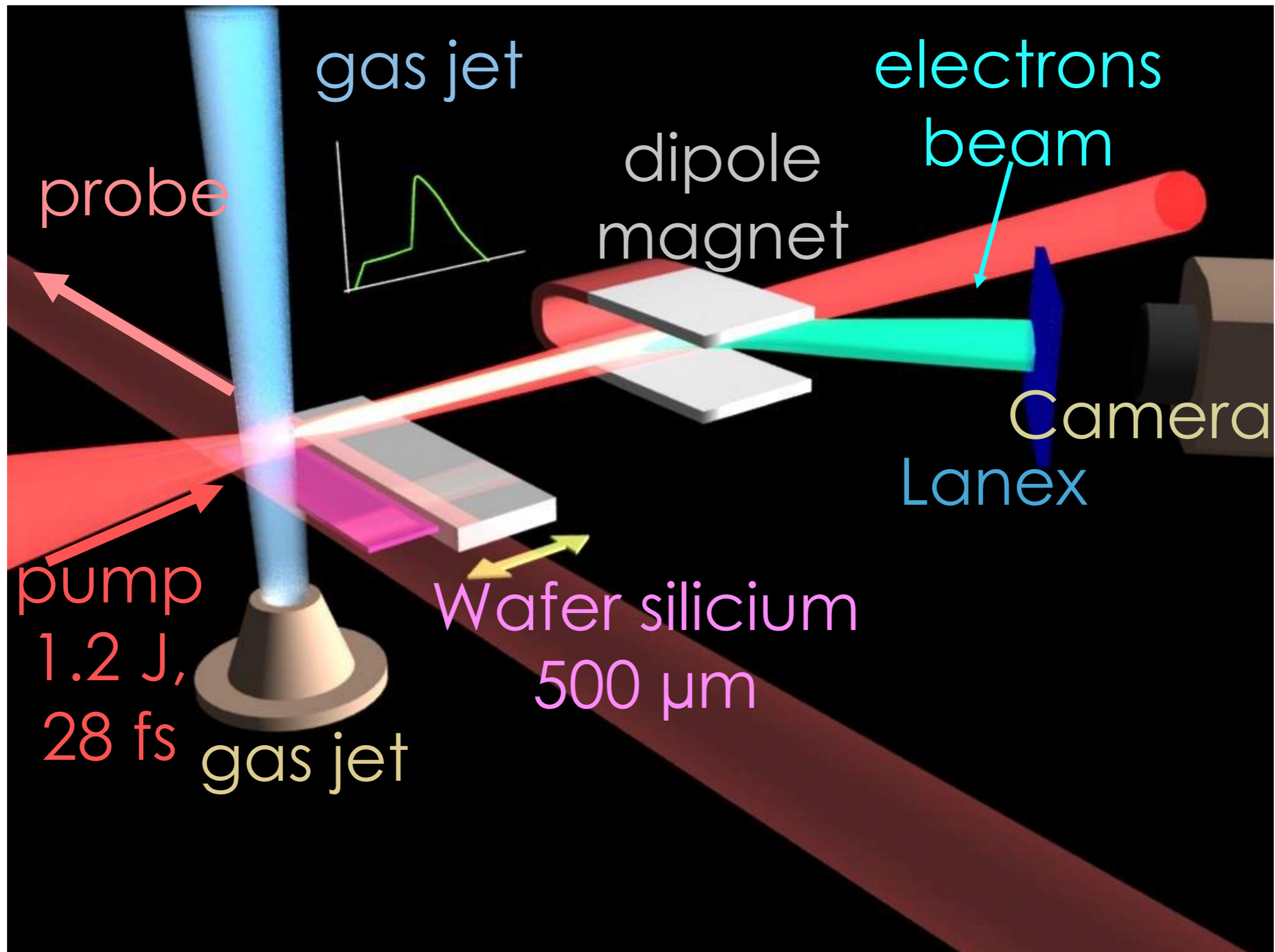


laser The reduction of the bubble size at the right position by increasing suddenly the density resets the electrons phase.

Electrons can start again to gain energy.

R. Lehe

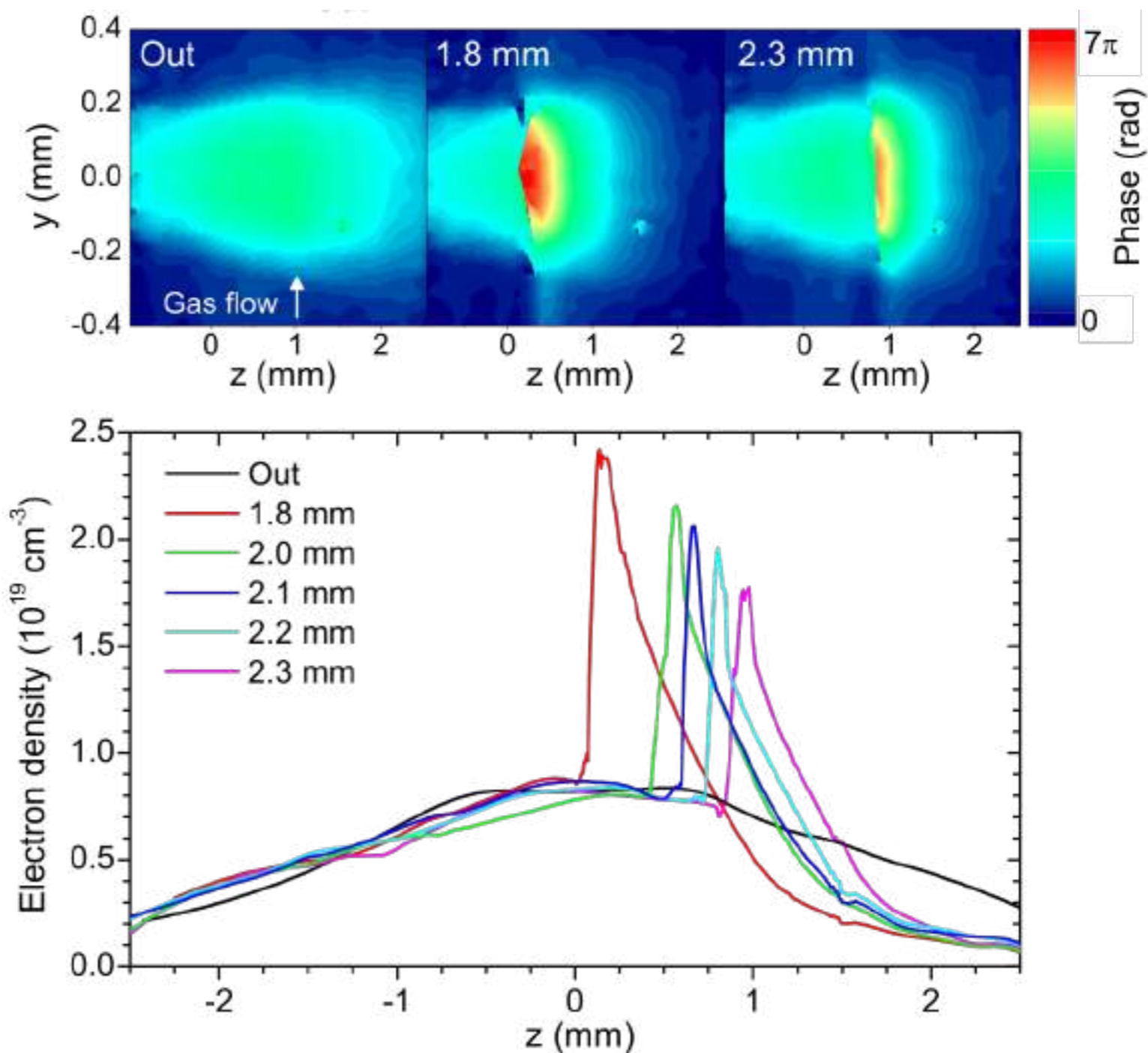
Overcoming the dephasing limit: experiments



Overcoming the dephasing limit: results



The density transition is controlled by changing the wafer position

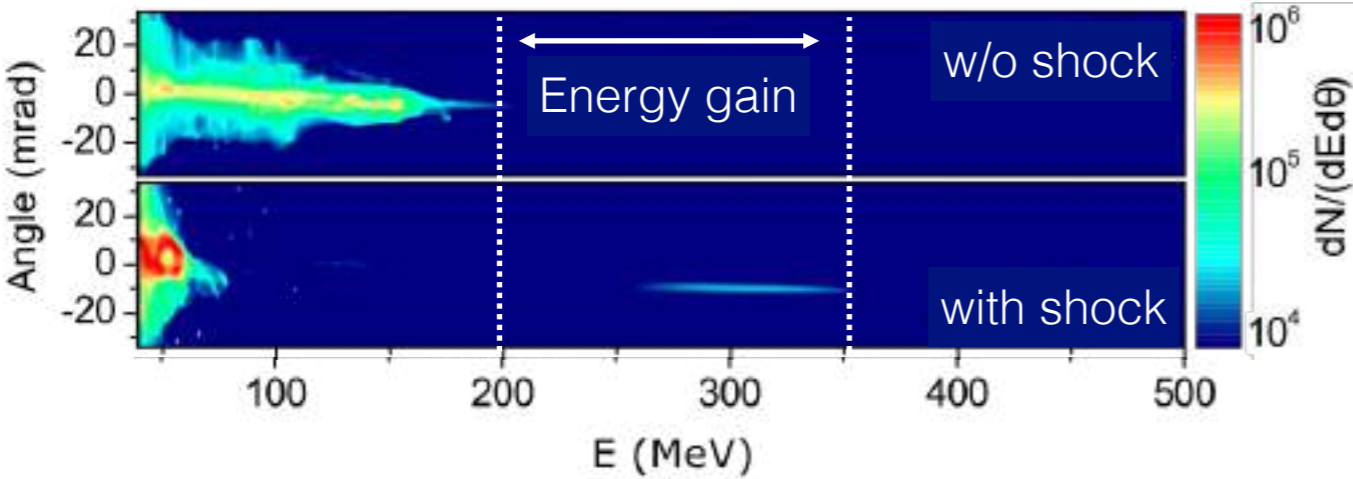


Overcoming the dephasing limit: experimental results & simulations

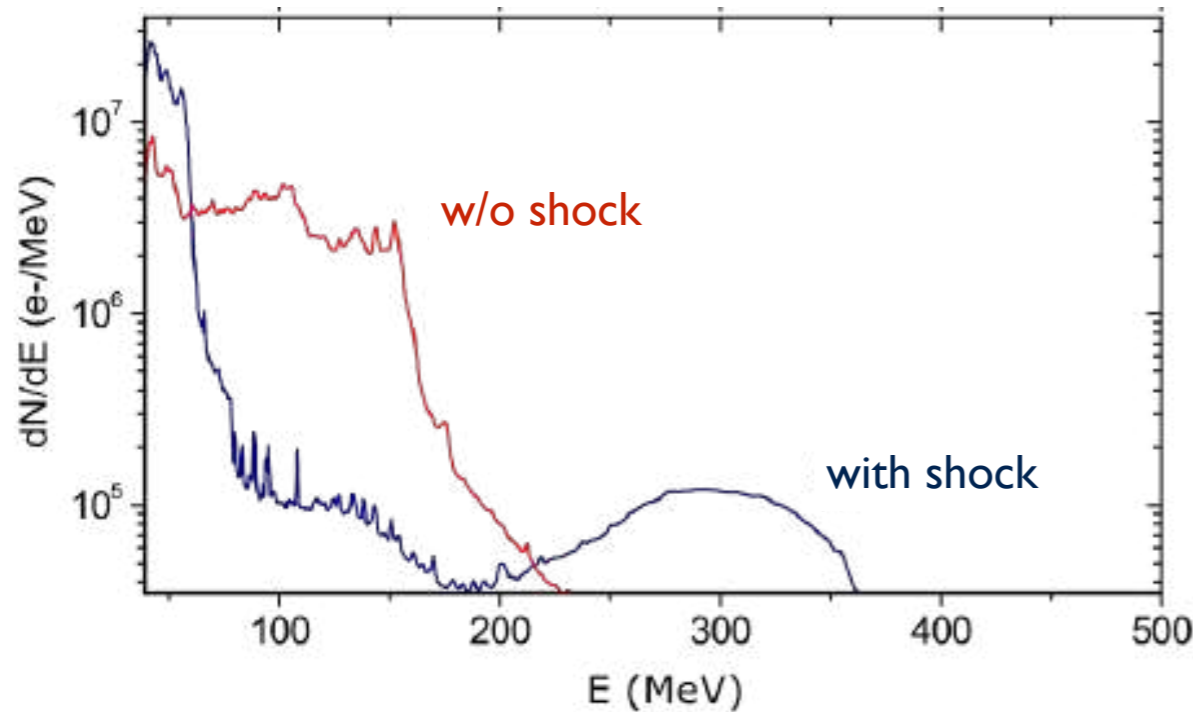


Experiment

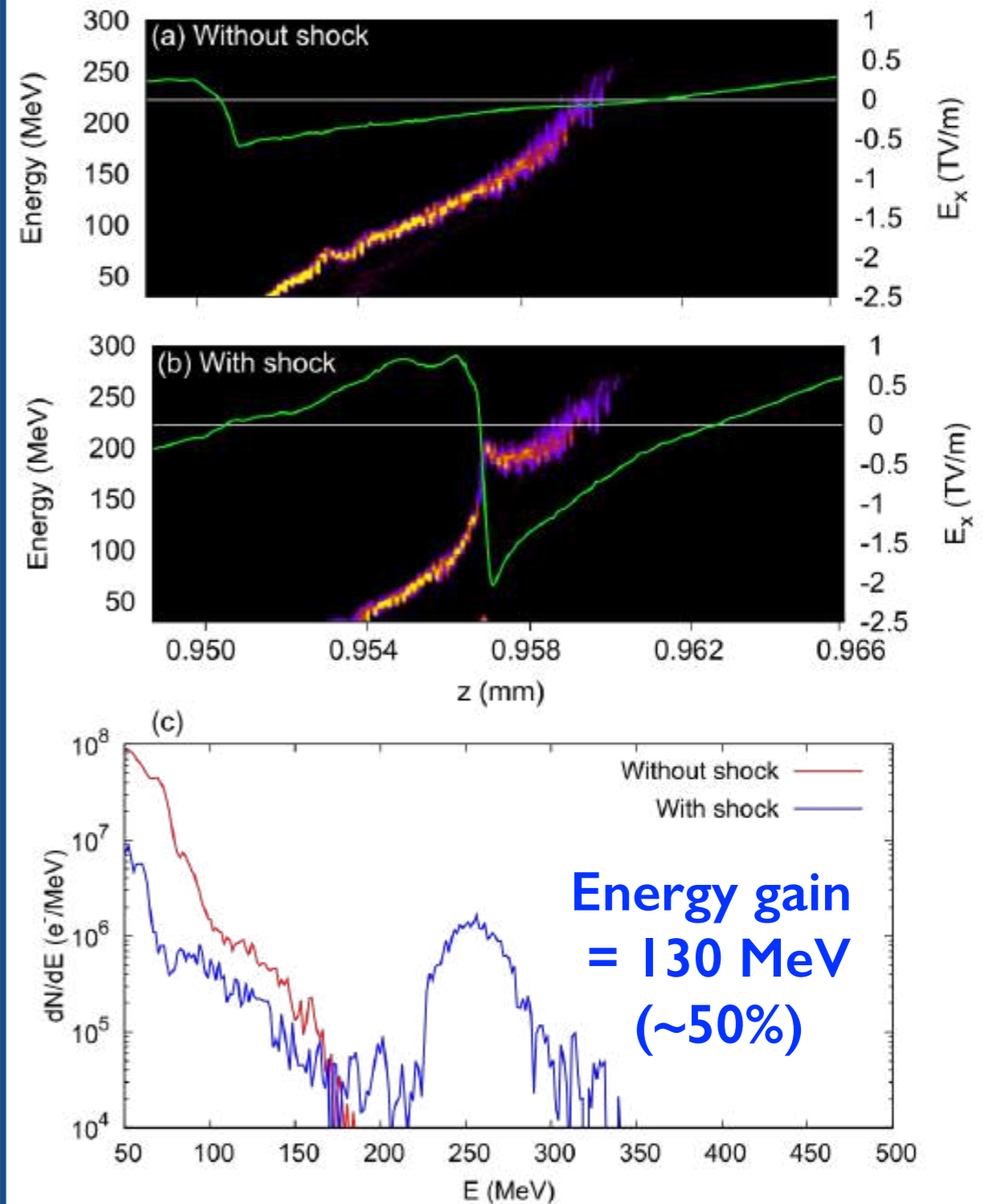
2D dispersion corrected spectra



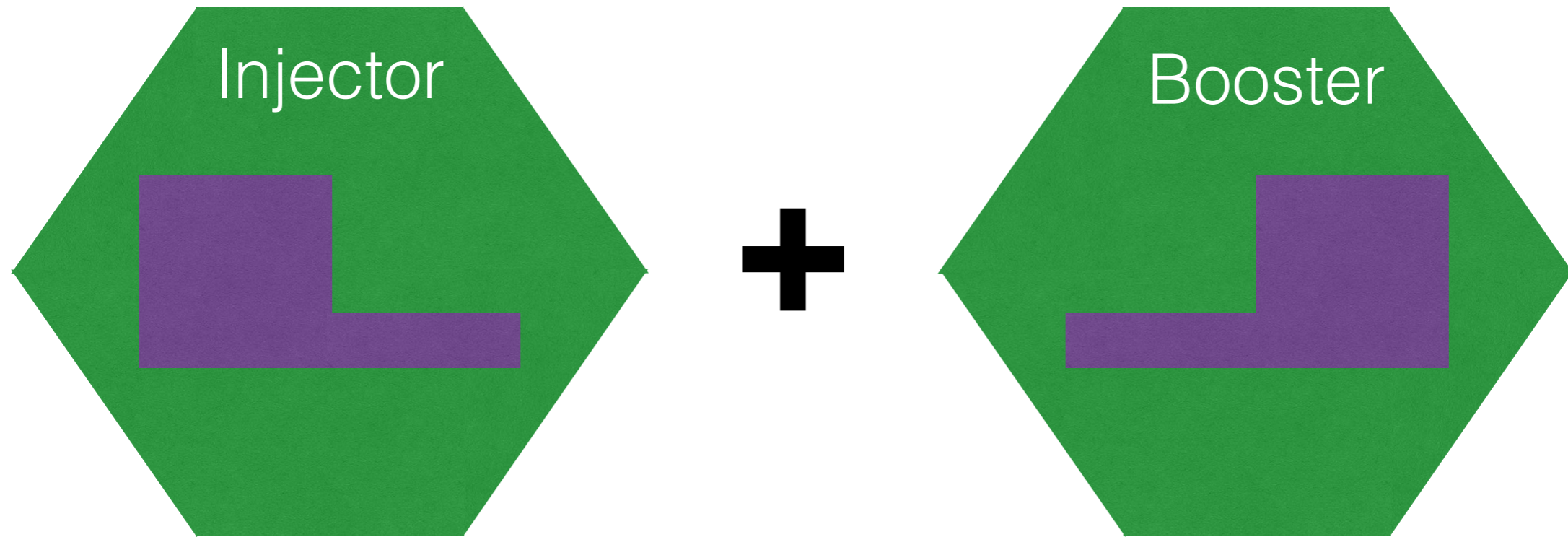
Angularly integrated spectra



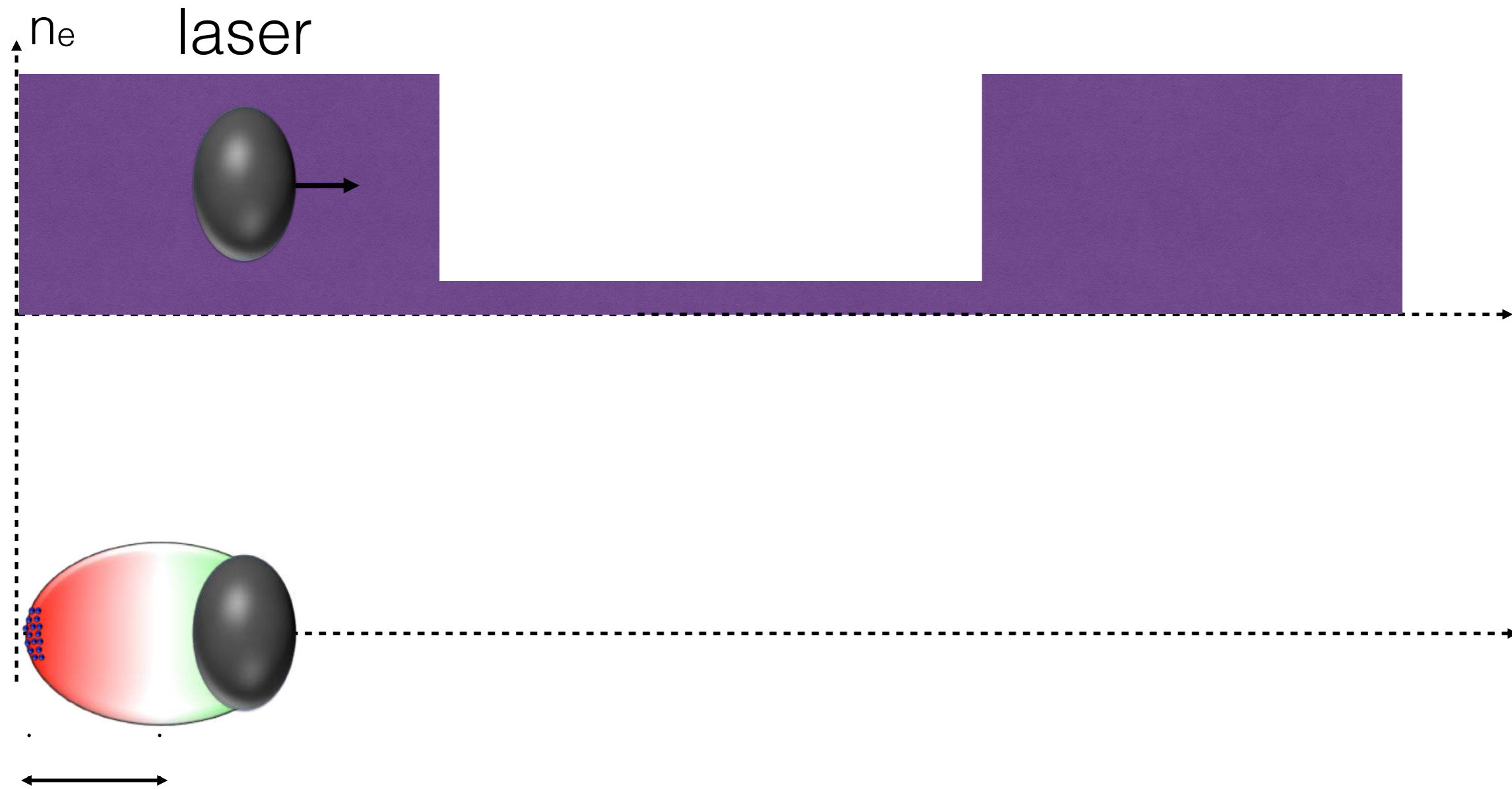
Calder-Circ PIC Simulations



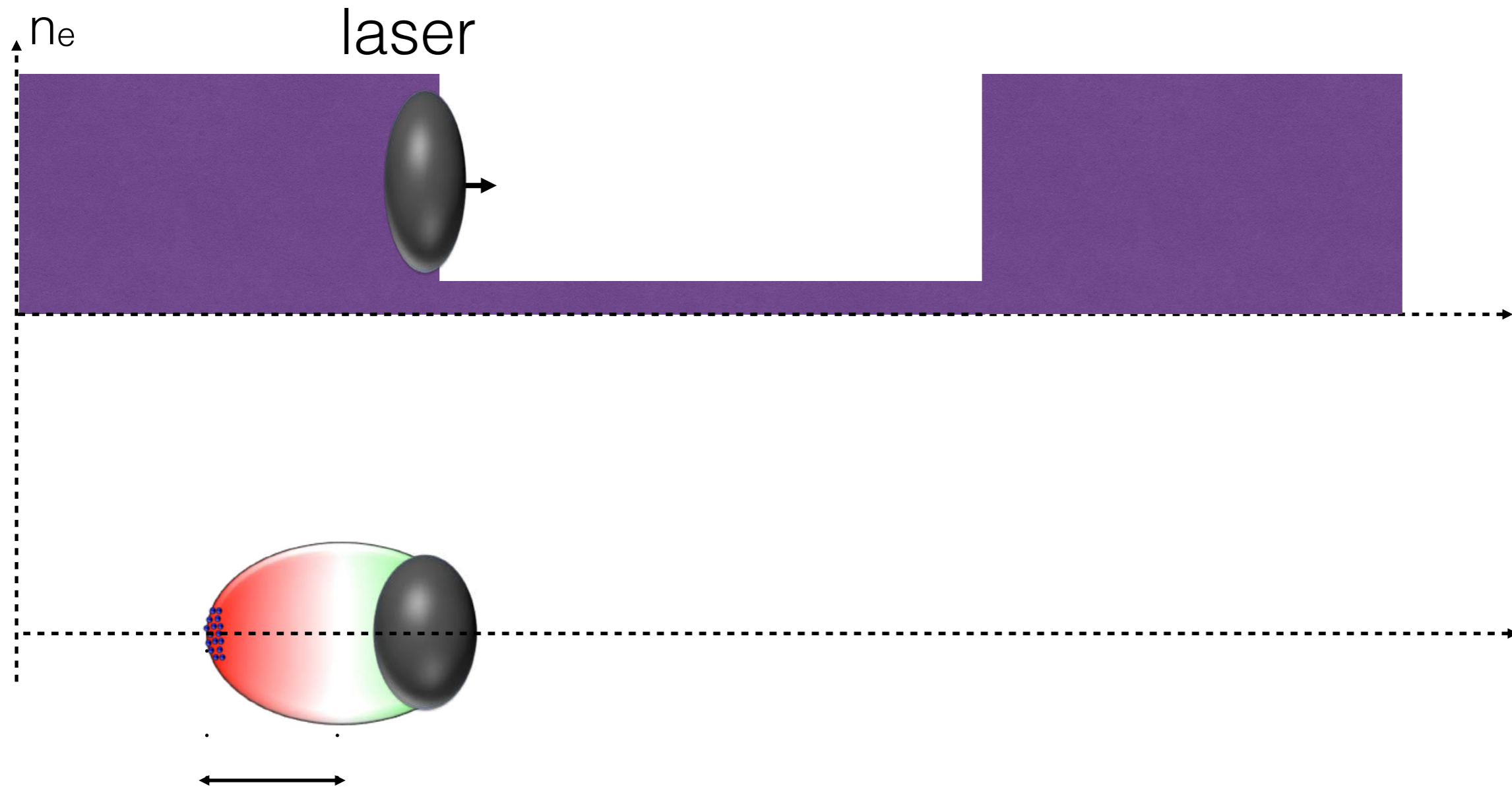
Combining Injector and Booster



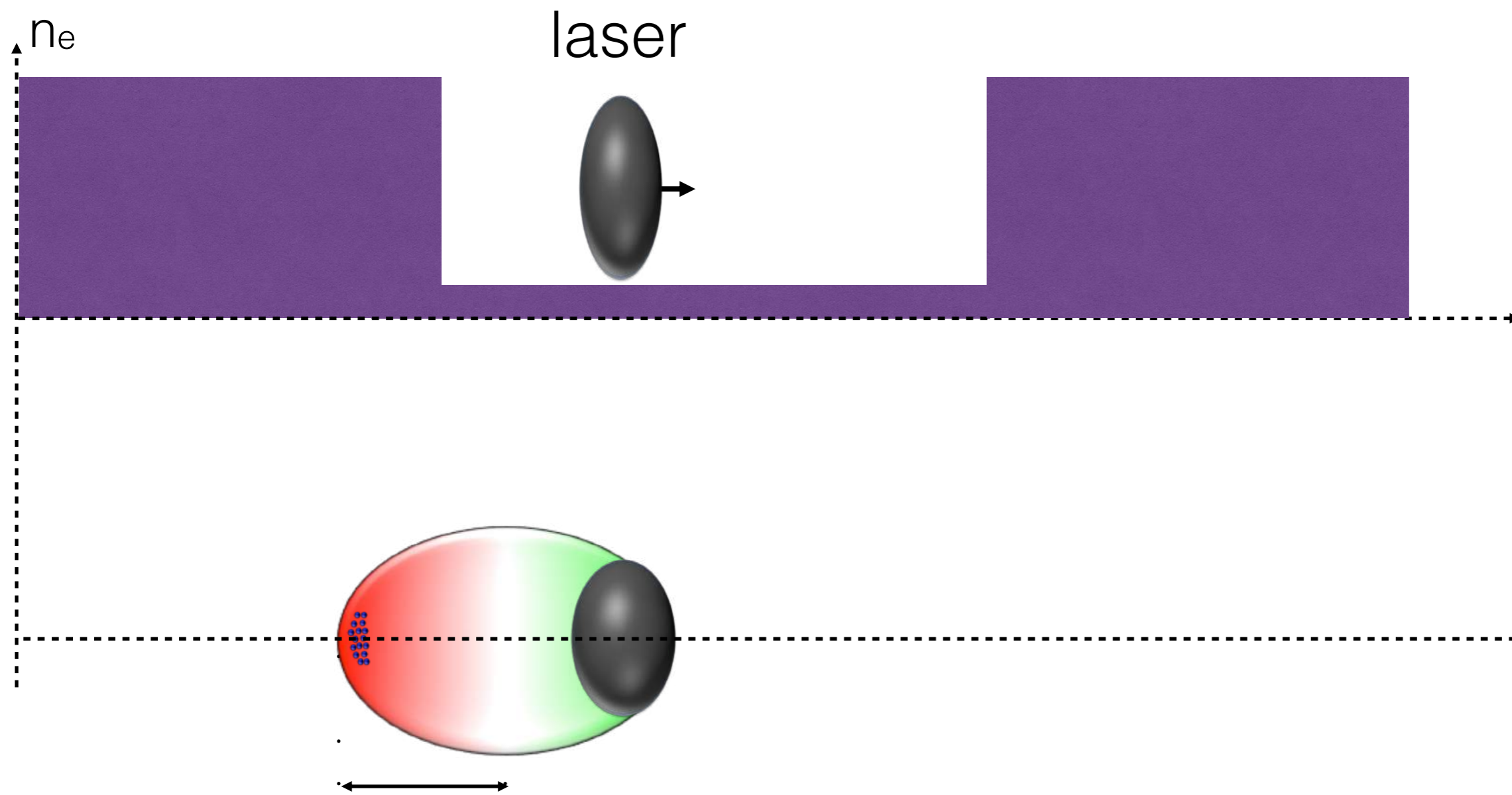
Combining Injector and Booster



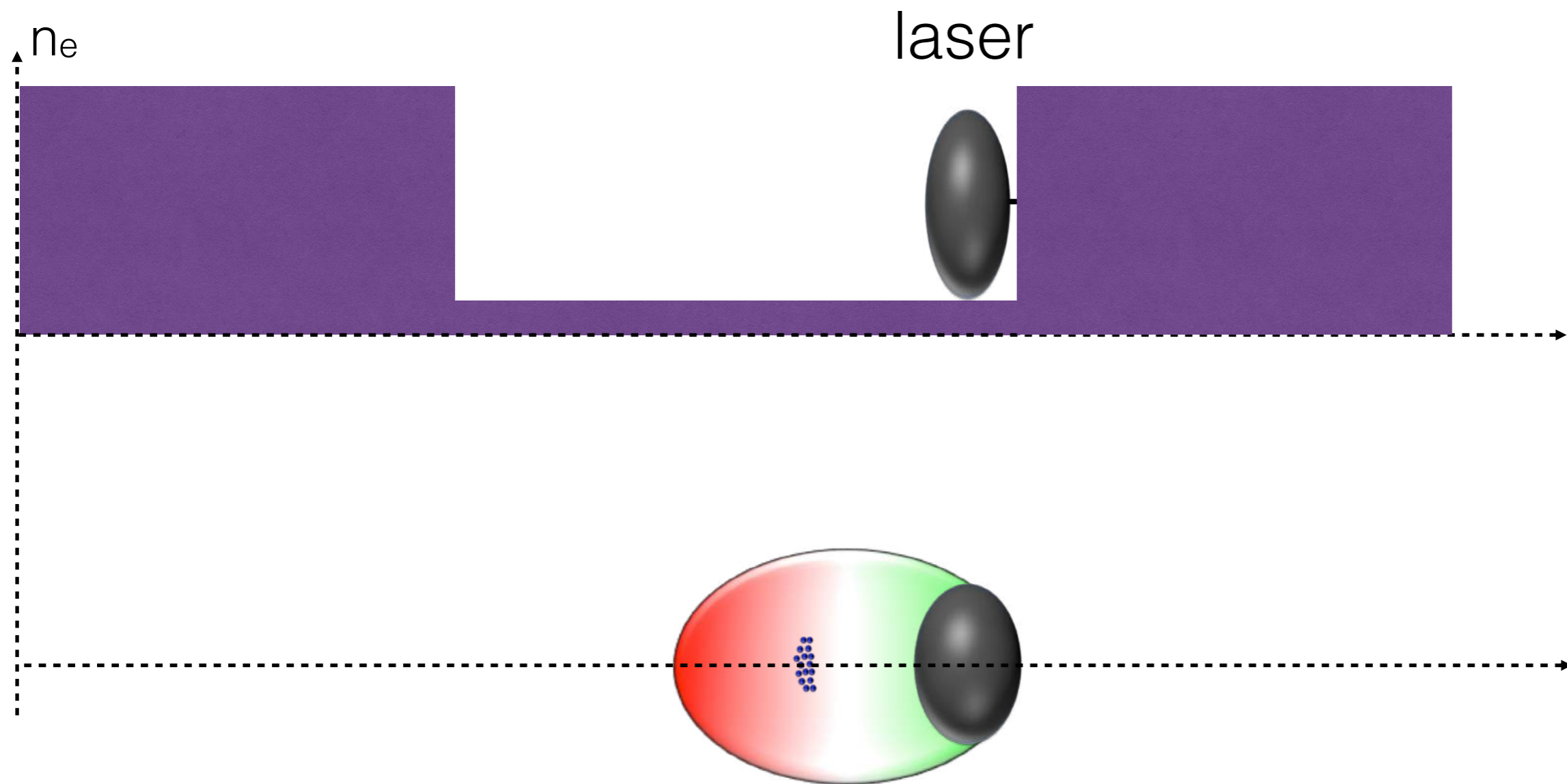
Combining Injector and Booster



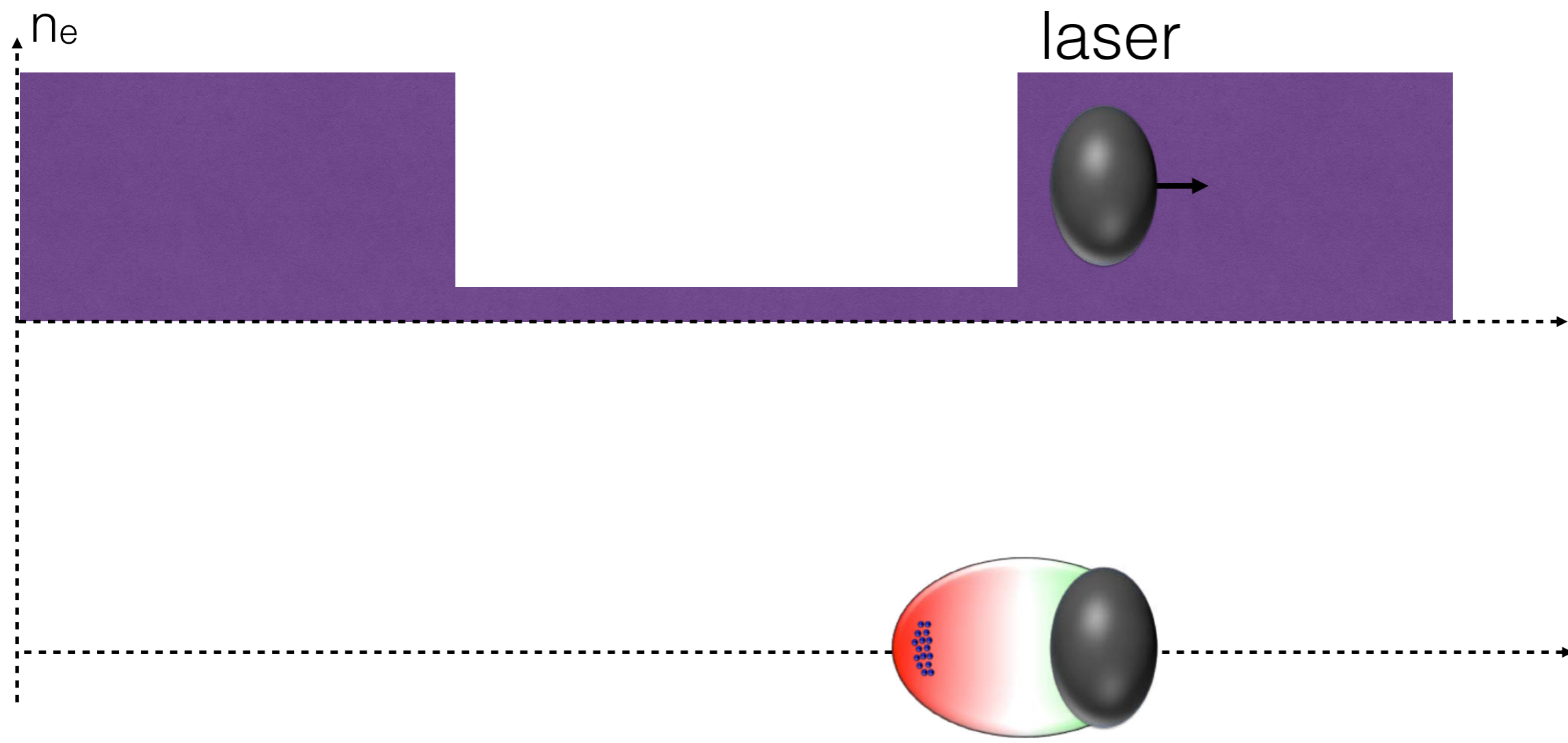
Combining Injector and Booster



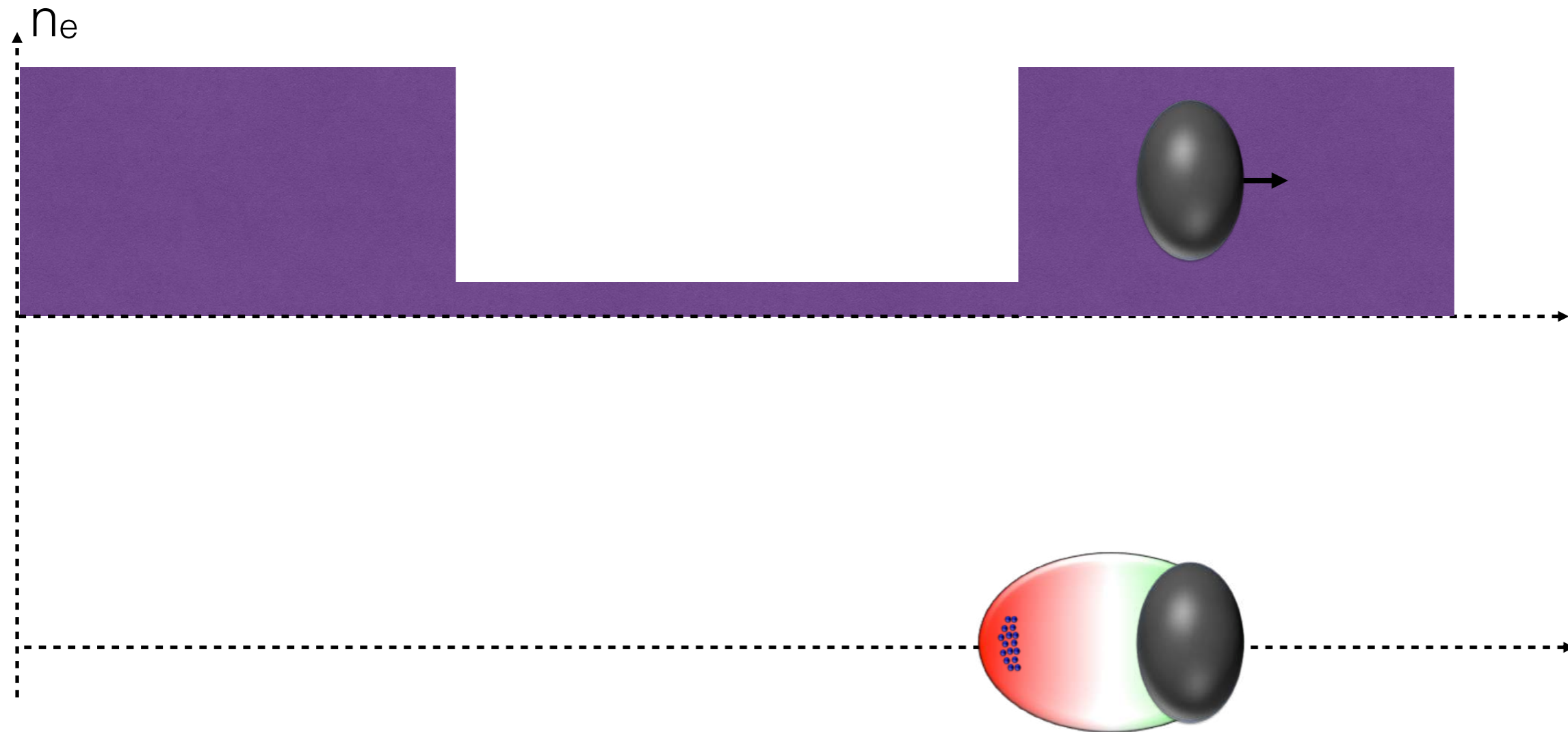
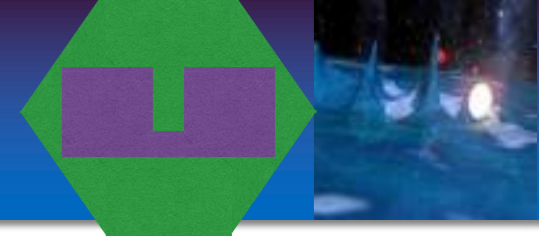
Combining Injector and Booster



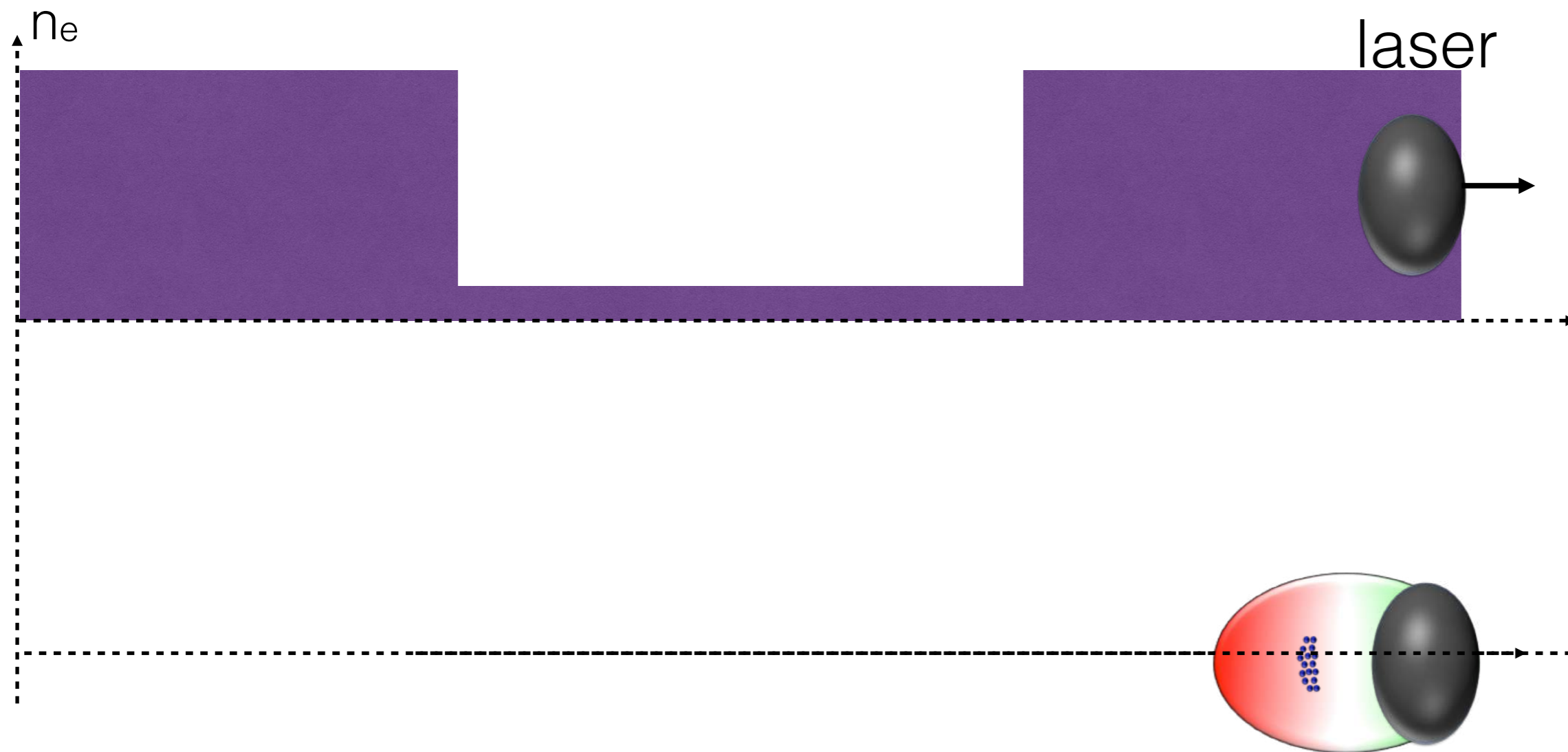
Combining Injector and Booster



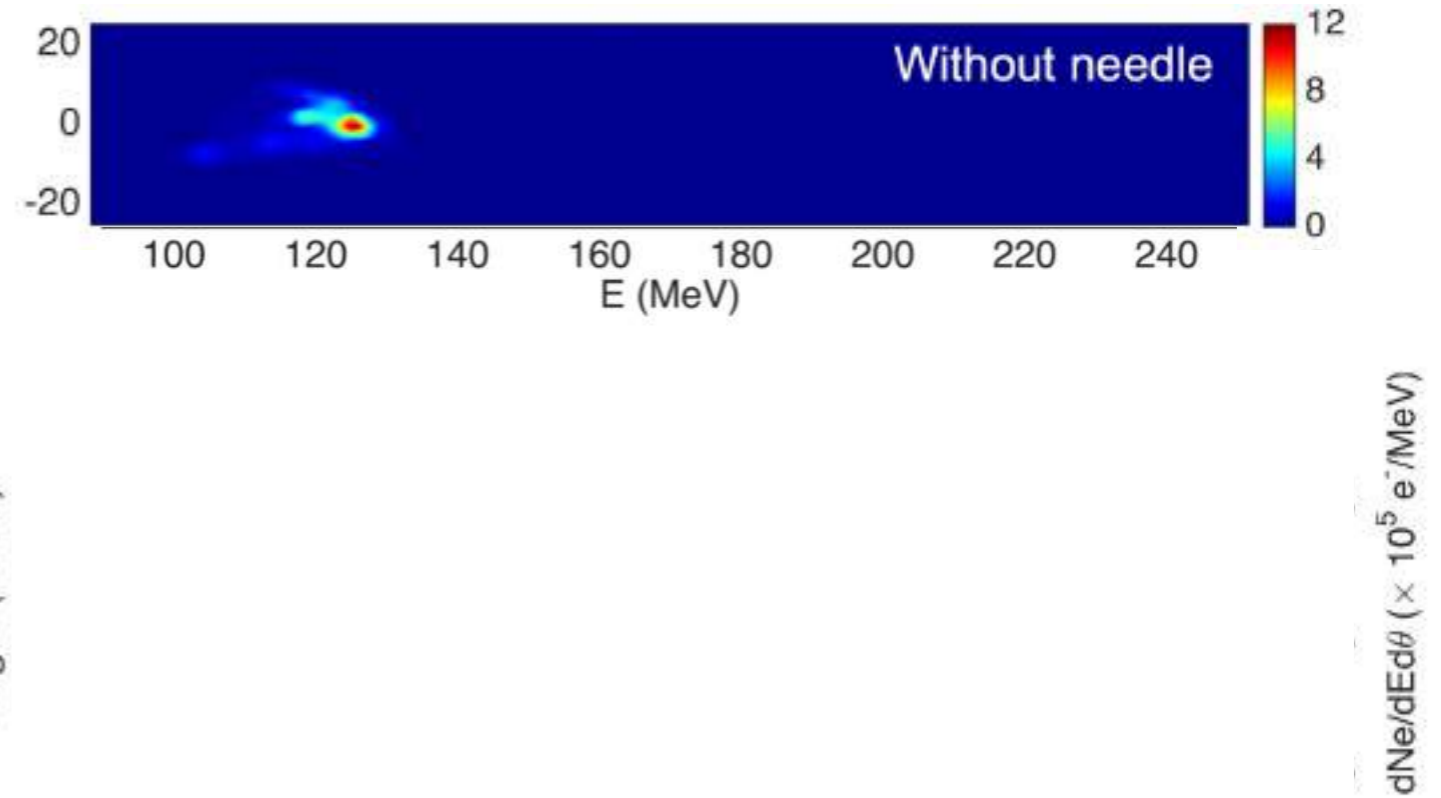
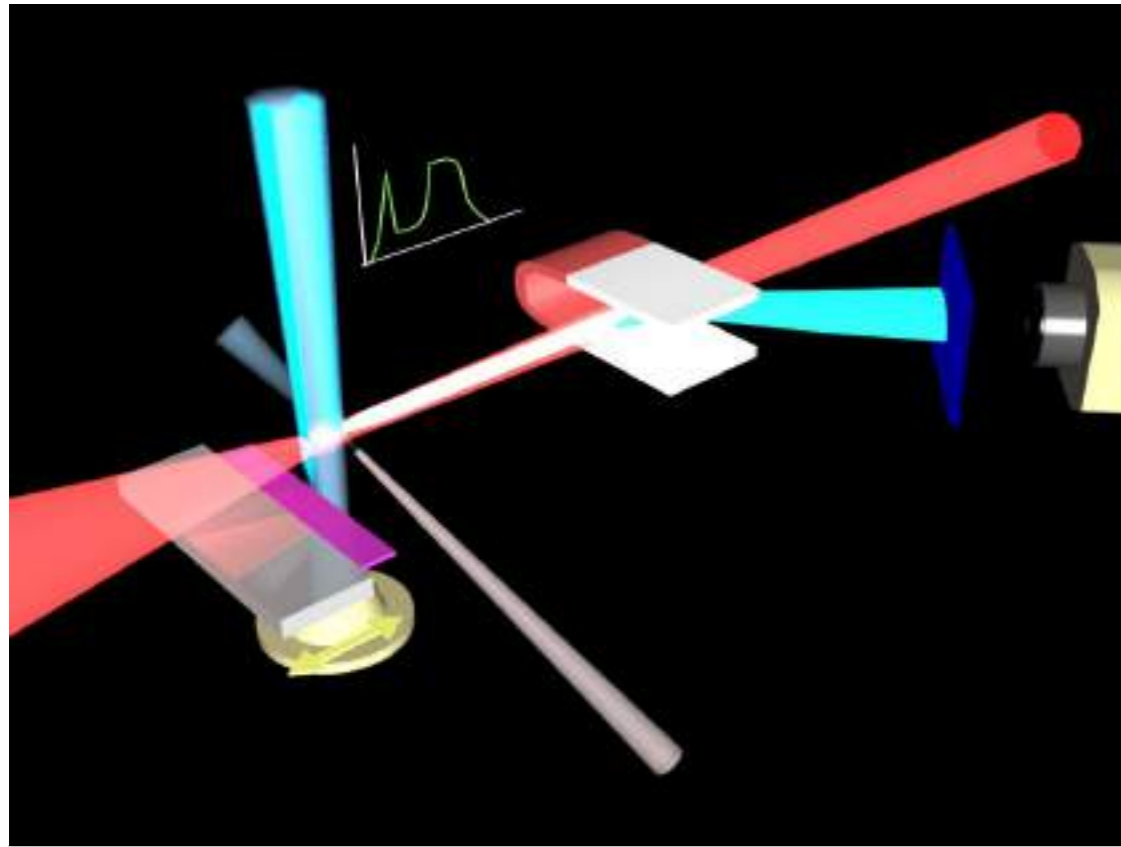
Combining Injector and Booster



Combining Injector and Booster



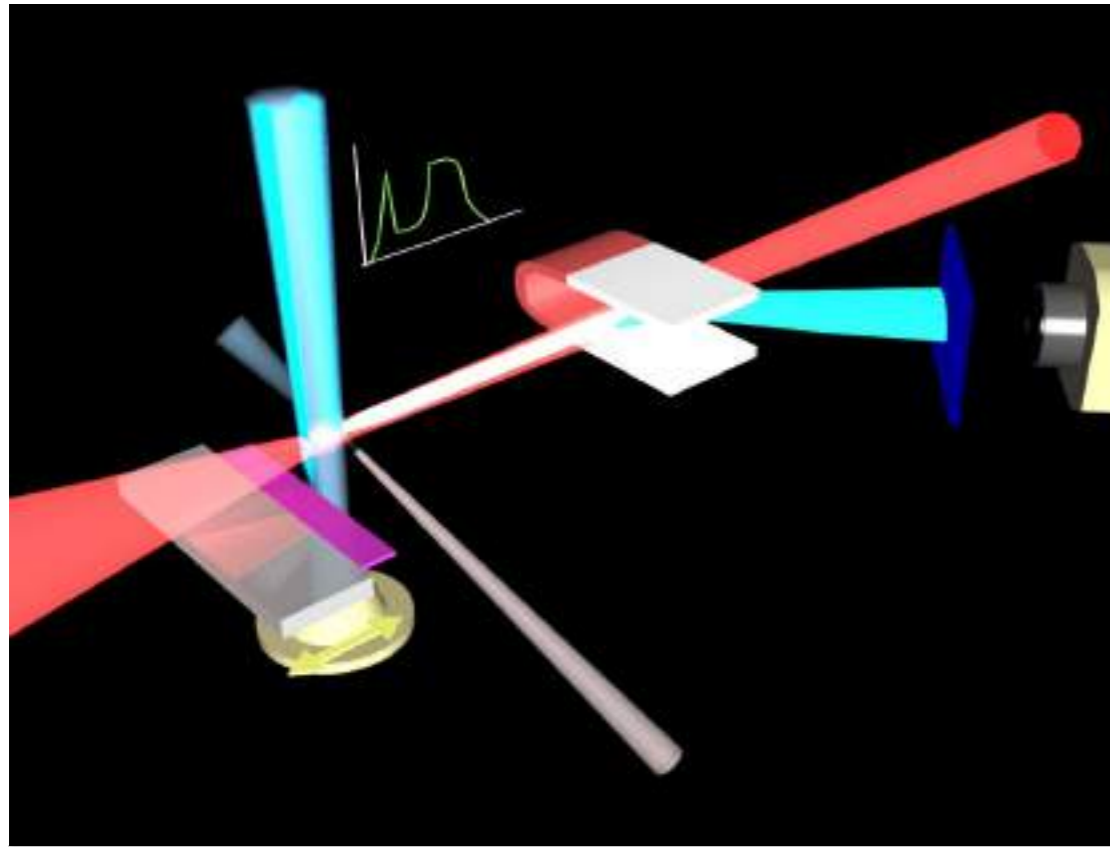
Energy boost of a mono-energetic e-beam



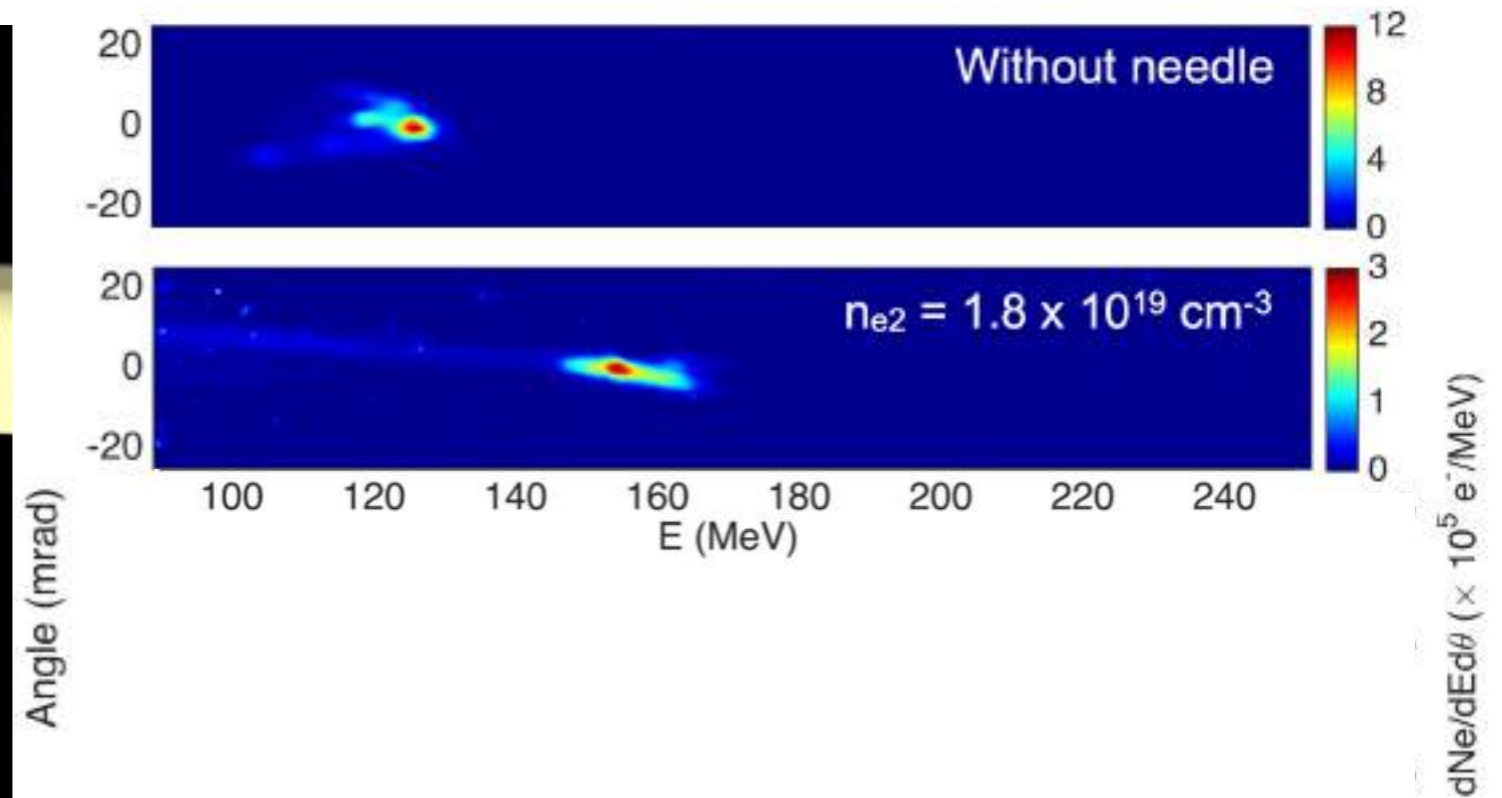
boosting a monoenergetic
electron beam

E. Guillaume et al., PRL **115** (2015)

Energy boost of a mono-energetic e-beam

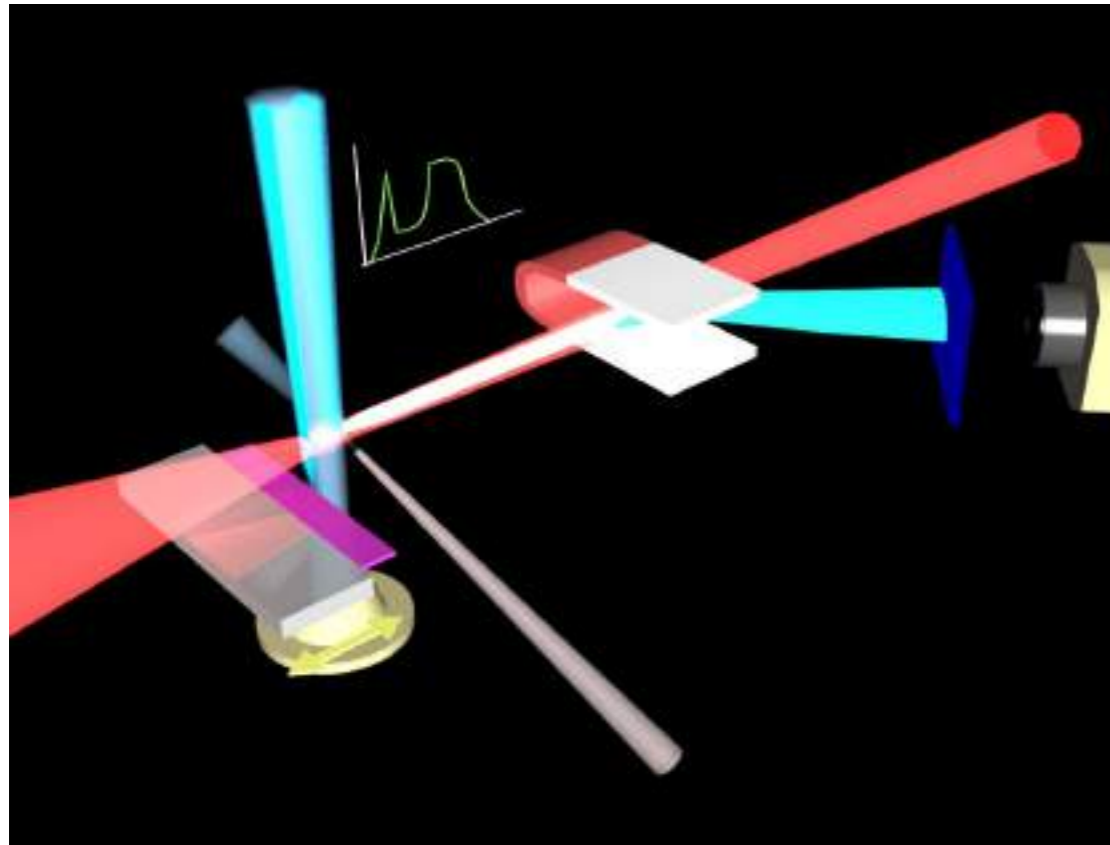


boosting a monoenergetic
electron beam

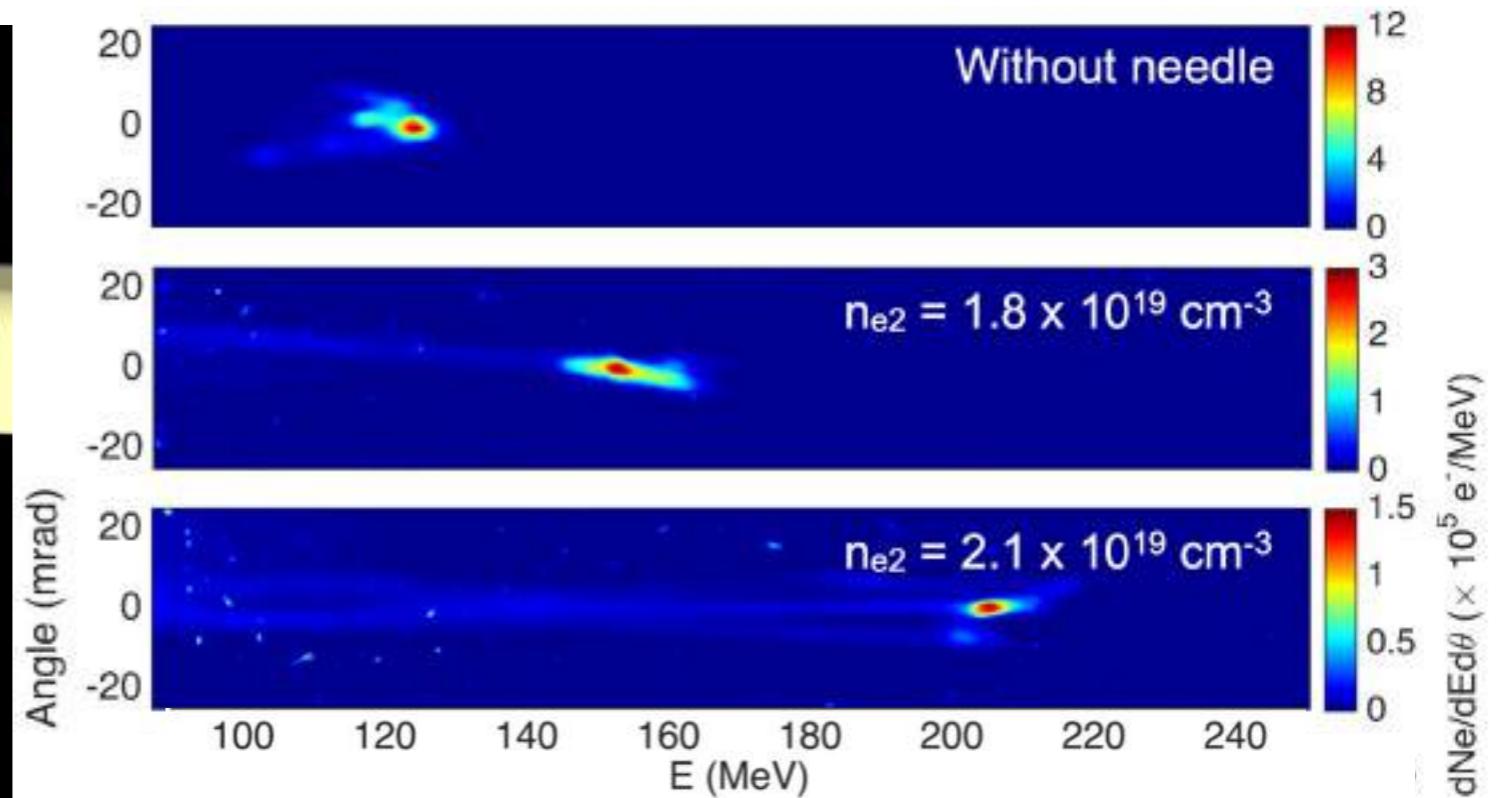


E. Guillaume et al., PRL **115** (2015)

Energy boost of a mono-energetic e-beam

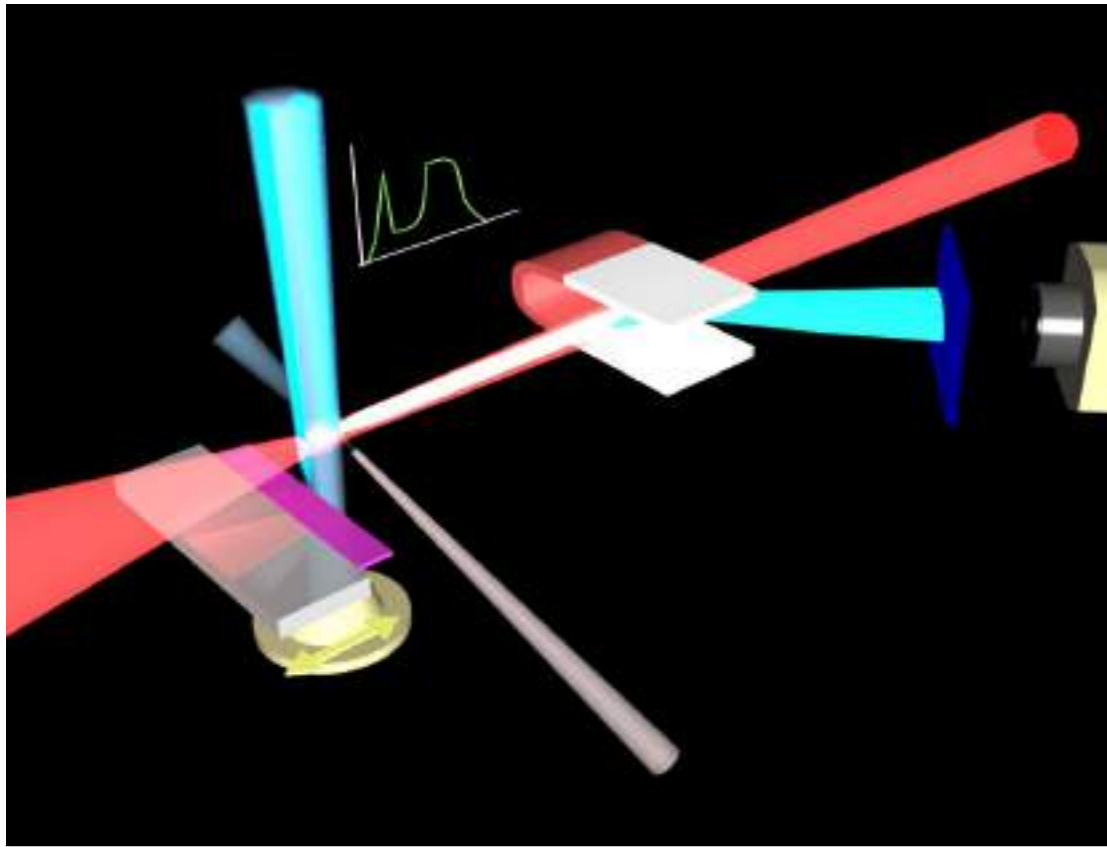


boosting a monoenergetic
electron beam

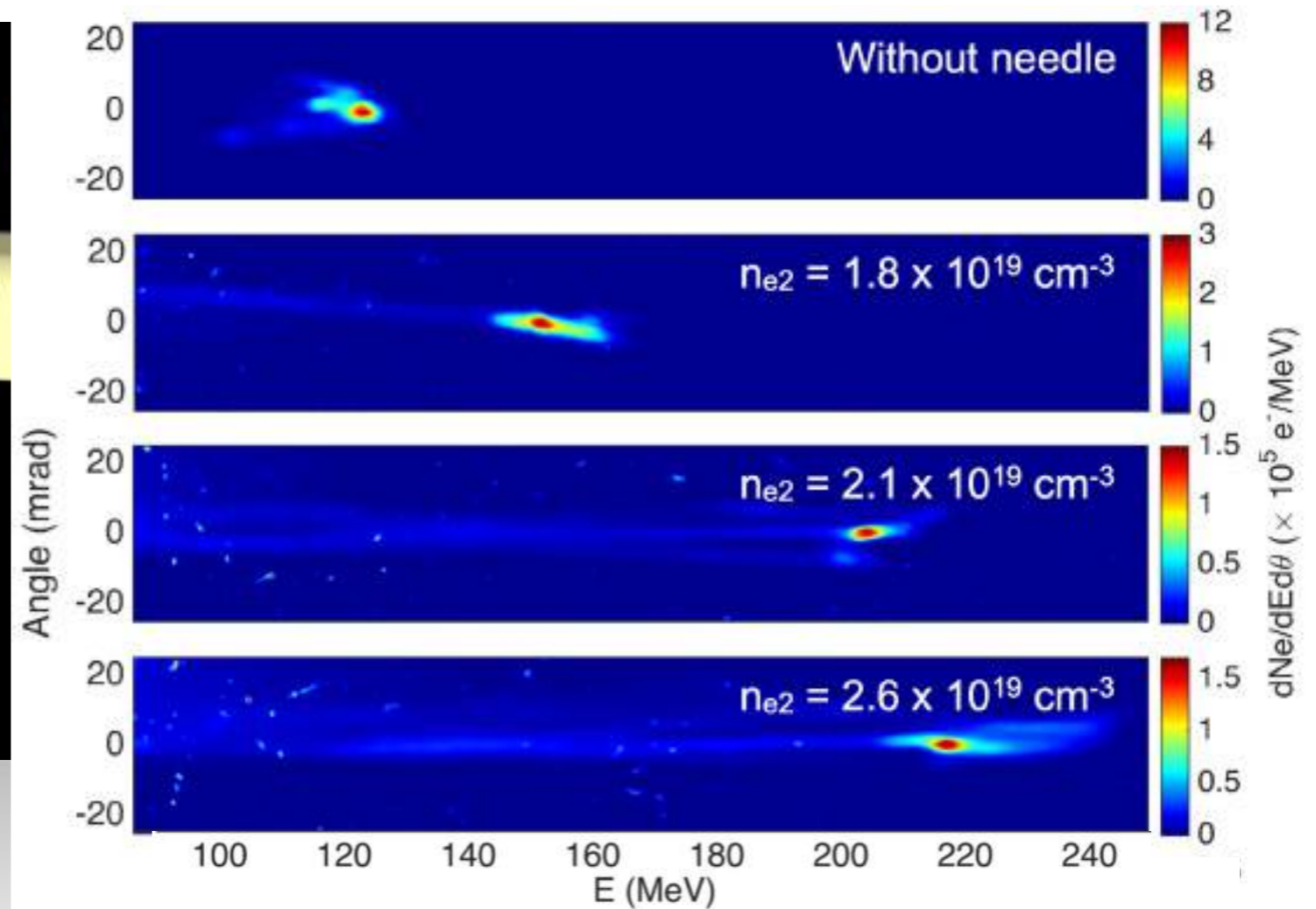


E. Guillaume et al., PRL **115** (2015)

Energy boost of a mono-energetic e-beam

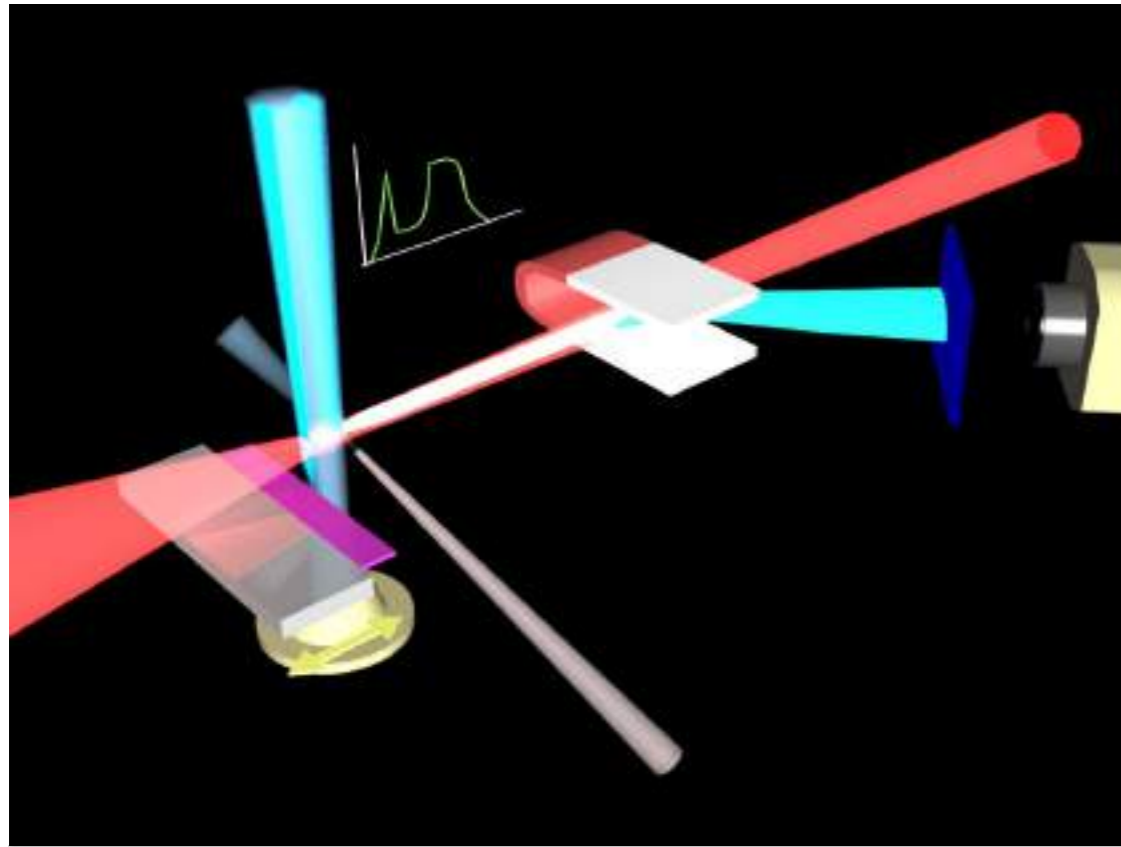


boosting a monoenergetic
electron beam

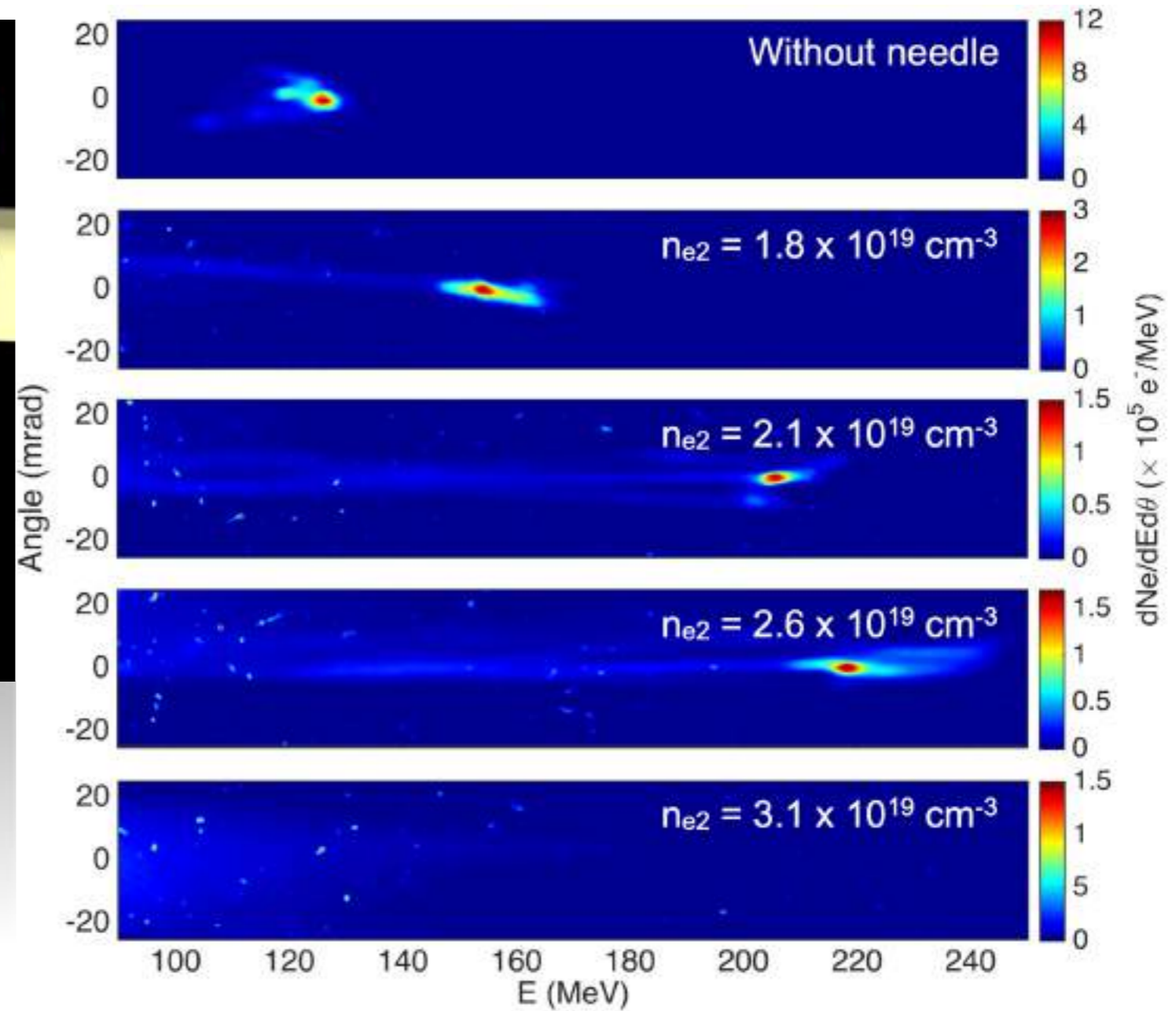


E. Guillaume et al., PRL **115** (2015)

Energy boost of a mono-energetic e-beam



boosting a monoenergetic
electron beam

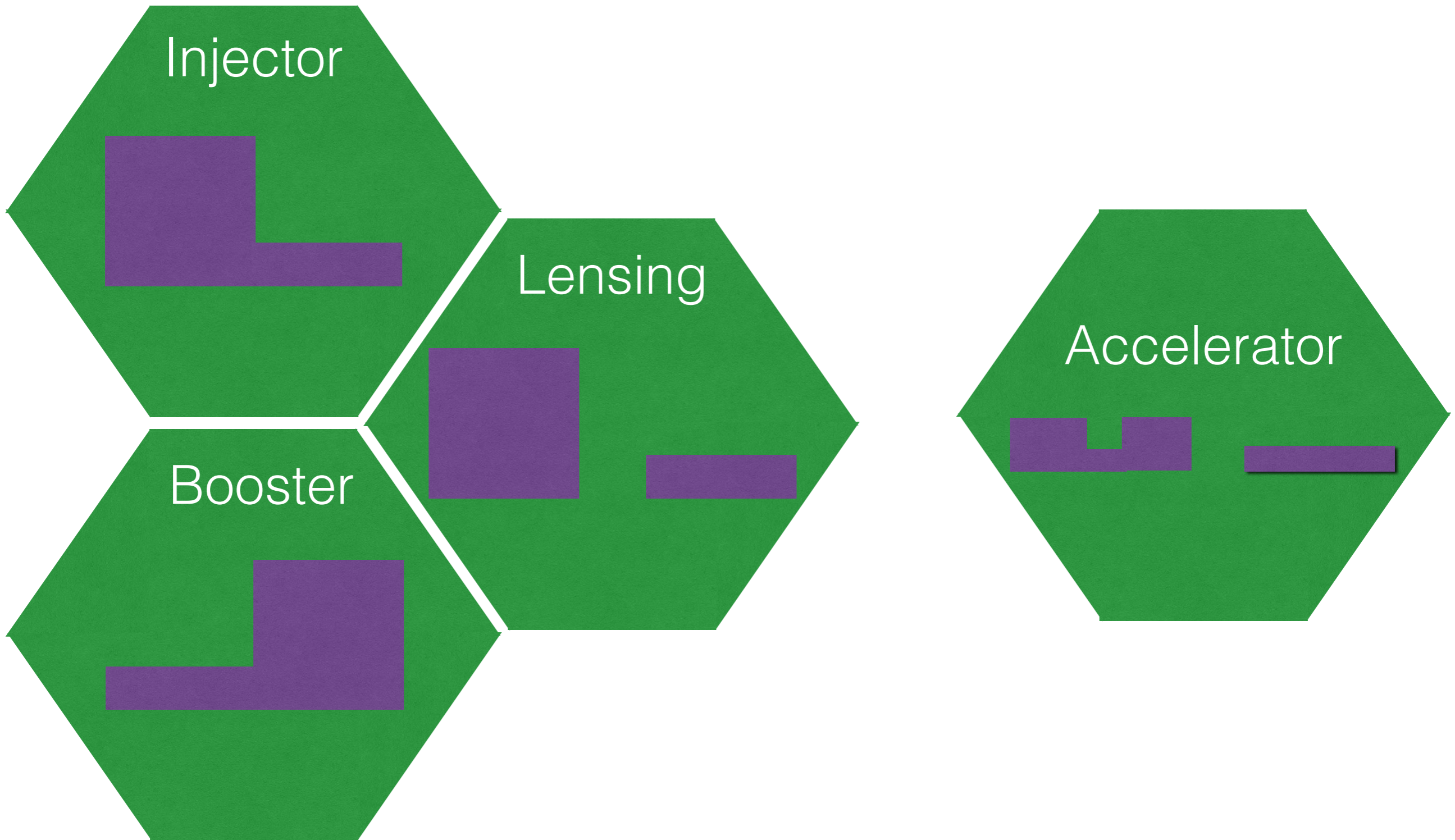


E. Guillaume et al., PRL **115** (2015)

Laser Plasma Accelerators : Outline

- Introduction : context and motivations
- Injection in a density gradient
- Manipulating the longitudinal momentum
- Manipulating the transverse momentum
- Conclusion and perspectives

Simple plasma devices produced with a single laser pulse



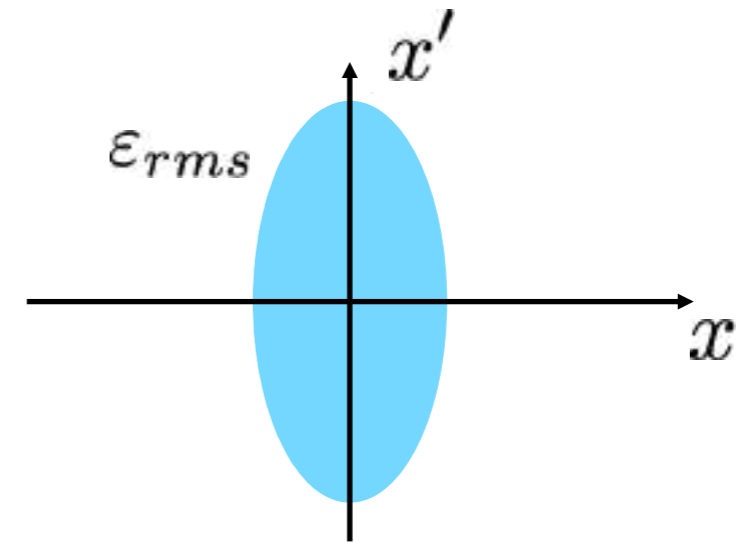
Manipulating the p_{\perp} momentum : emittance definition



electrons beam emittance :

$$\epsilon_{rms} = \sqrt{\underbrace{\langle x^2 \rangle}_{\text{transverse size}} \underbrace{\langle x'^2 \rangle}_{\text{beam divergence}} - \langle xx' \rangle^2}$$

transverse size
beam divergence



typical transverse size of the e-beam **< 1 μm**

typical divergence of the e-beam : **~ 4 mrad**

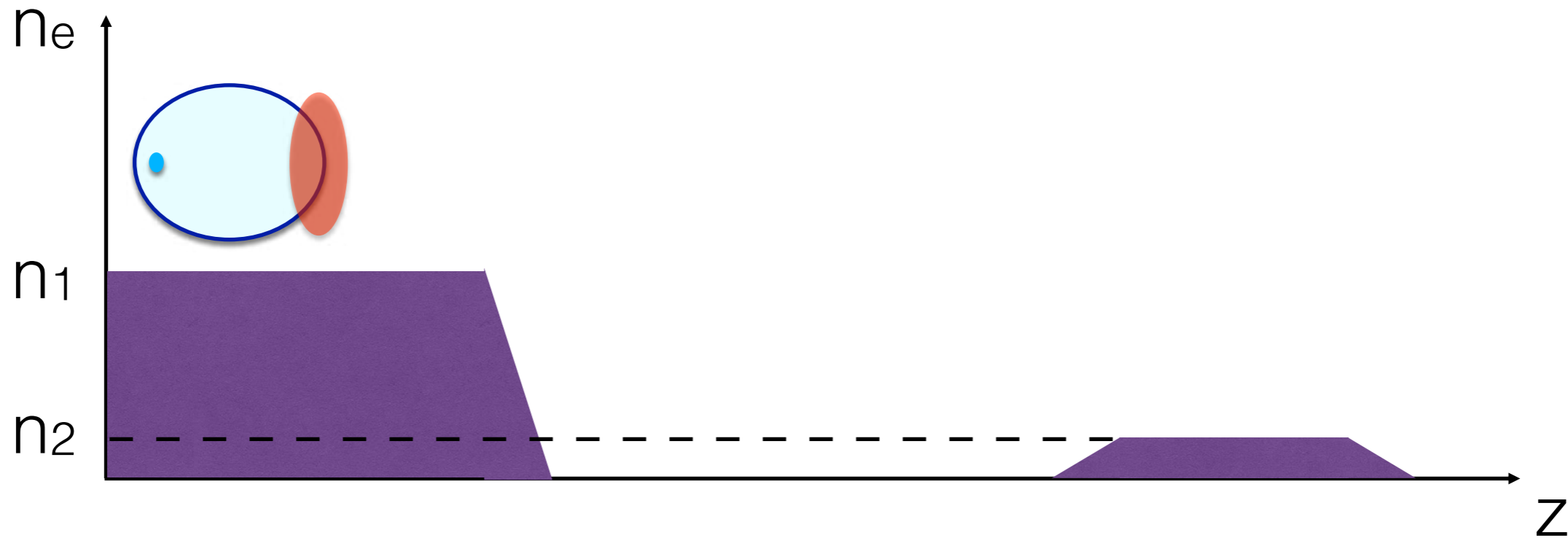
} emittance is dominated by the divergence

→ too large for example for some applications (FEL, ...)

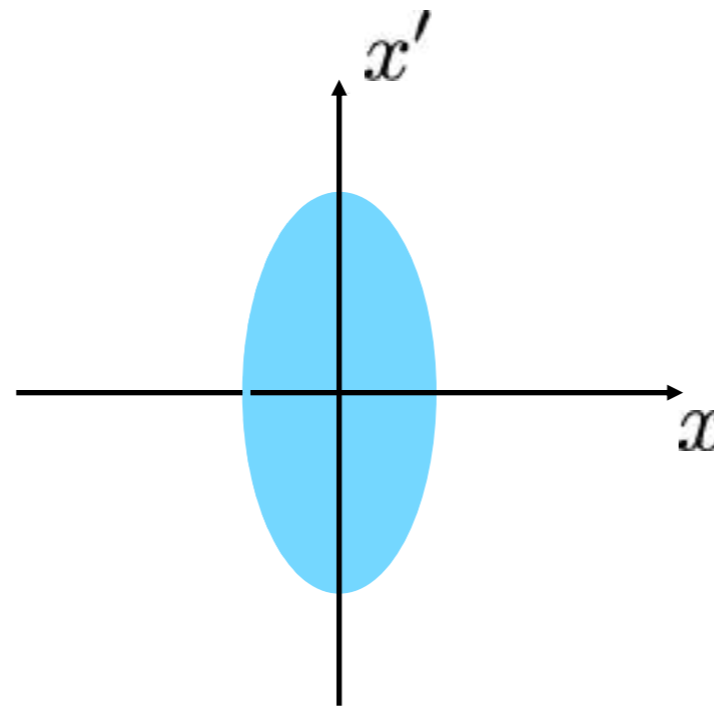
Goal :

reduce the divergence of the beam by manipulating the transverse phase space

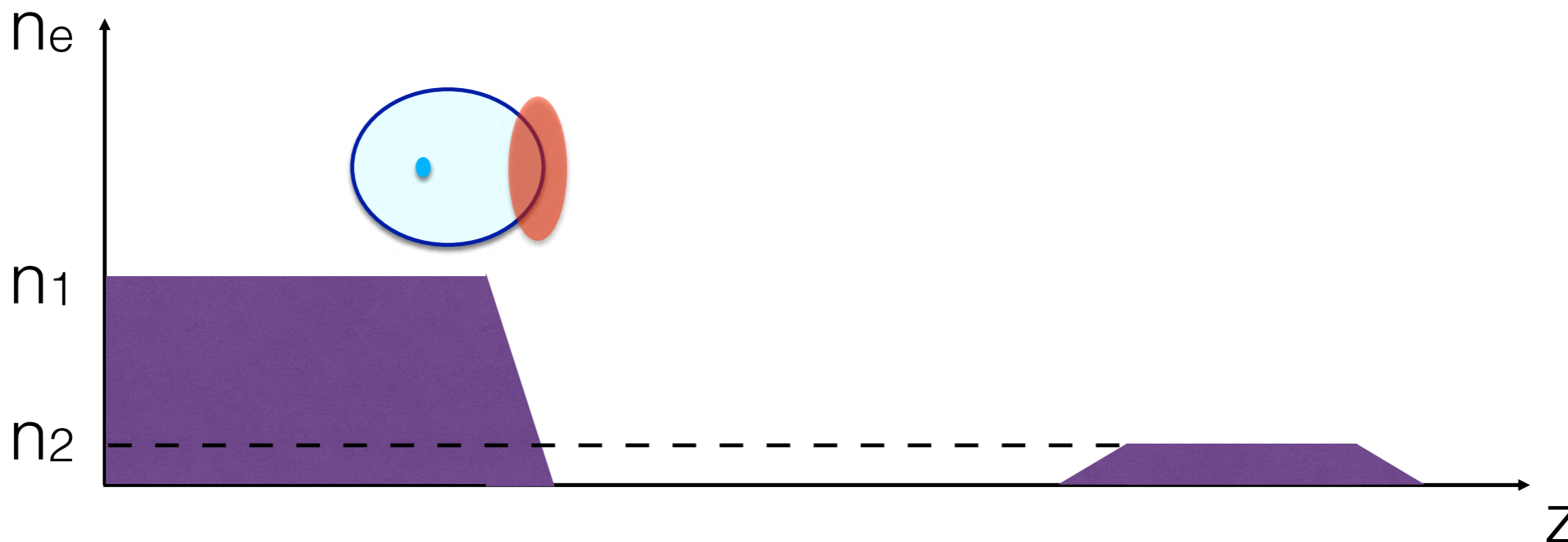
Manipulating the p_{\perp} momentum : principle



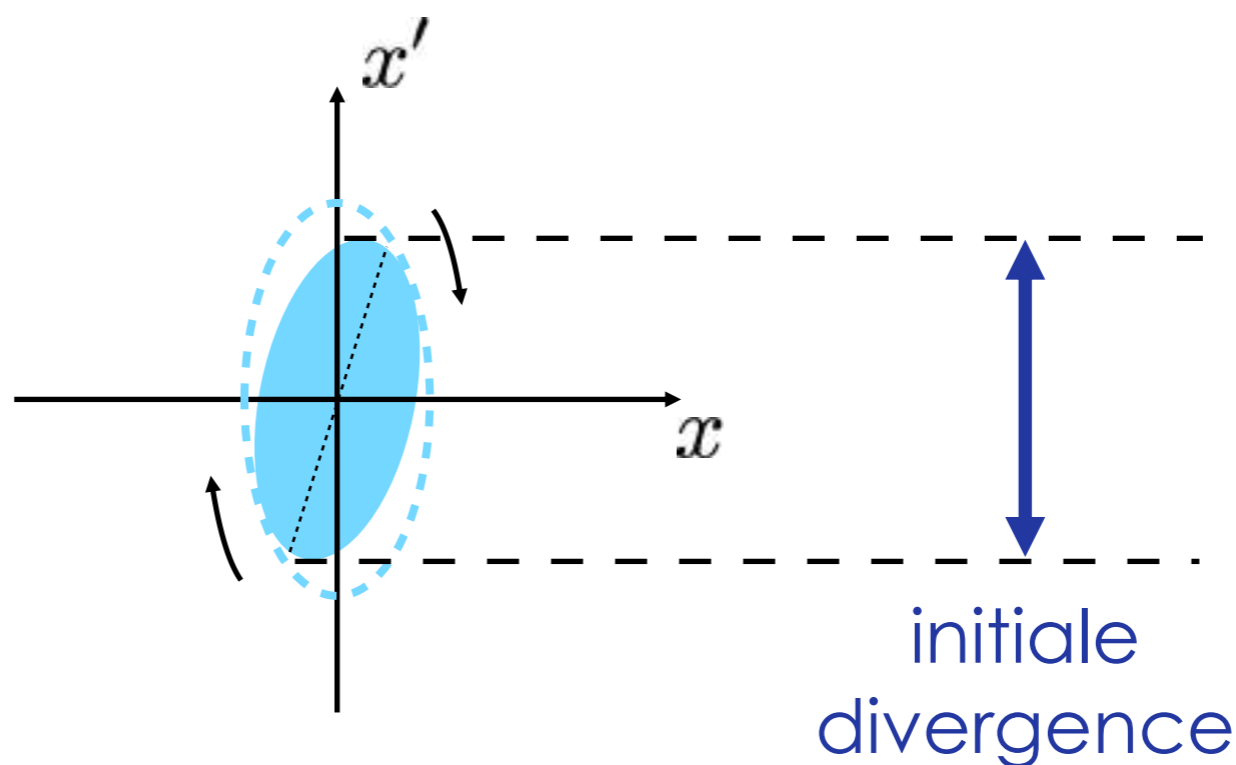
Acceleration &
betatron oscillation



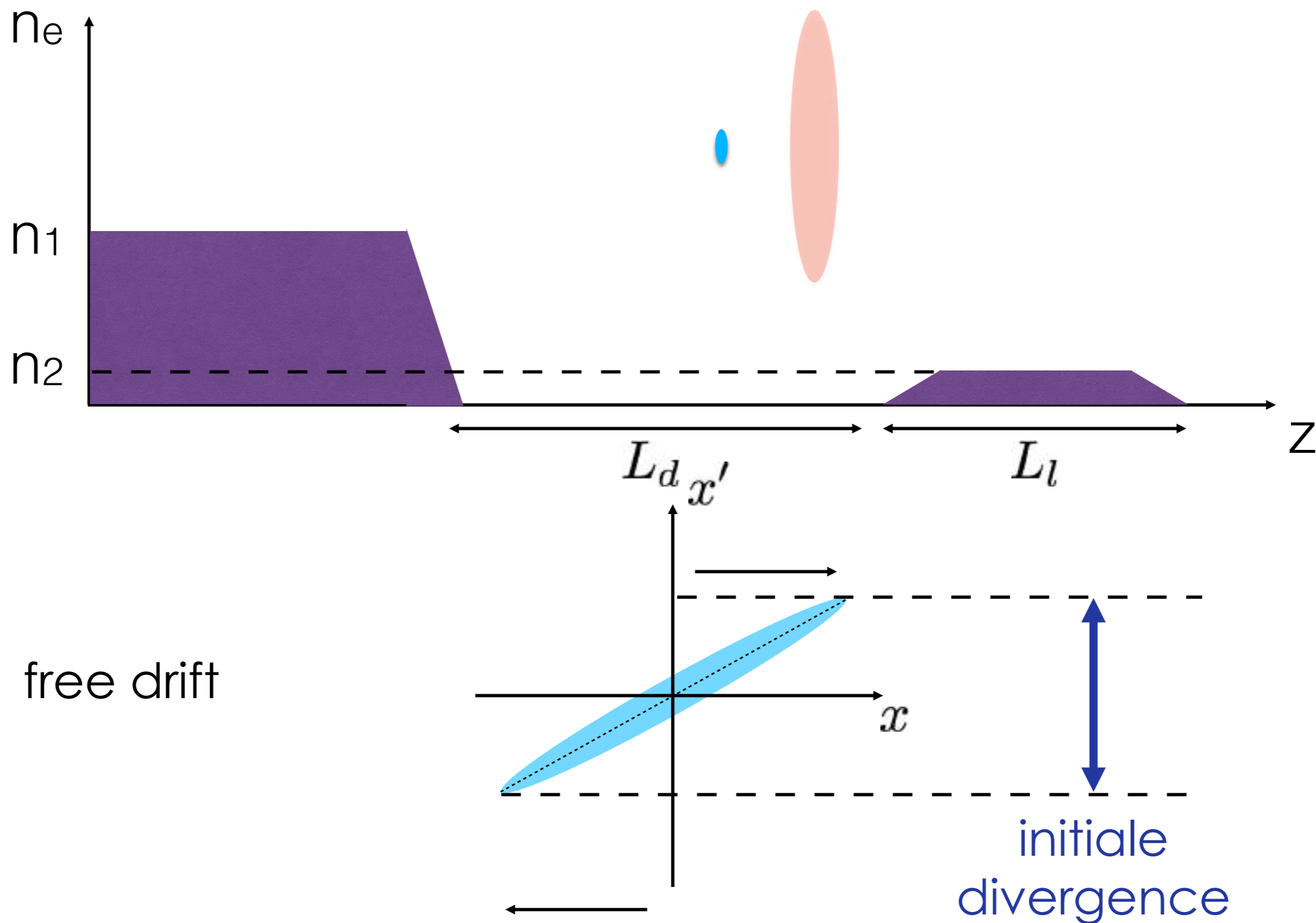
Manipulating the p_{\perp} momentum : principle



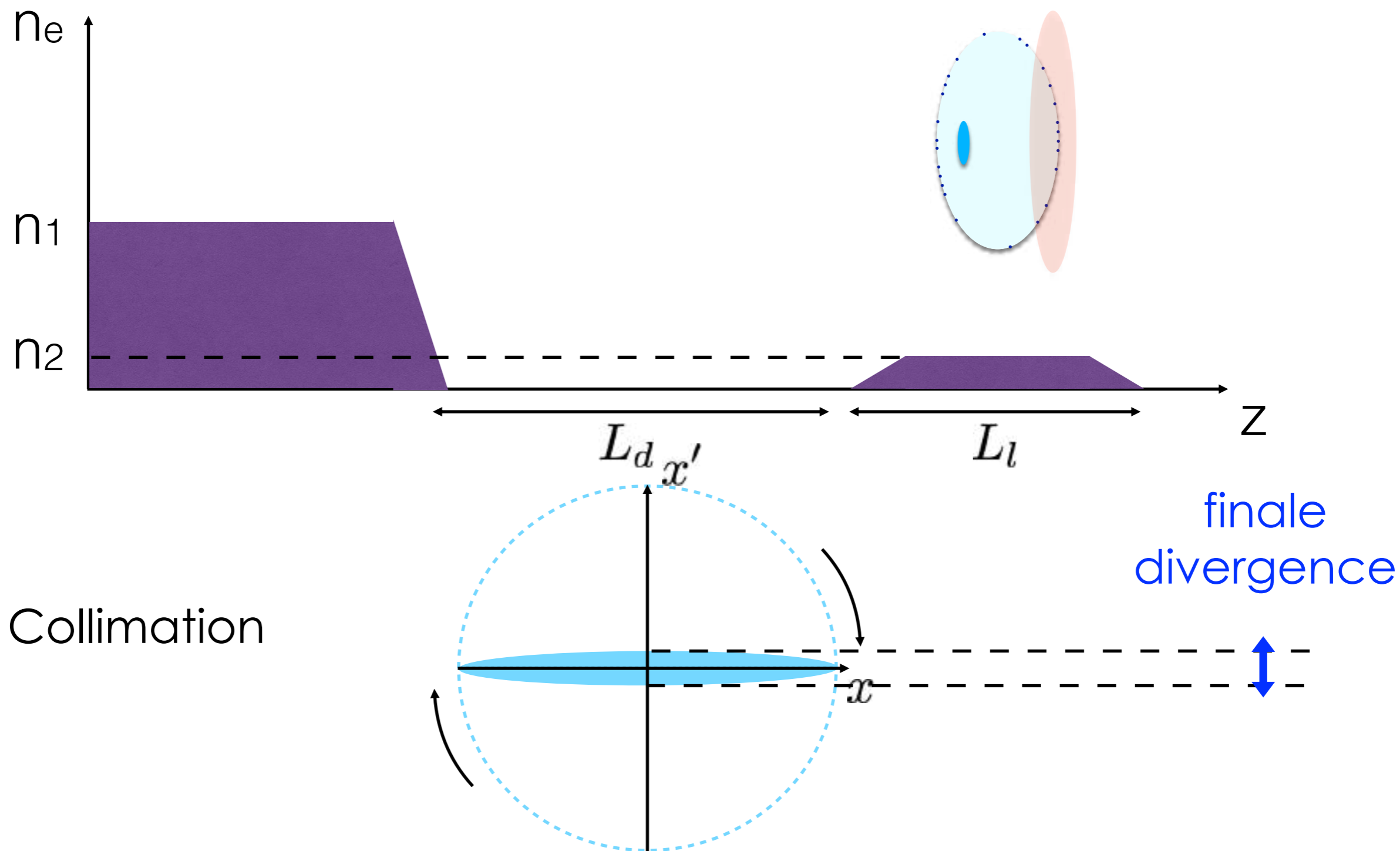
Acceleration & betatron oscillation



Manipulating the p_{\perp} momentum : principle



Manipulating the p_{\perp} momentum : principle



Manipulating the p_{\perp} momentum : experimental set-up

Acceleration stage

Laser beam:

0.9 J, 28 fs, 12 microns FWHM

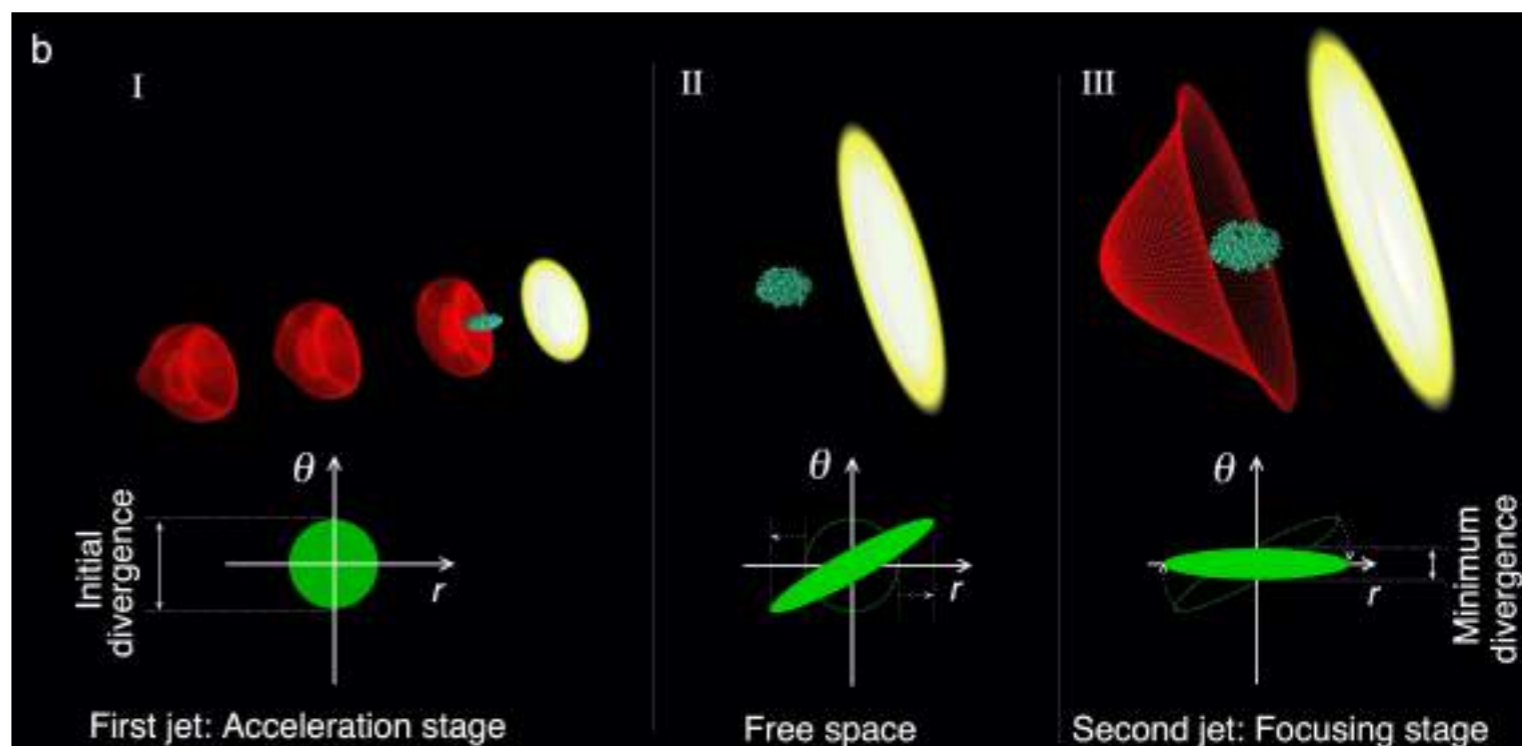
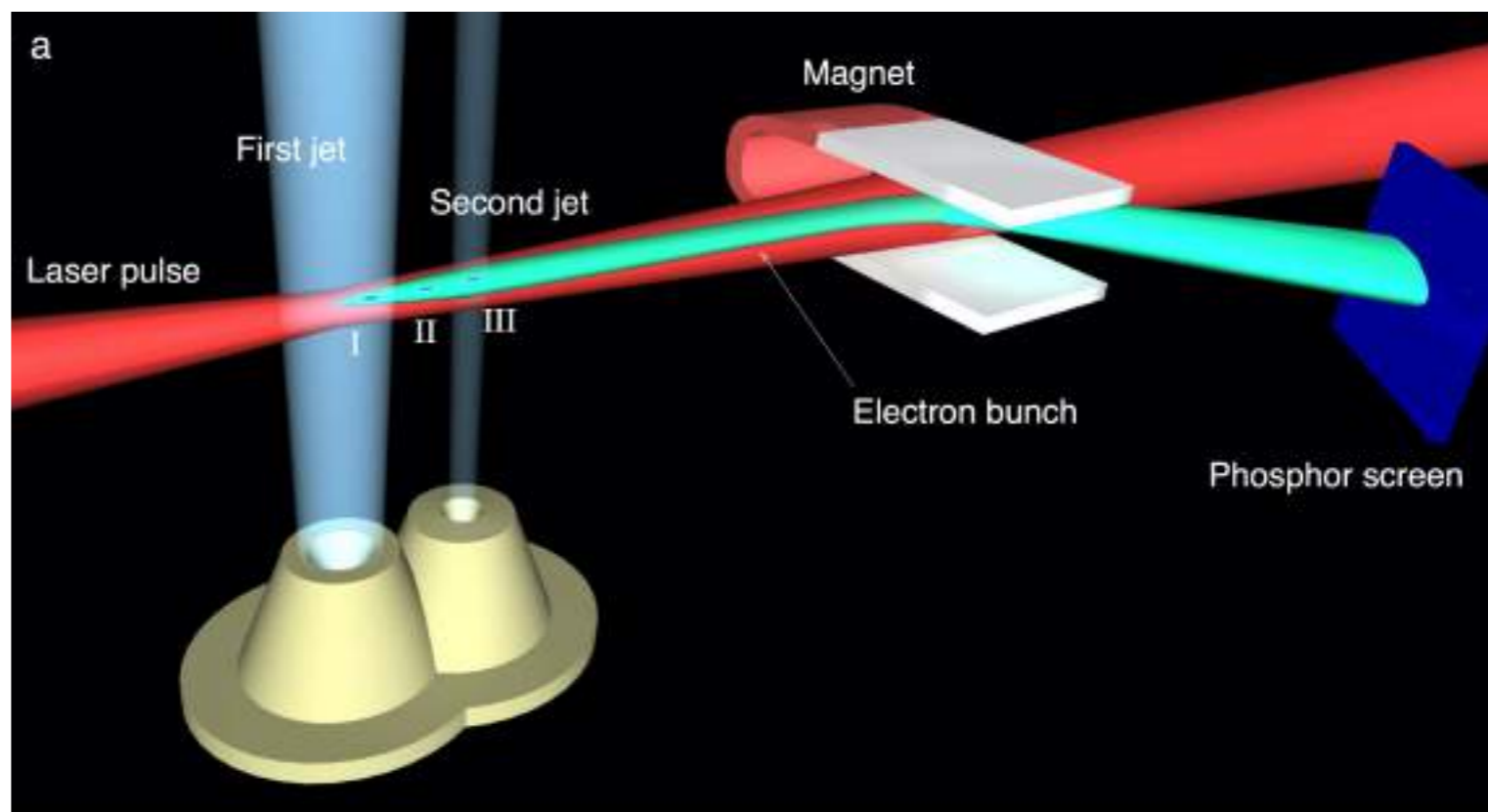
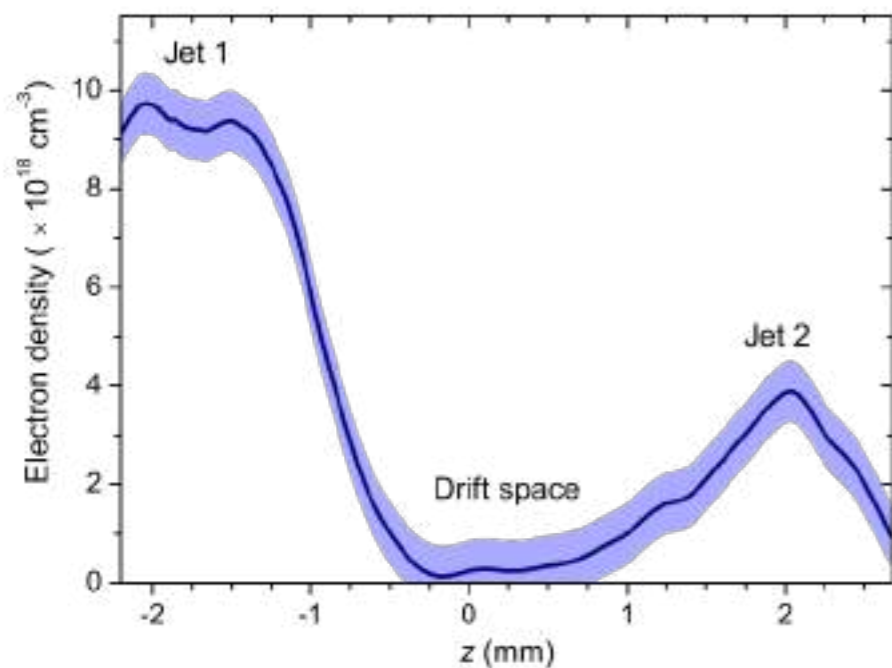
Focused with a 1 m OAP at the
entrance of a 3 mm gas jet

$n_1 = 9.2 \times 10^{18} \text{ cm}^{-3}$

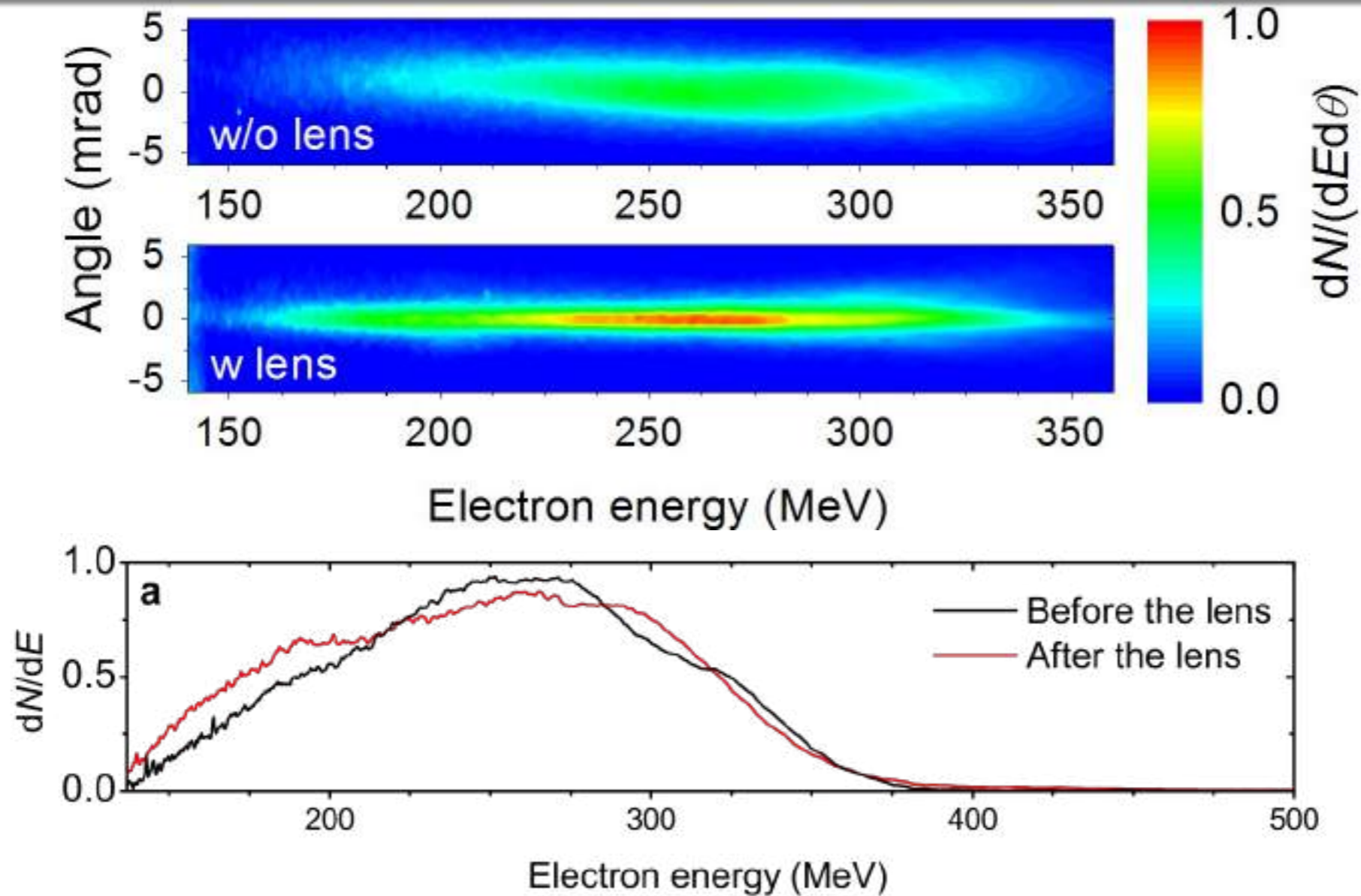
Focusing stage

1 mm nozzle with variable n_2

Variable L_d



Manipulating the p_{\perp} momentum : demonstration of the laser plasma lens



Focusing stage parameters :

$$L_d = 1.8 \text{ mm}$$

$$n_2 = 3.9 \times 10^{18} \text{ cm}^{-3}$$

Divergence after the lens (FWHM)

$$\sigma_{\theta} = 1.6 \pm 0.2 \text{ mrad}$$

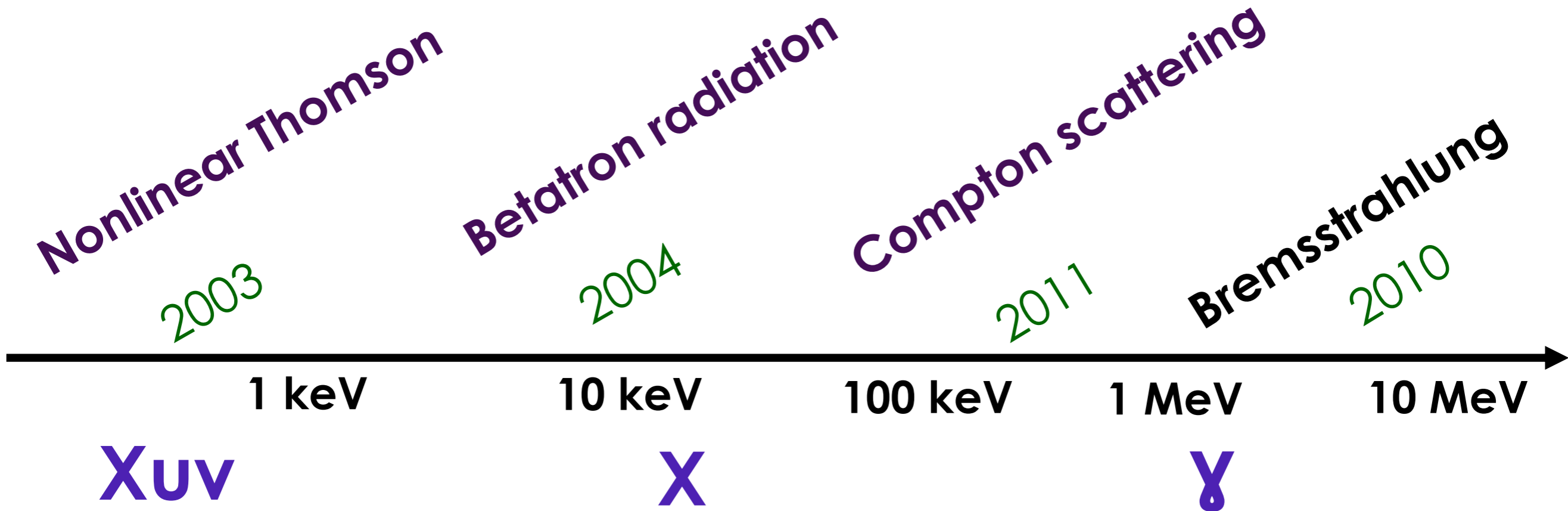
Divergence reduction $\sim 2.6 \pm 0.7$

C. Thaury *et al.*, Nature Comm. **6**, 6860 (2015)

Laser Plasma Accelerators : Outline

- Introduction : context and motivations
- Colliding laser pulses scheme
- Injection in a density gradient
- Manipulating the longitudinal momentum
- Manipulating the transverse momentum
- Applications
- Conclusion and perspectives

X rays source with Laser Plasma accelerators



Common features: Collimated beams (mrad)
Femtosecond duration (few fs)
Micron source size
High peak brightness ($>10^{20}$ ph/s/mm²/mrad²)

- naturally synchronized (ideal for pump-probe experiments)
- compacts and useful for small scale laboratories

Moving charge radiation



$$\frac{d^2 I}{d\omega d\Omega} = \frac{e^2}{4\pi^2 c} \left| \int_{-\infty}^{+\infty} e^{i\omega[t - \vec{n} \cdot \vec{r}(t)/c]} \frac{\vec{n} \times [(\vec{n} - \vec{\beta}) \times \dot{\vec{\beta}}]}{(1 - \vec{\beta} \cdot \vec{n})^2} dt \right|^2$$

Velocity
Acceleration

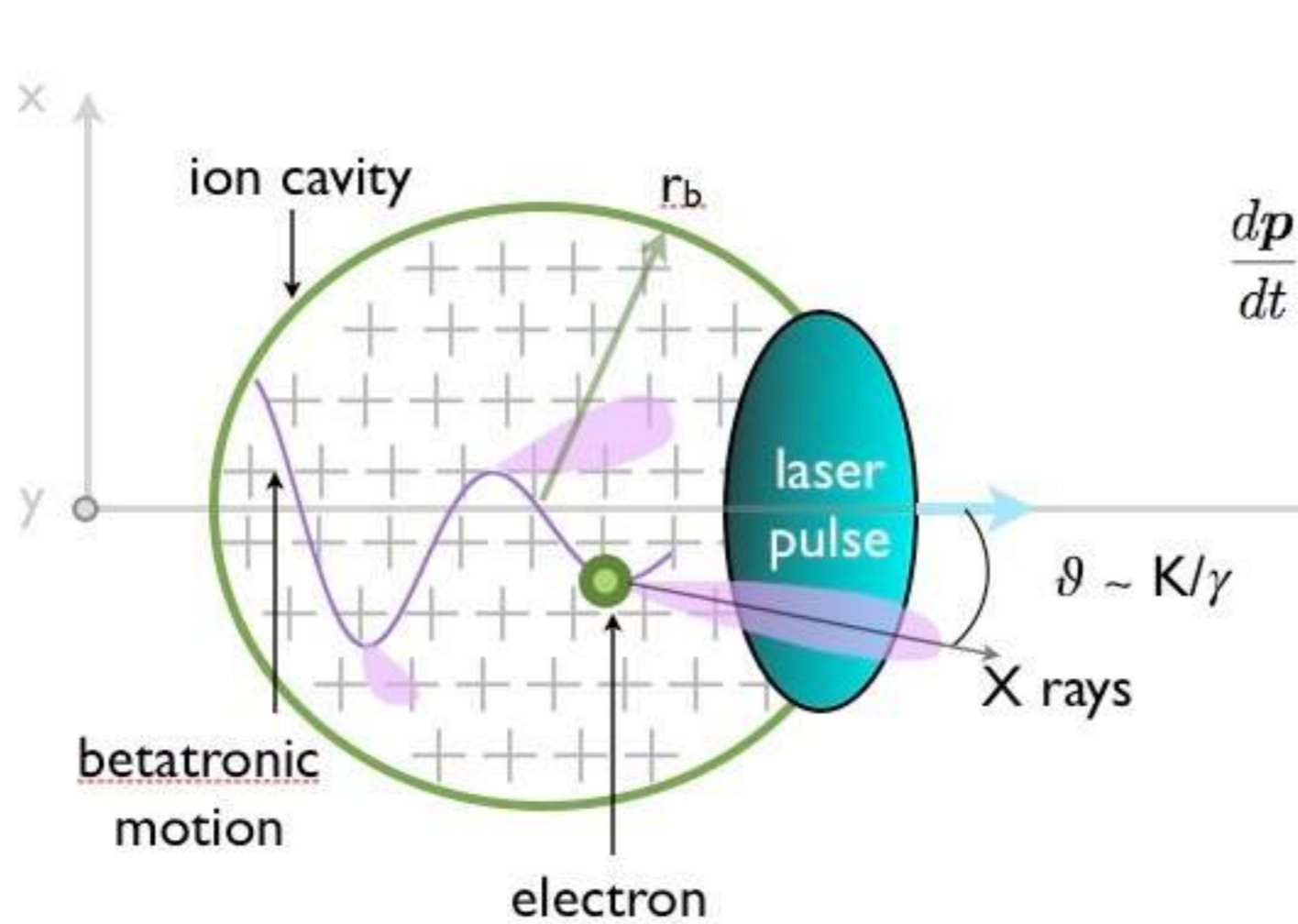
Radiated energy

\vec{n} unit vector in the observation direction



To efficiently produce X-ray radiation we need relativistic electrons undergoing oscillations (synchrotron radiation)

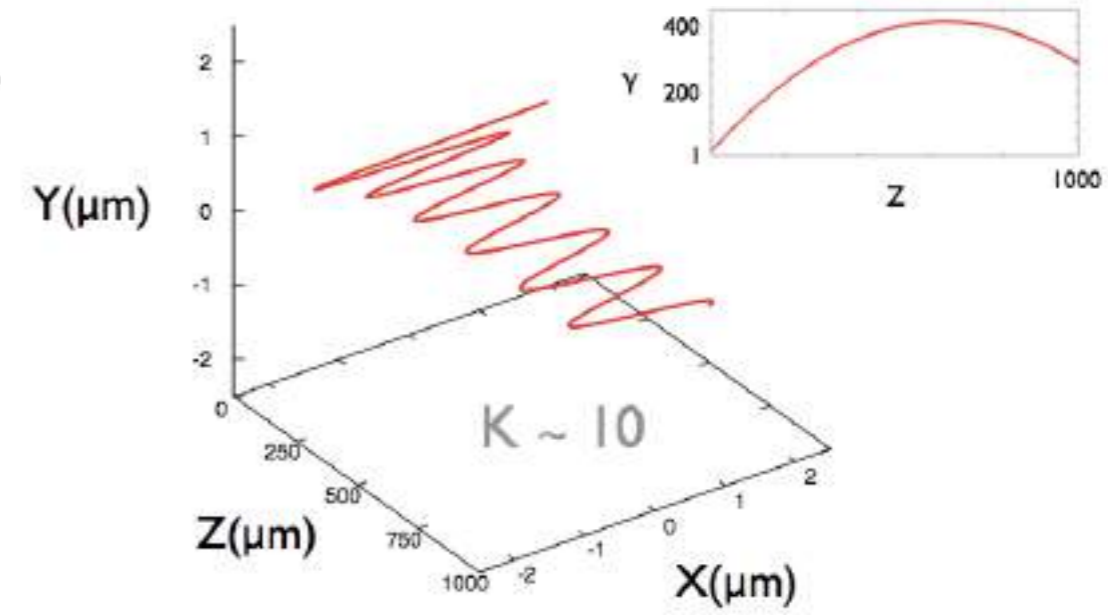
Betatron radiation properties



Transverse force

$$\frac{d\mathbf{p}}{dt} = \mathbf{F}_{\parallel} + \mathbf{F}_{\perp} = -\frac{m\omega_p^2}{2}\zeta\hat{z} - \frac{m\omega_p^2}{2}(x\hat{x} + y\hat{y})$$

Longitudinal Force



Betatron oscillation properties:

$$\lambda_u = \sqrt{2\gamma}\lambda_p$$

$$K = r_\beta k_p \sqrt{\gamma/2}$$

$\sim 100 \text{ MeV}$

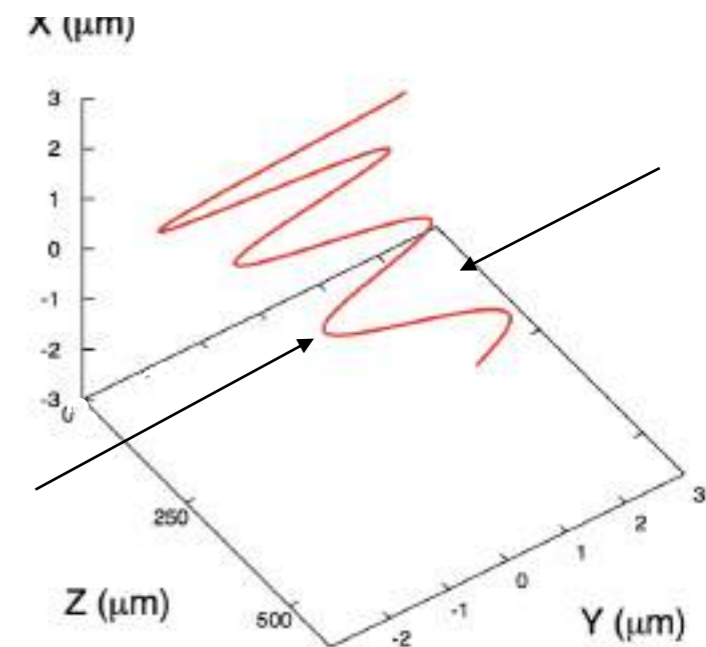
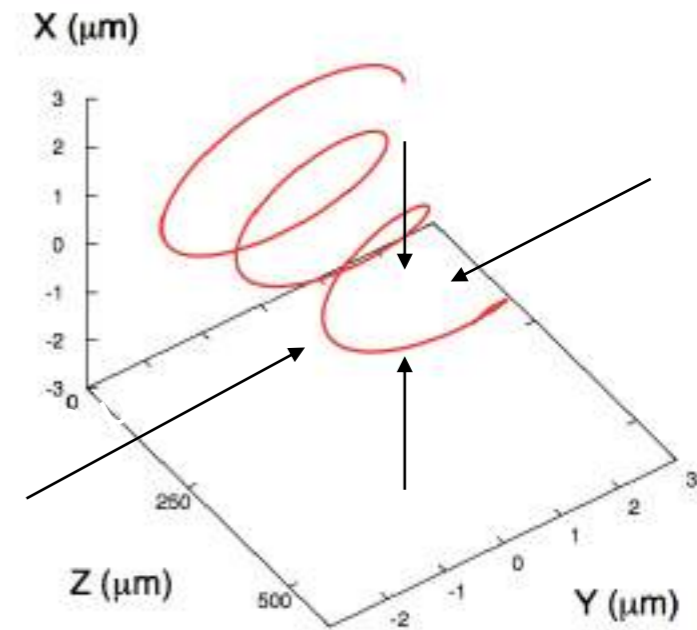
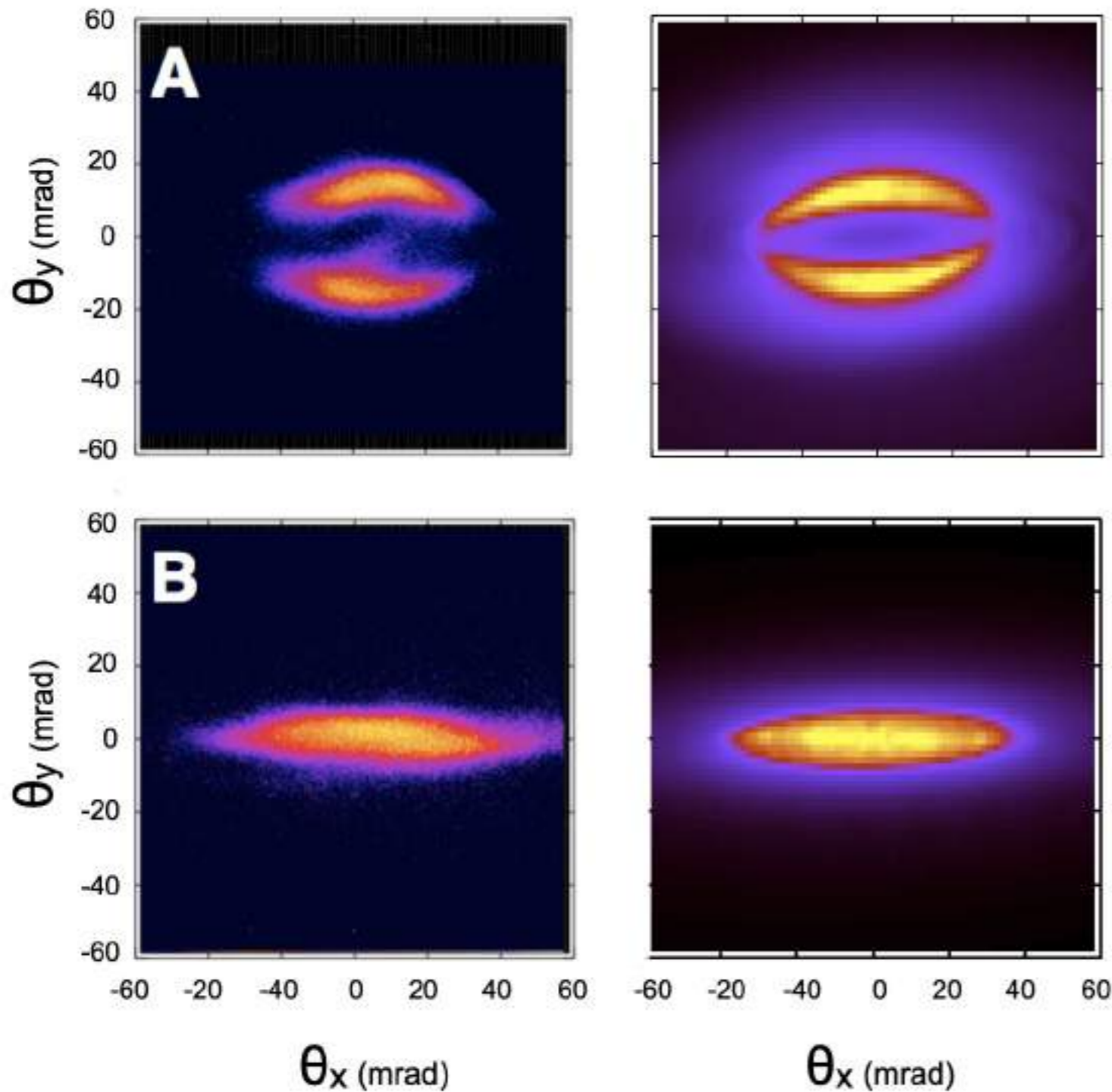
$r_\beta \sim 1 \mu\text{m}$

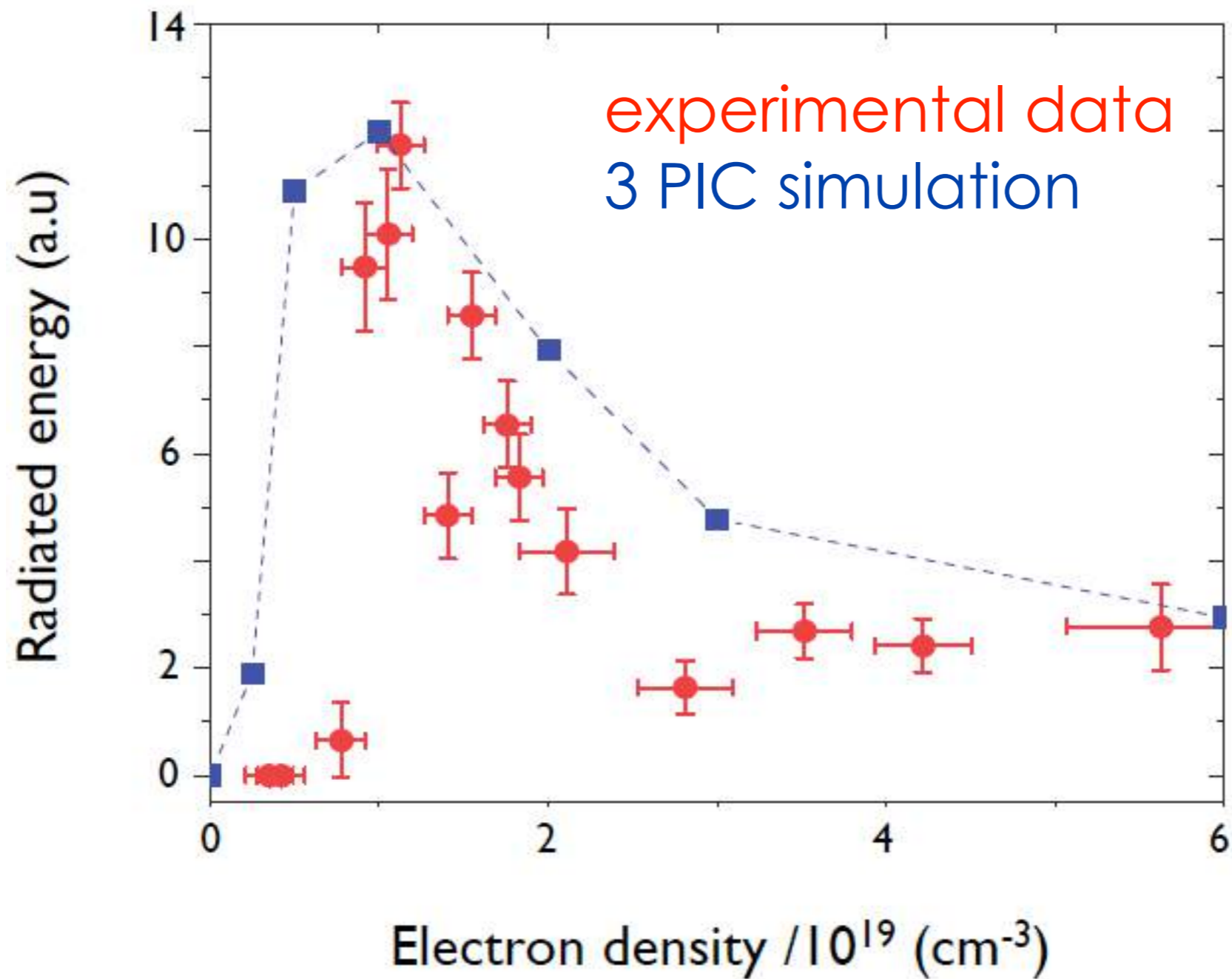
$n_e \sim 10^{19} \text{ cm}^{-3}$

$\lambda_u \sim 200 \mu\text{m}$

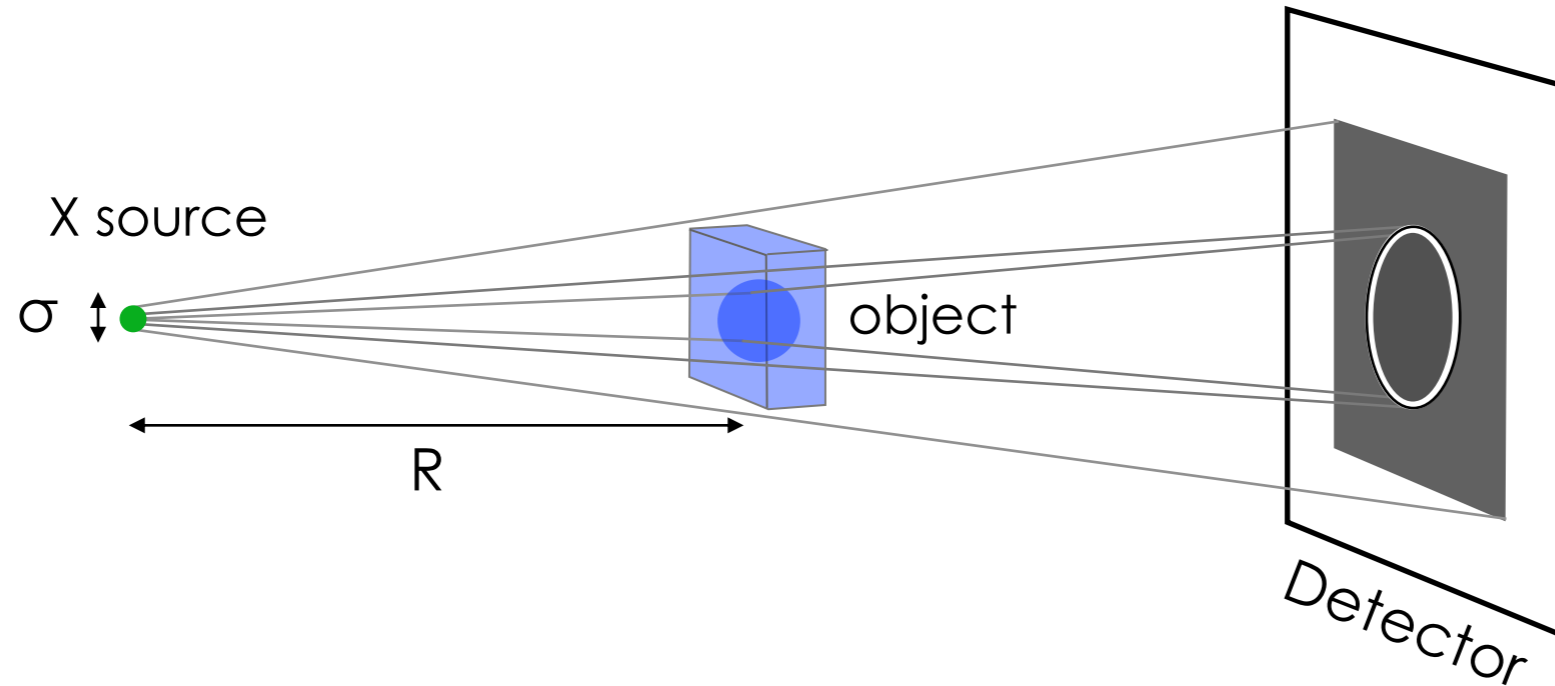
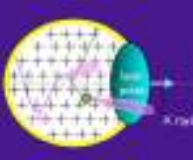
$K \sim 5$

Betatron radiation properties





A. Rousse *et al.*, Phys. Rev. Lett., 93, 135005 (2004)



- Absorption contrast

Contrast is due to the absorption difference in the object

It works only with object with important absorption difference

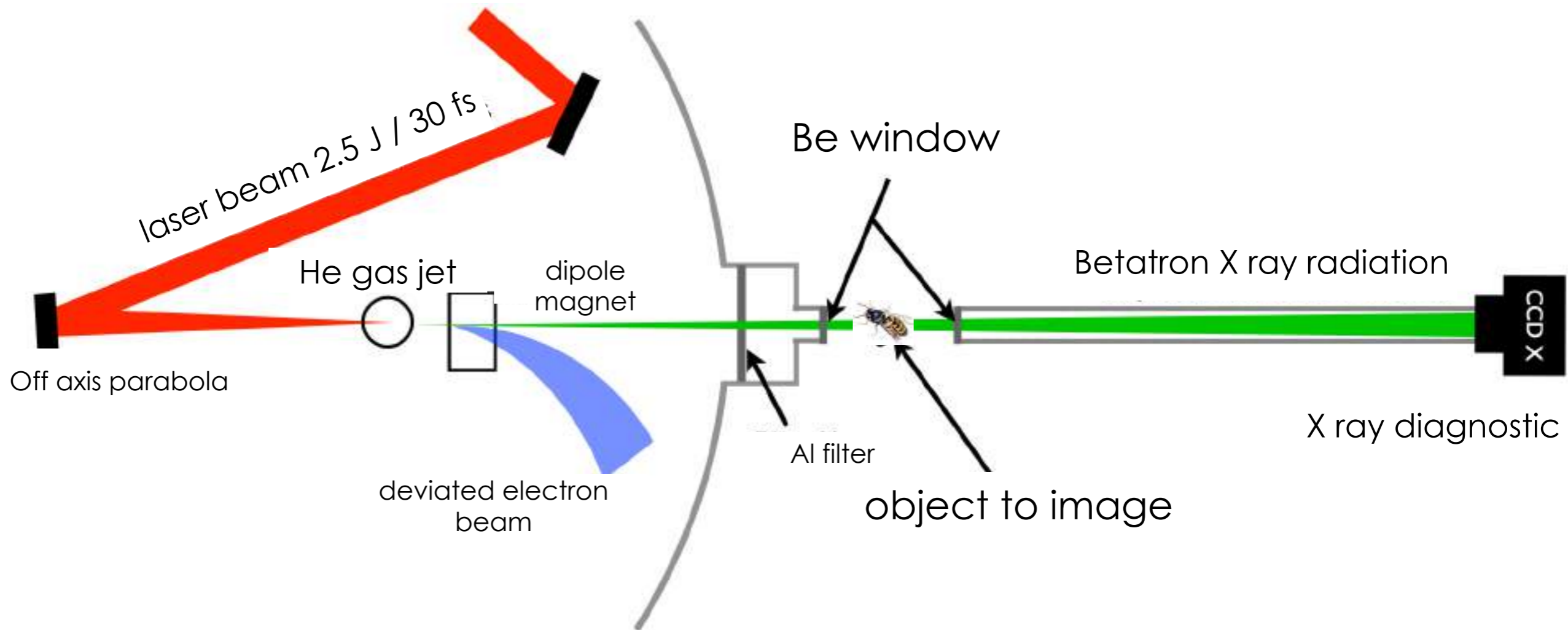
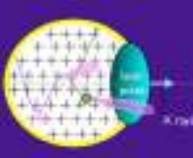
- Phase contrast

Interferences can reveal object interfaces

Biological objects have phase contrast 1000 times higher than absorption contrast

It requires a very high spatial coherence (10's microns) :

$$d = \lambda R / 2\pi\sigma$$



Parameters of the source :

- $E_c = 12.3 \text{ keV}$
- 2.2×10^8 photons/0.1%BW/sr/shot at 10 keV
- $N = 10^9$ photons in 28 mrad (FWHM) divergence beam

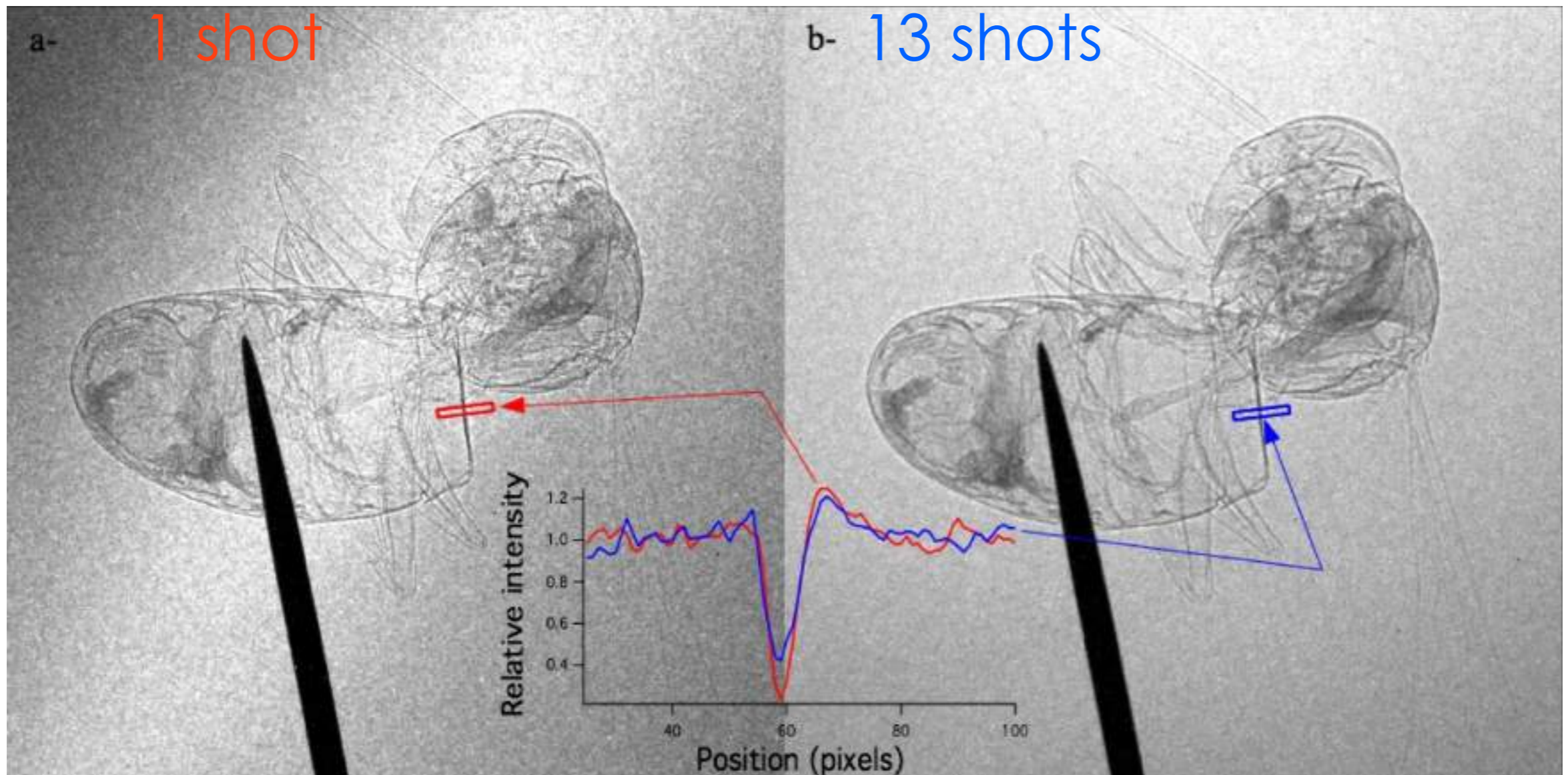
S. Fourmaux *et al.*, *Opt. Lett.* 36, 2426 (2011)



Phase contrast imaging : results

Bee contrast image :

- Contrast of 0.68 in single shot.
- Very tiny details can be observed in single shot that disappear in multi shots.



S. Fourmaux *et al.*, *Opt. Lett.* **36**, 2426 (2011)

X Contrast Phase Imaging

Early detection of tumour with an 10 micrometers resolution



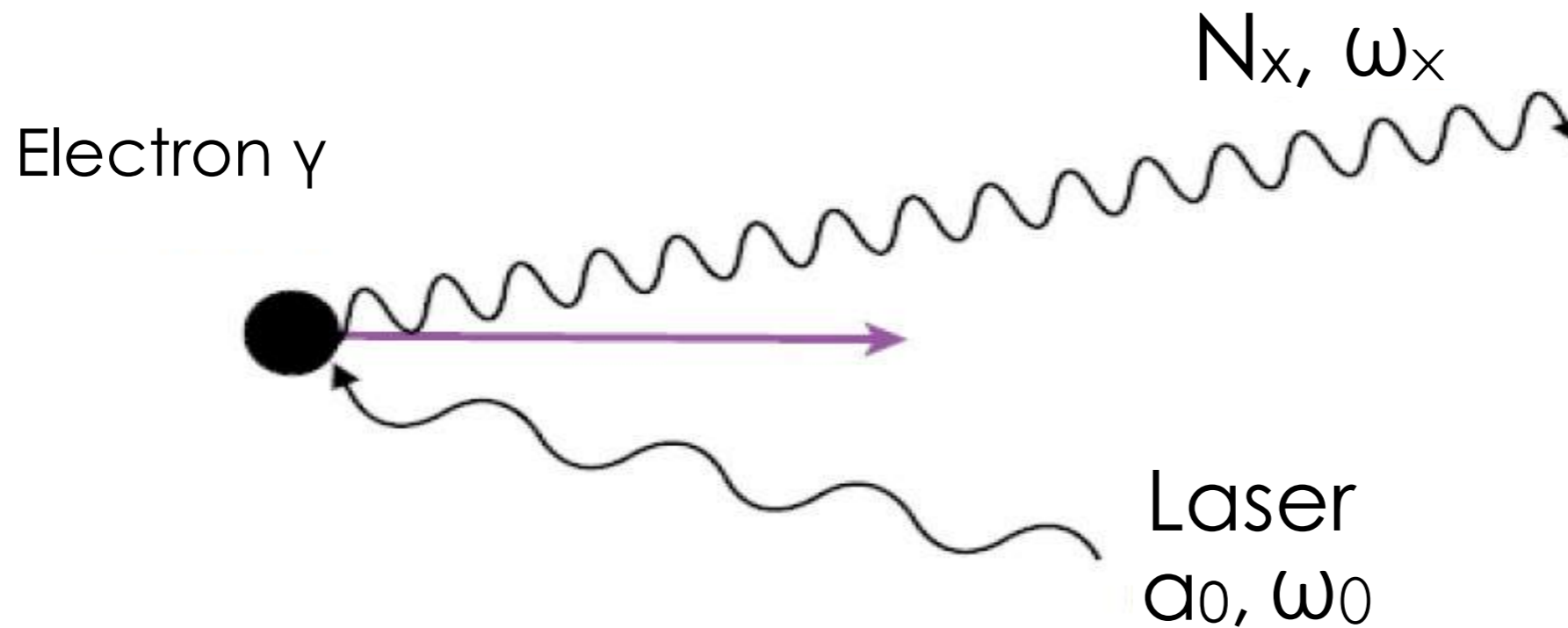
X ray Absorption Imaging



X ray Contrast Phase Imaging

M. Bech *et al.*, *Scientific reports* (2013)

Inverse Compton Scattering



Doppler upshift : high energy photons with modest e^- energy : $\omega_x = 4\gamma^2 \omega_0$

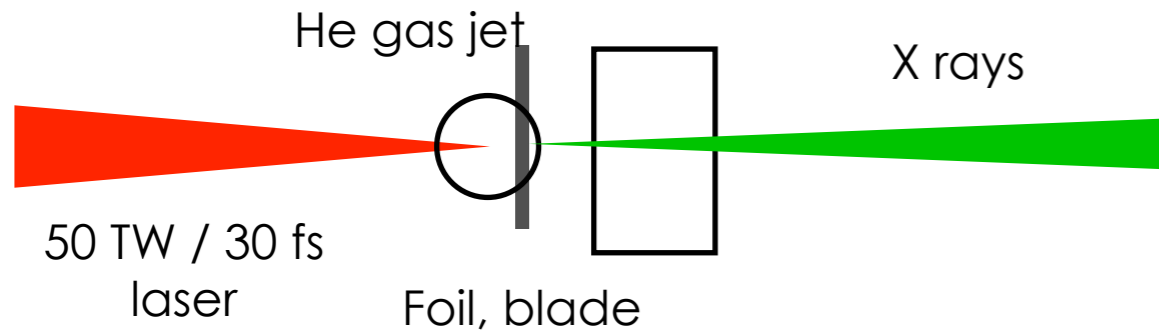
For example : 20 MeV electrons can produce 10 keV photons
200 MeV electrons can produce 1 MeV photons

The number of photons depends on the n_e and a_0^2 : $n_x \propto a_0^2 \times n_e$

Duration (fs), source size (μm) = e^- bunch length and electron beam size

Spectral bandwidth : $\Delta E/E \propto 2\Delta\gamma/\gamma, \gamma^2\Delta\theta^2$

Inverse Compton Scattering : new scheme



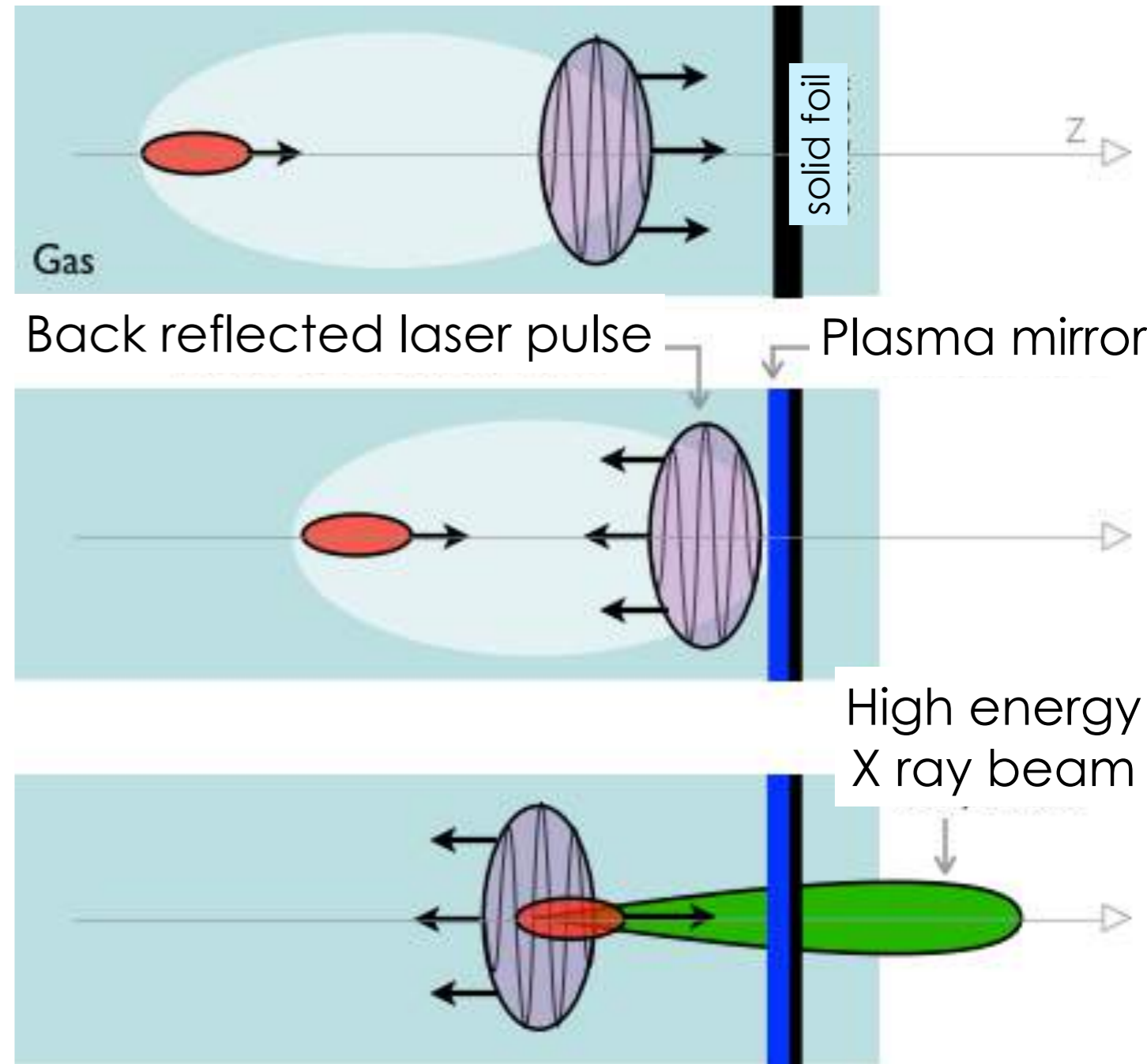
A single laser pulse

A plasma mirror reflects the laser beam

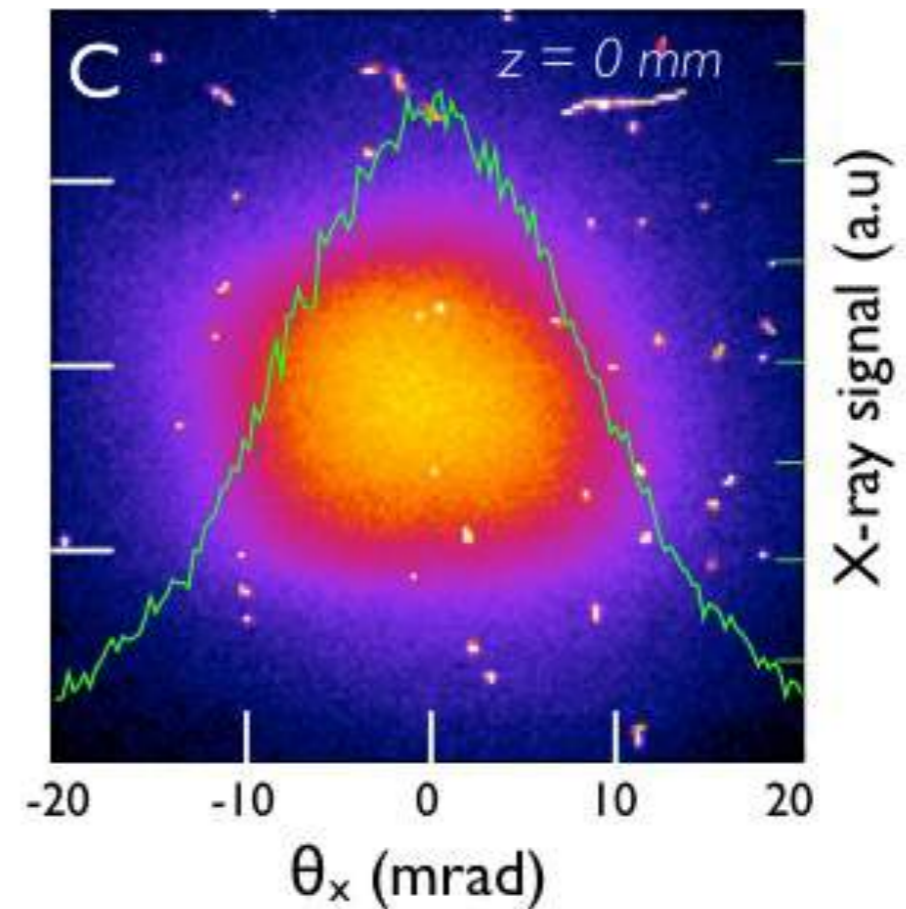
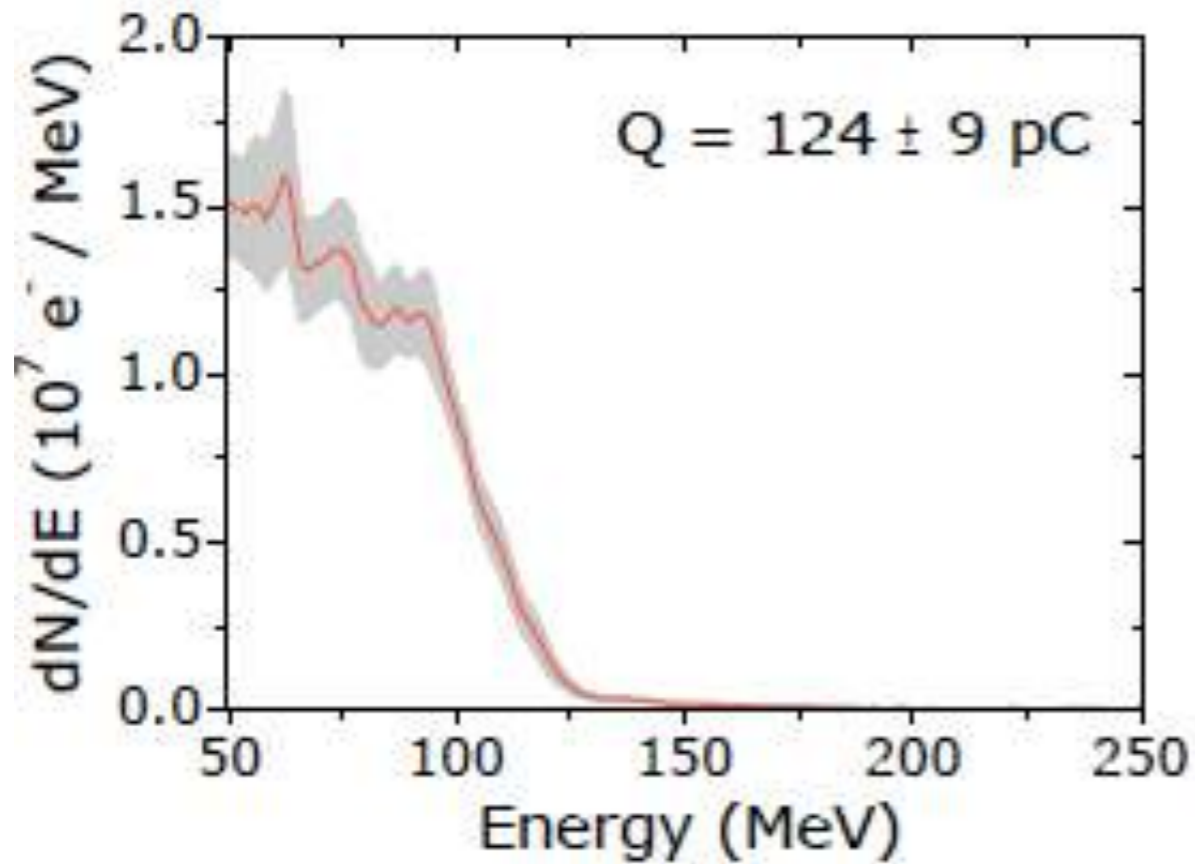
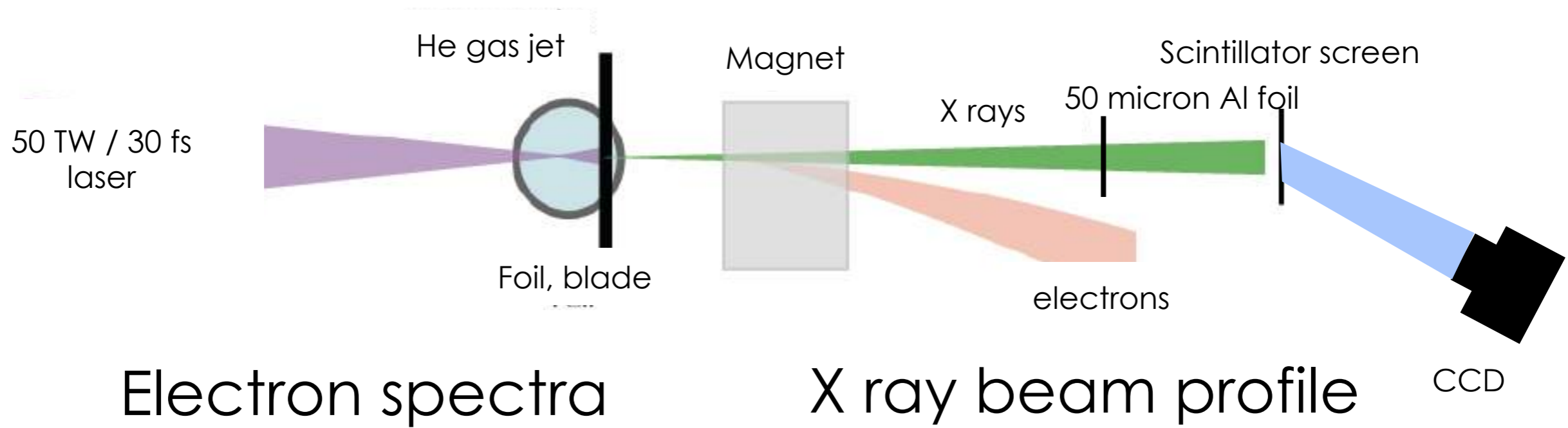
The back reflected laser collides with the accelerated electrons

No alignment : the laser and the electron beams naturally overlap

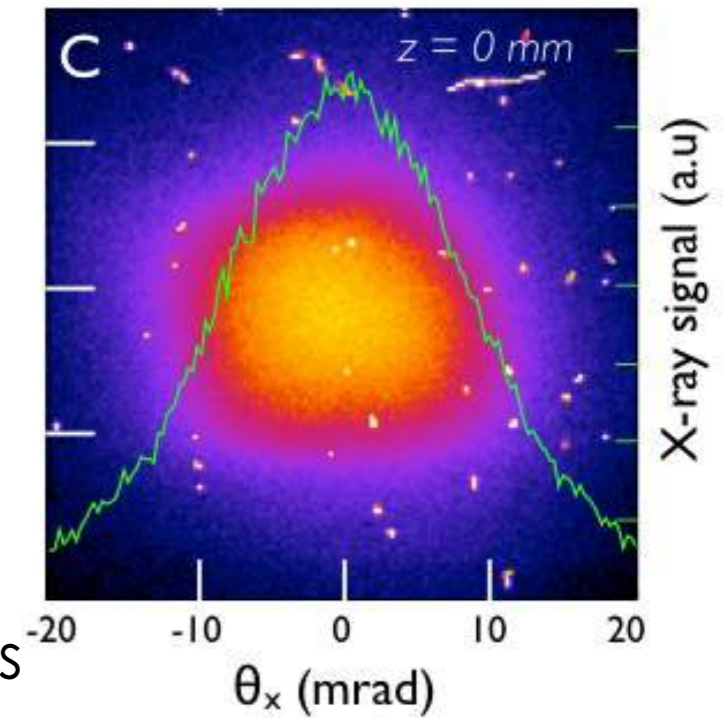
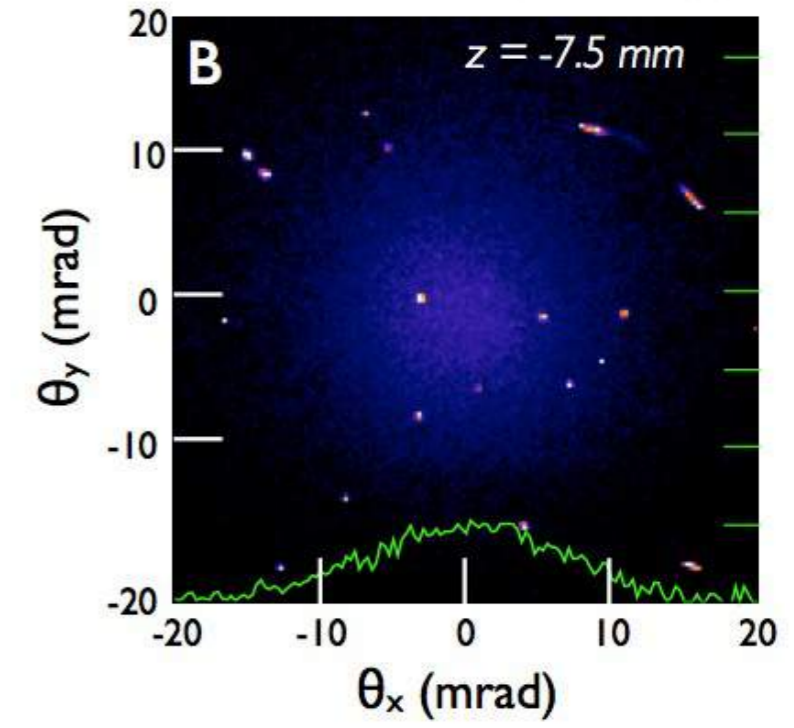
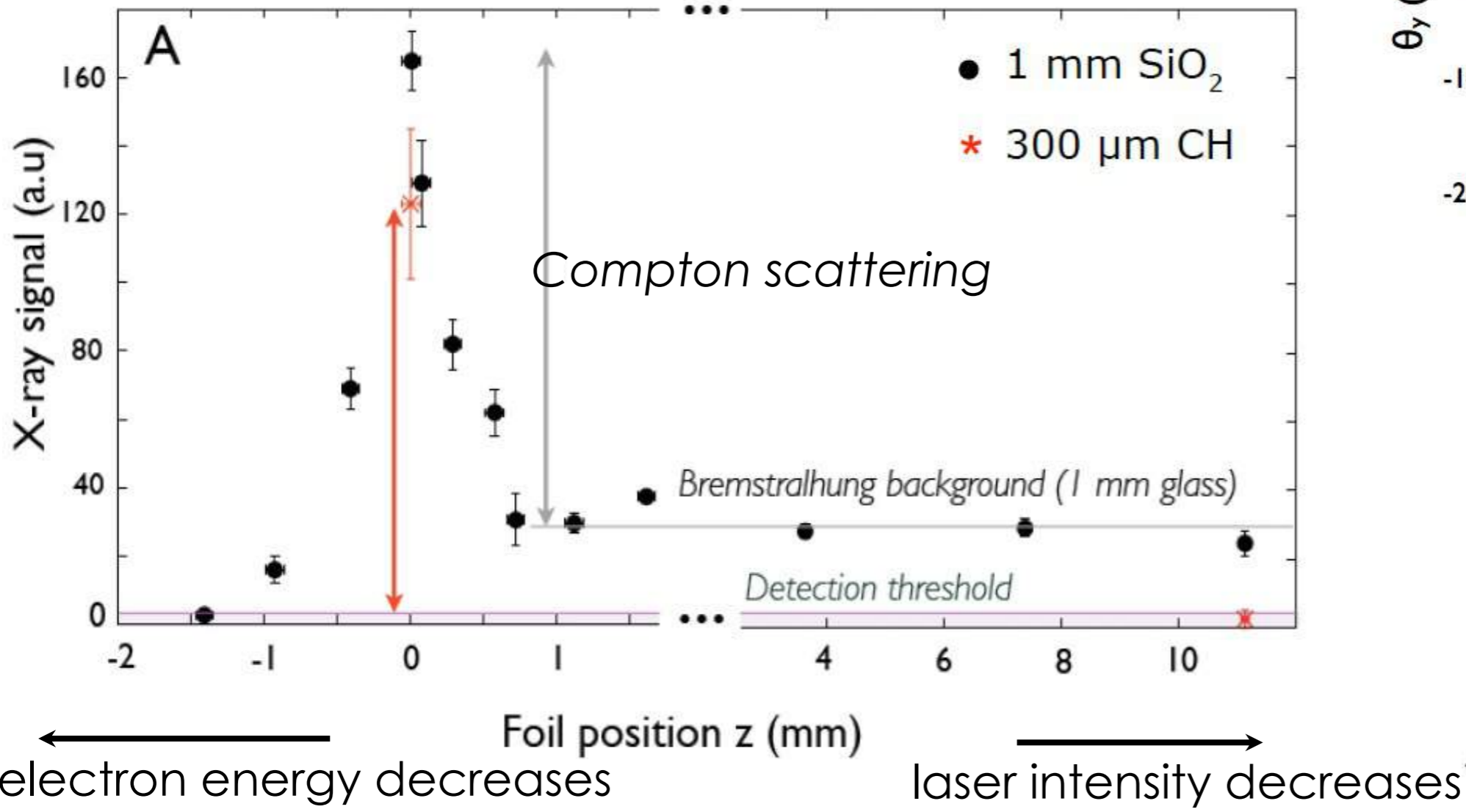
Save the laser energy !



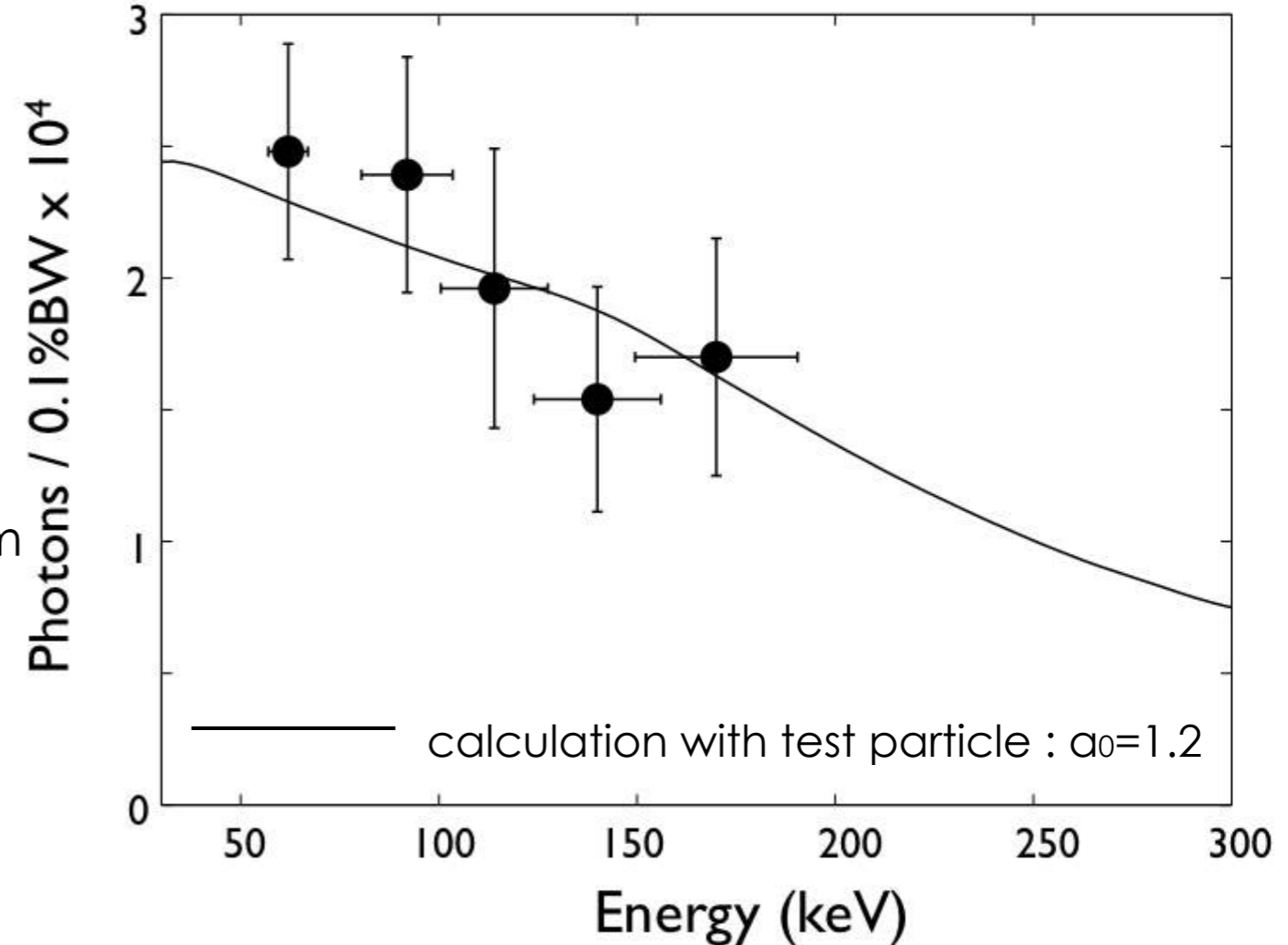
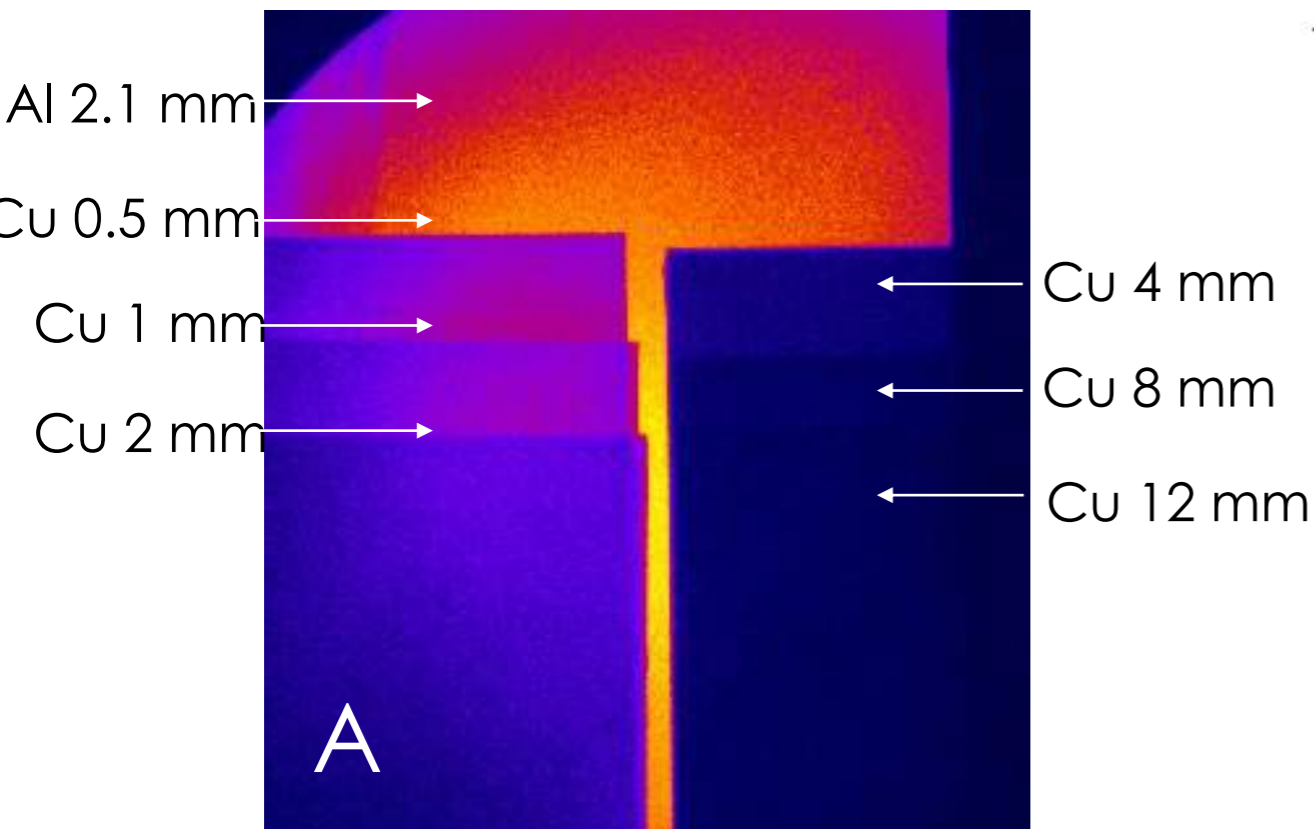
Inverse Compton Scattering : Exp. set-up



Inverse Compton Scattering : Exp. results



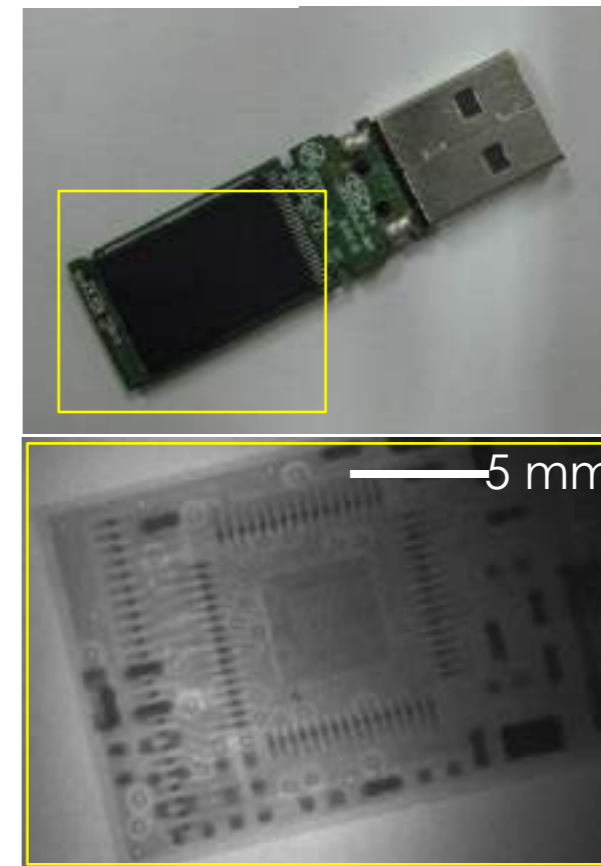
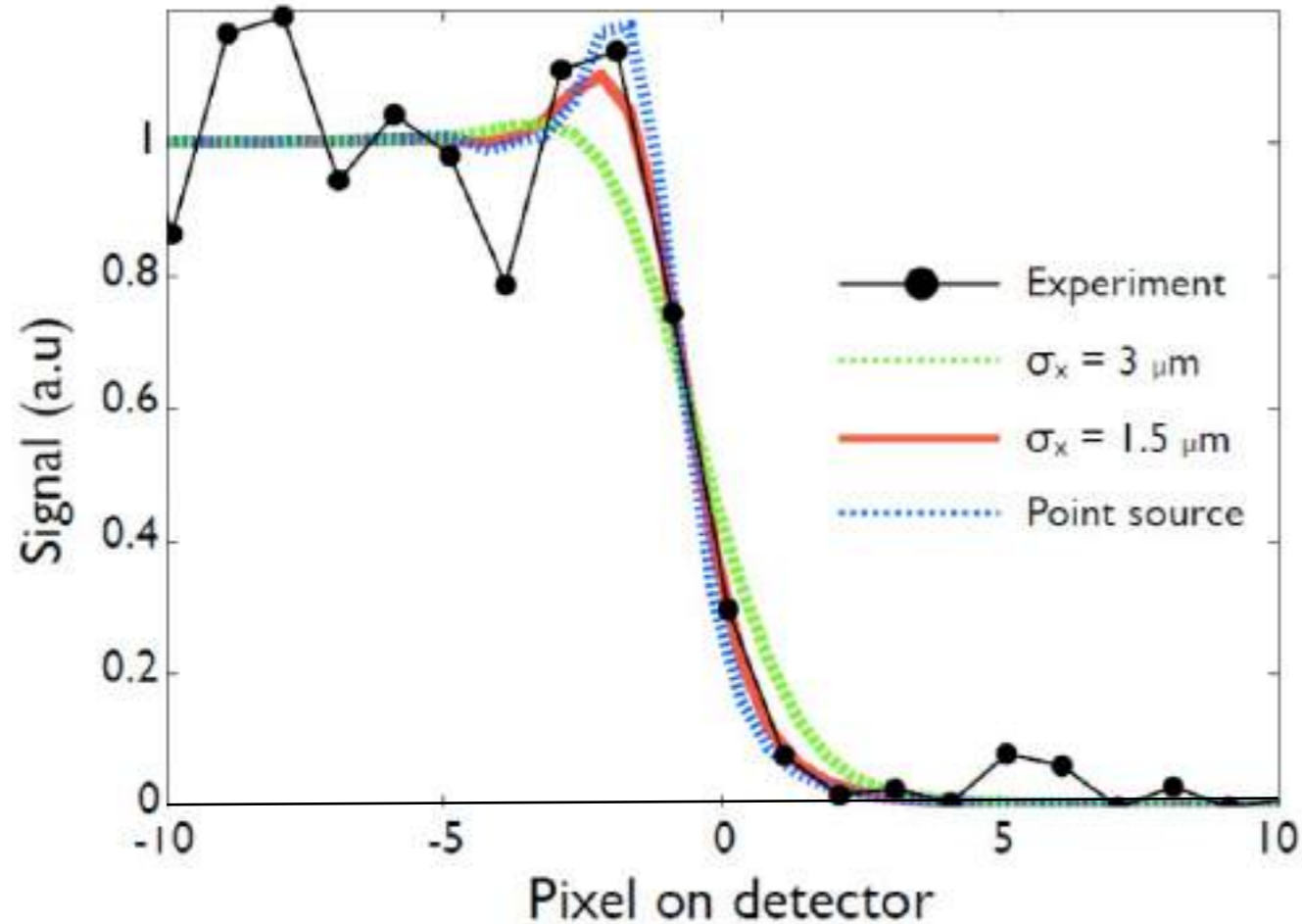
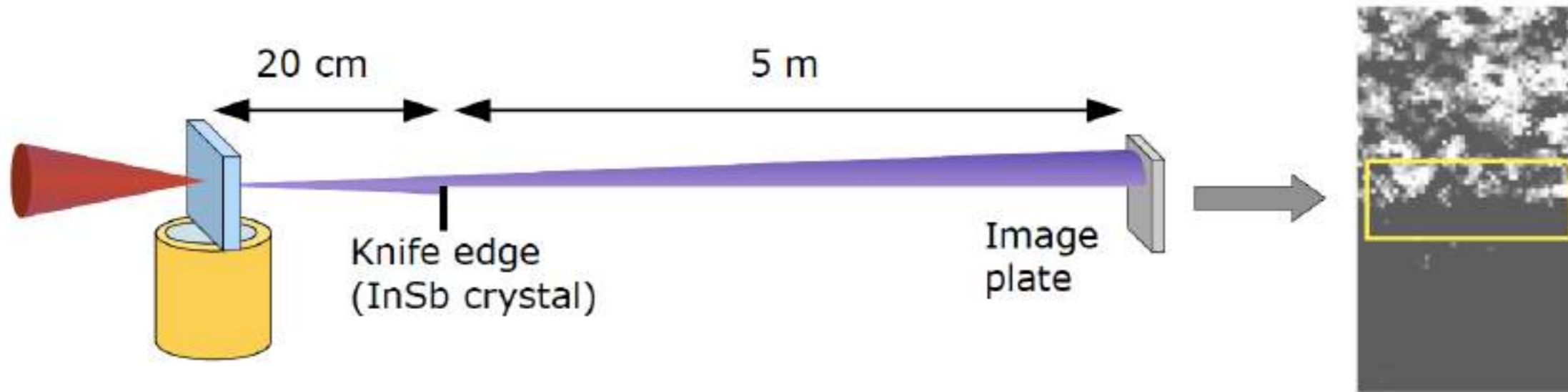
- The foil must be placed at the right to maximize a_0 and the electrons energy



- About 10^8 ph/shot, a few 10^4 ph/shot/0.1%BW@100 keV
- Broad electron spectrum => broad X ray spectra
- Brightness: 10^{21} ph/s/mm²/mrad²/0.1%BW @100 keV

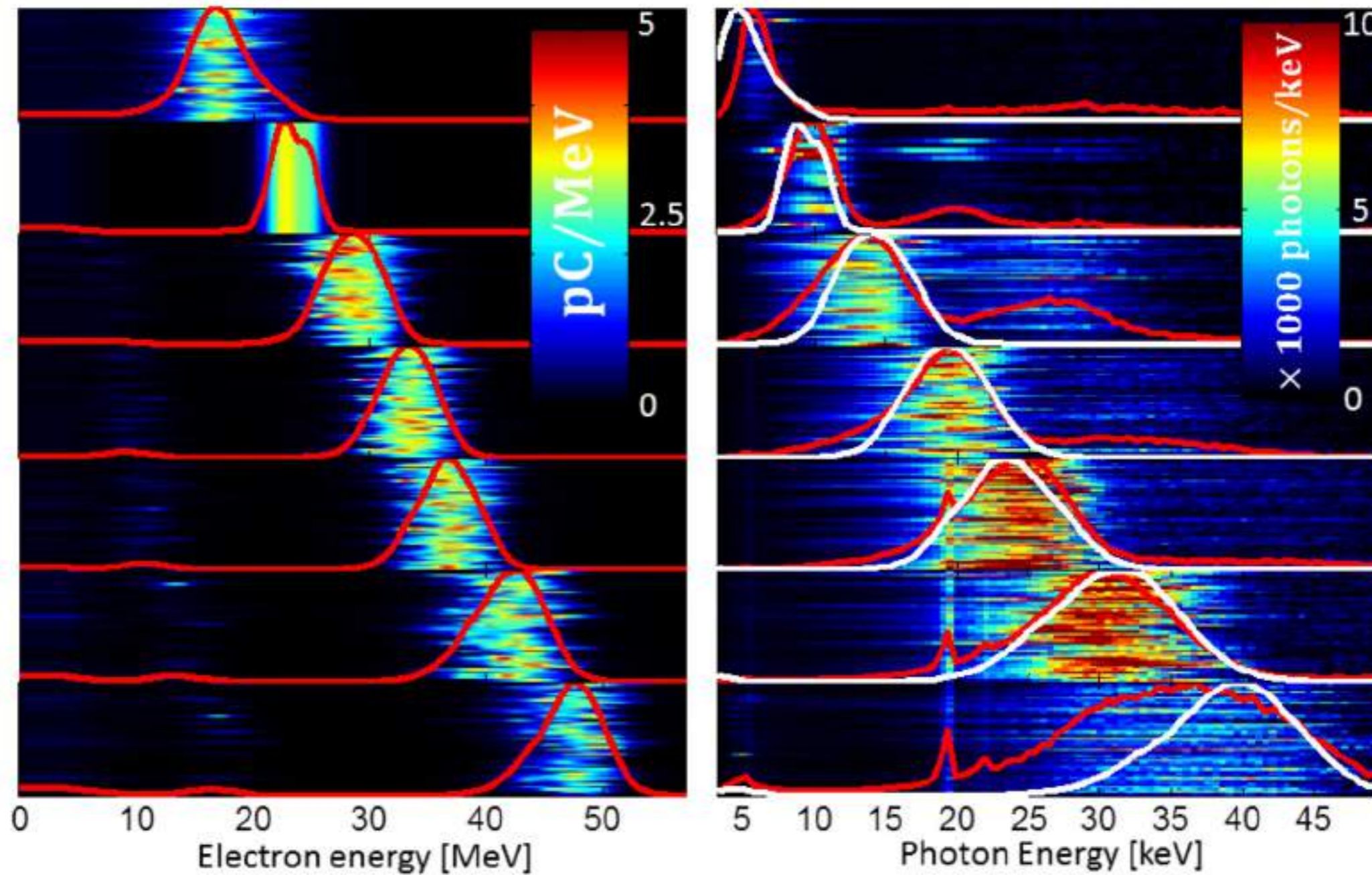
K. Ta Phuoc *et al.*, Nature Photonics (2012)

Inverse Compton Scattering : Source size



- In this image the resolution is limited by the detector and the small magnification

Inverse Compton Scattering : Compton Spectra



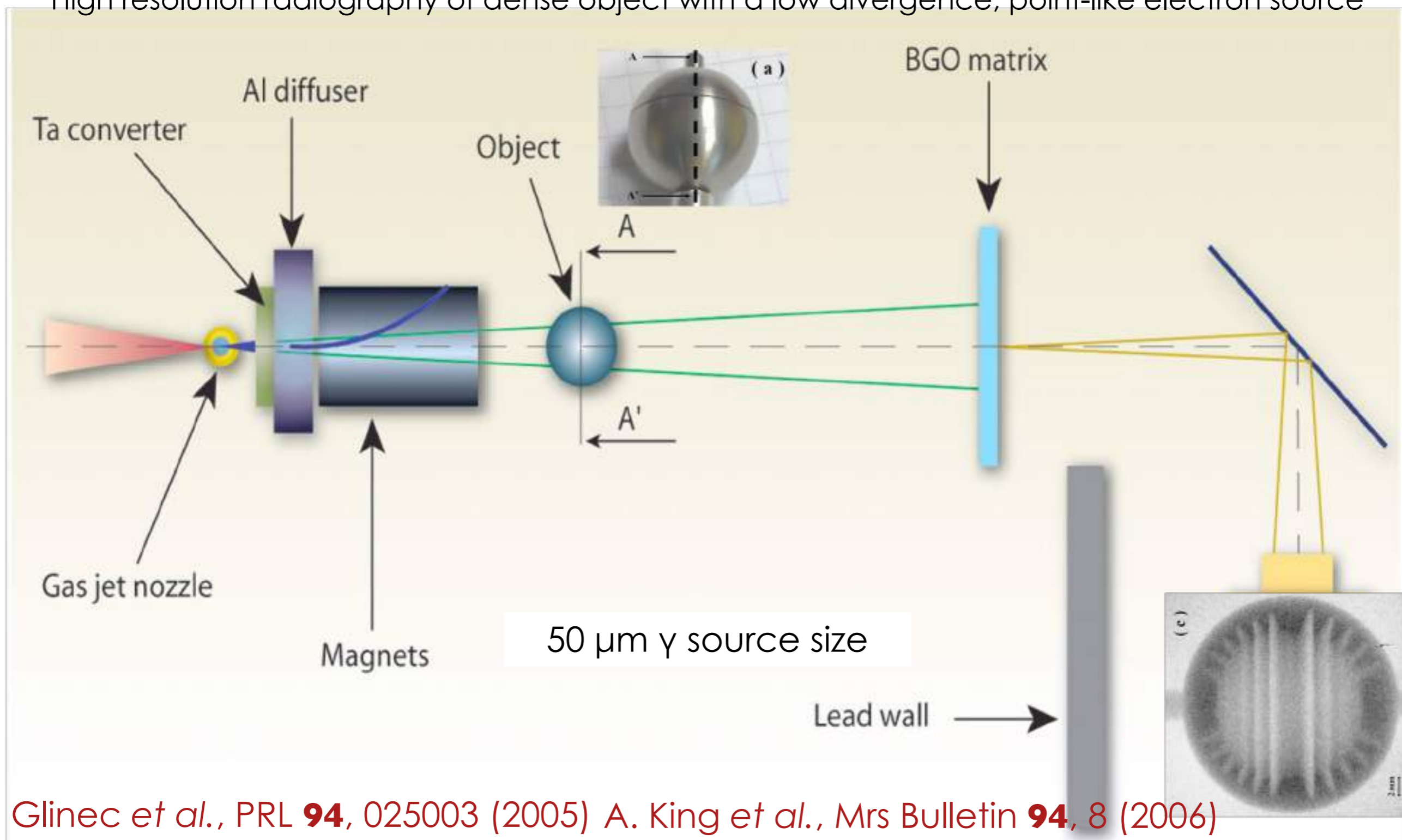
Courtesy of S. Karsh

Some examples of applications : radiography



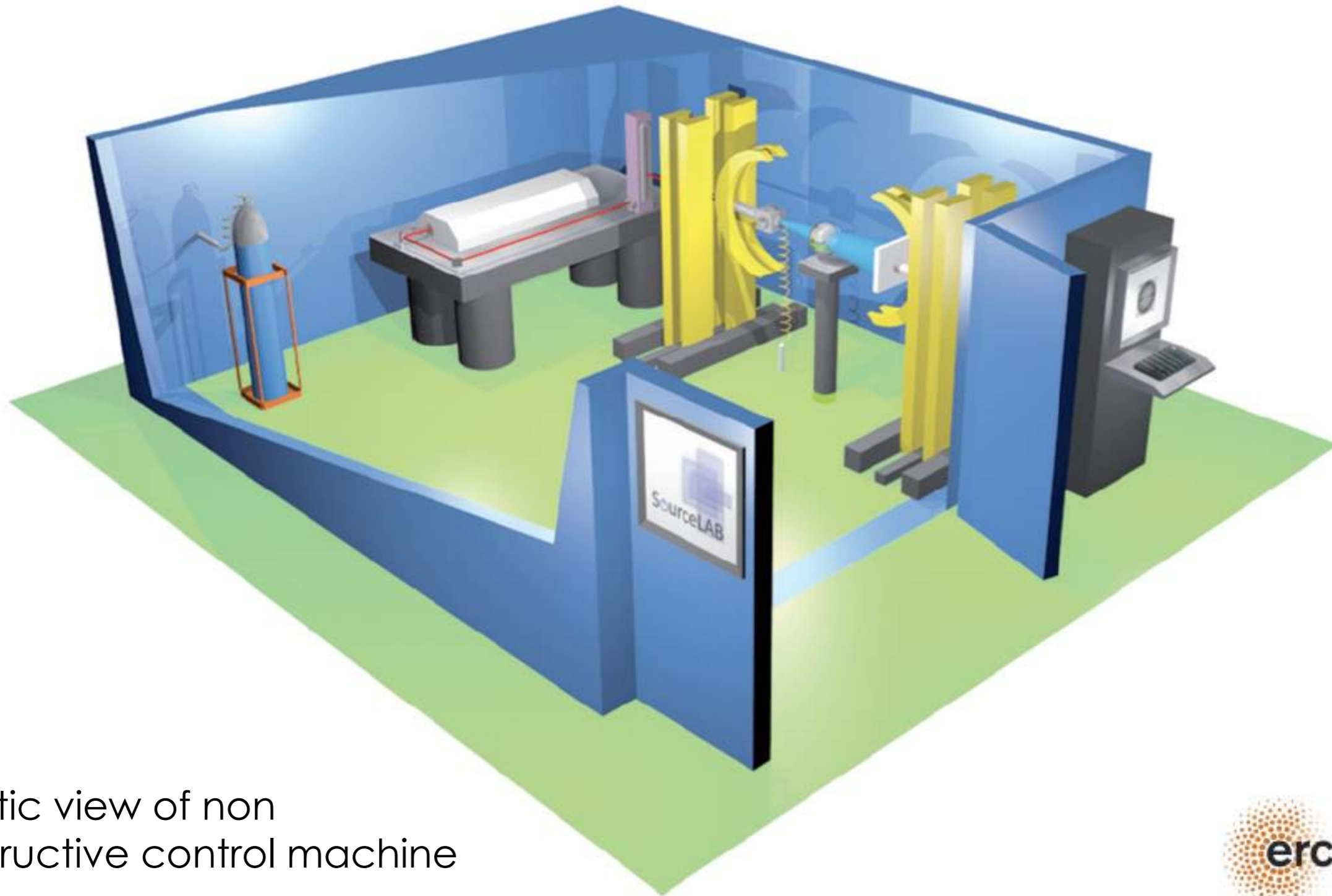
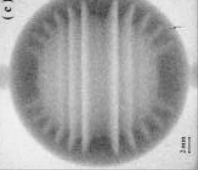
Non destructive dense matter inspection

High resolution radiography of dense object with a low divergence, point-like electron source



Y. Glinec *et al.*, PRL **94**, 025003 (2005) A. King *et al.*, Mrs Bulletin **94**, 8 (2006)

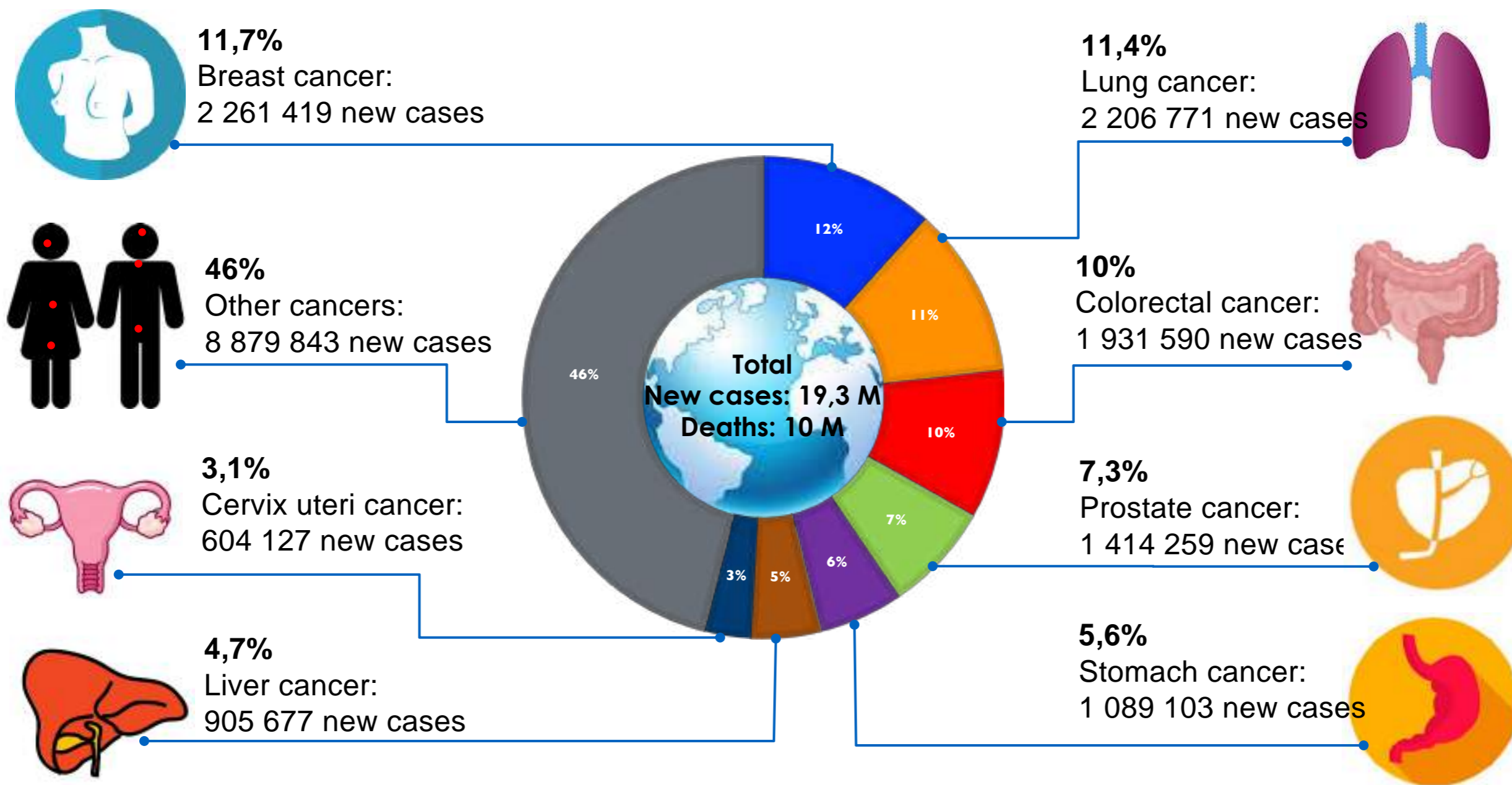
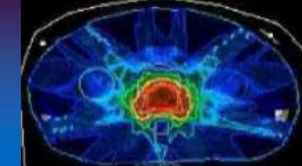
A. Ben-Ismaïl *et al.*, Nucl. Instr. and Meth. A **629** (2010), App. Phys. Lett. **98**, 264101 (2011)



Artistic view of non destructive control machine



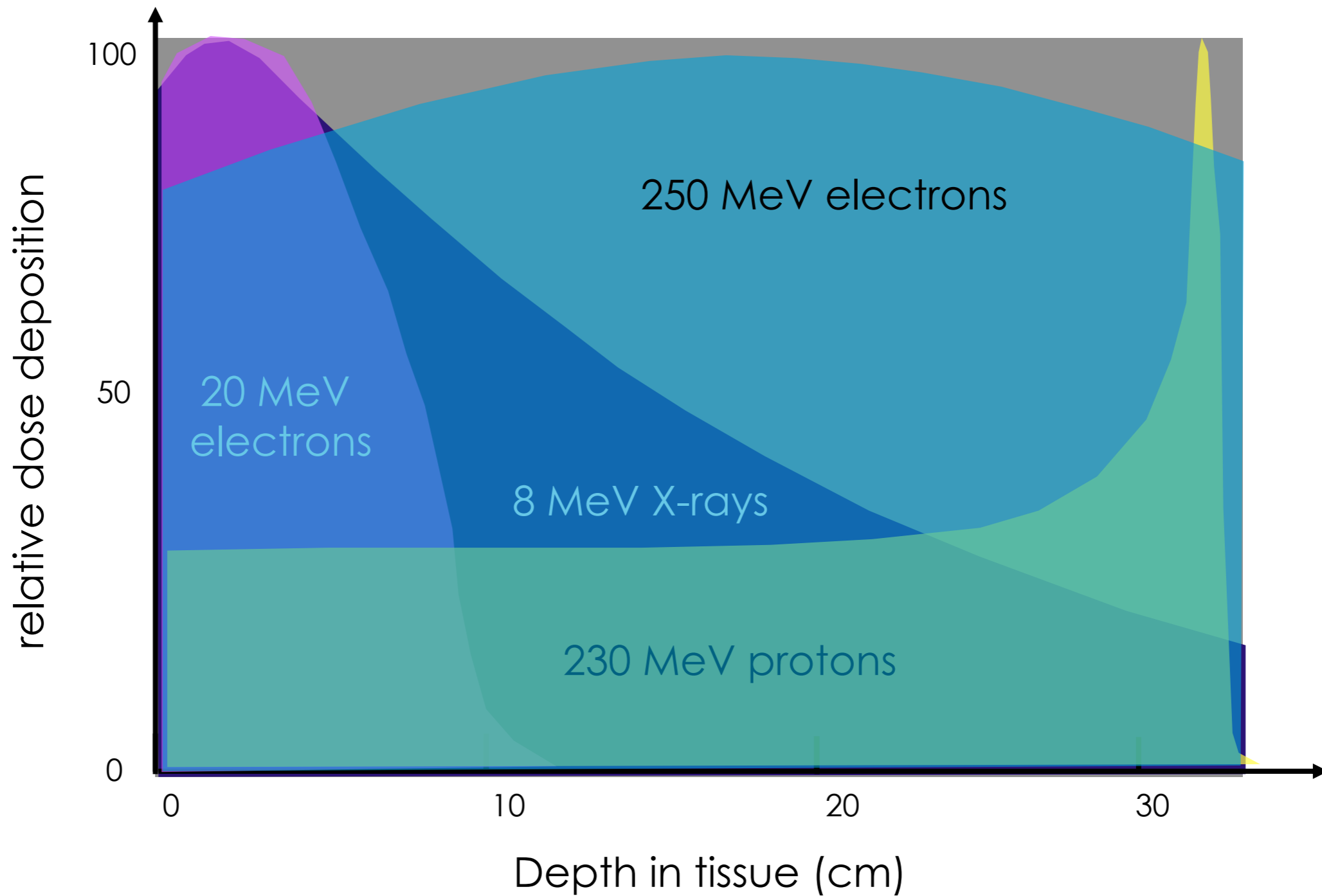
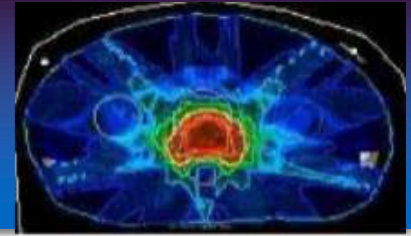
Cancer : facts and numbers

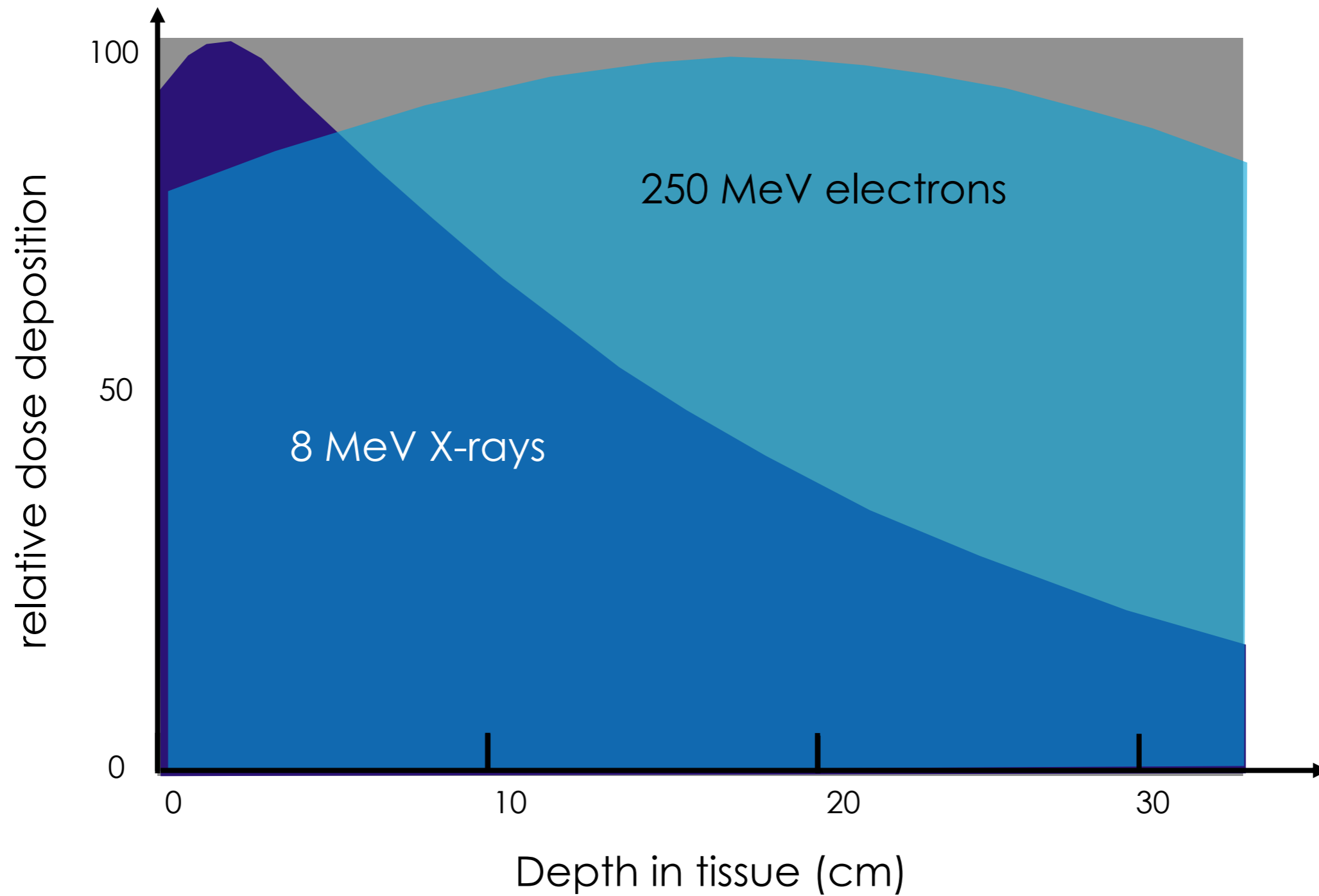
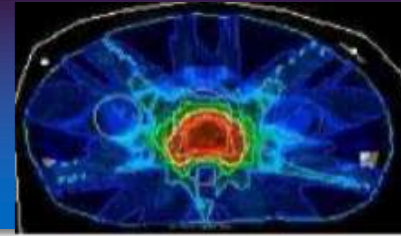


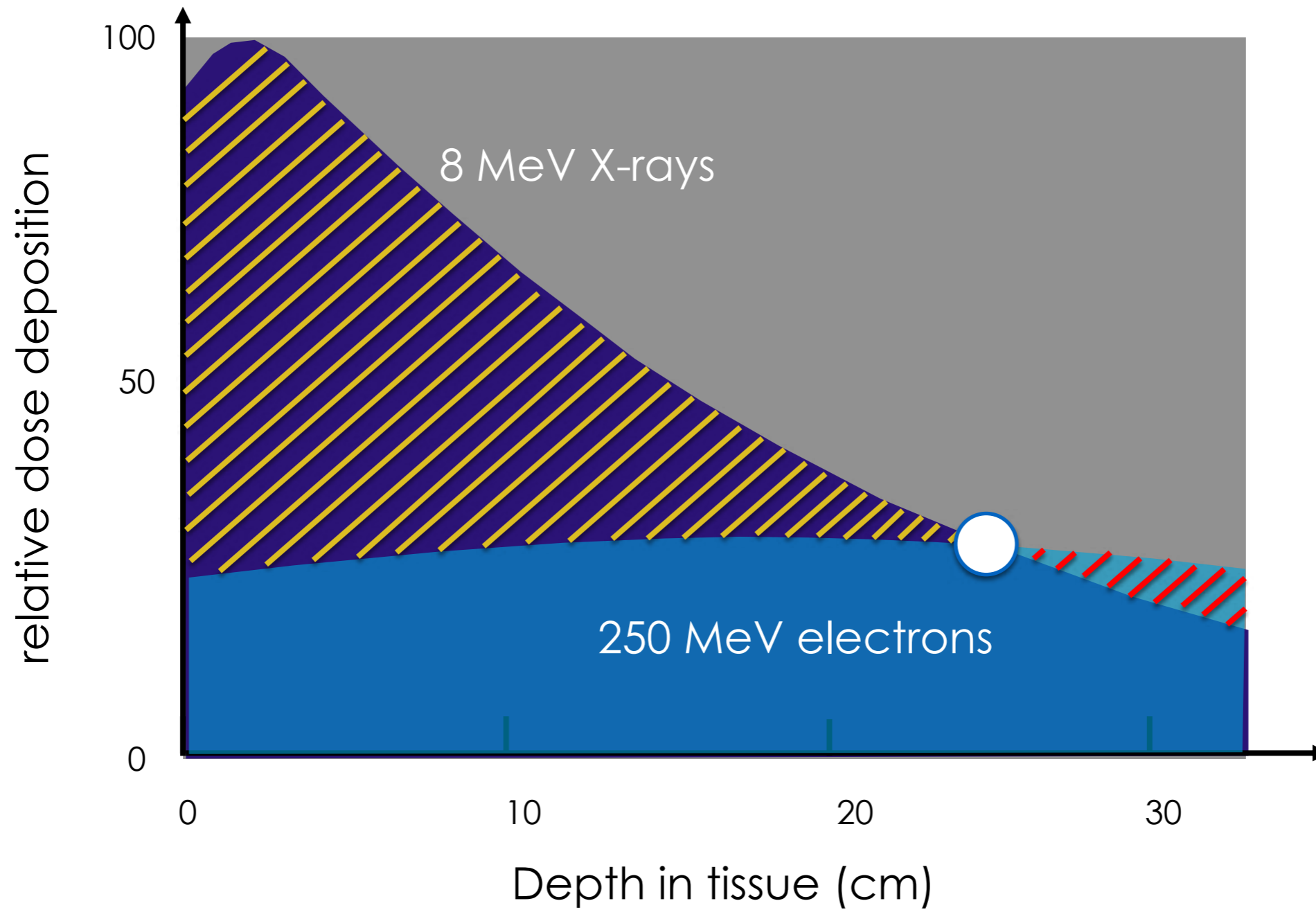
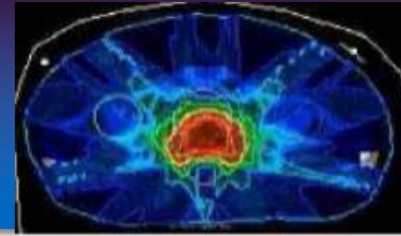
Estimated number of new cases in 2020, all cancers, both sexes, all ages*

*World Health Organization: press release No 238 (2020)

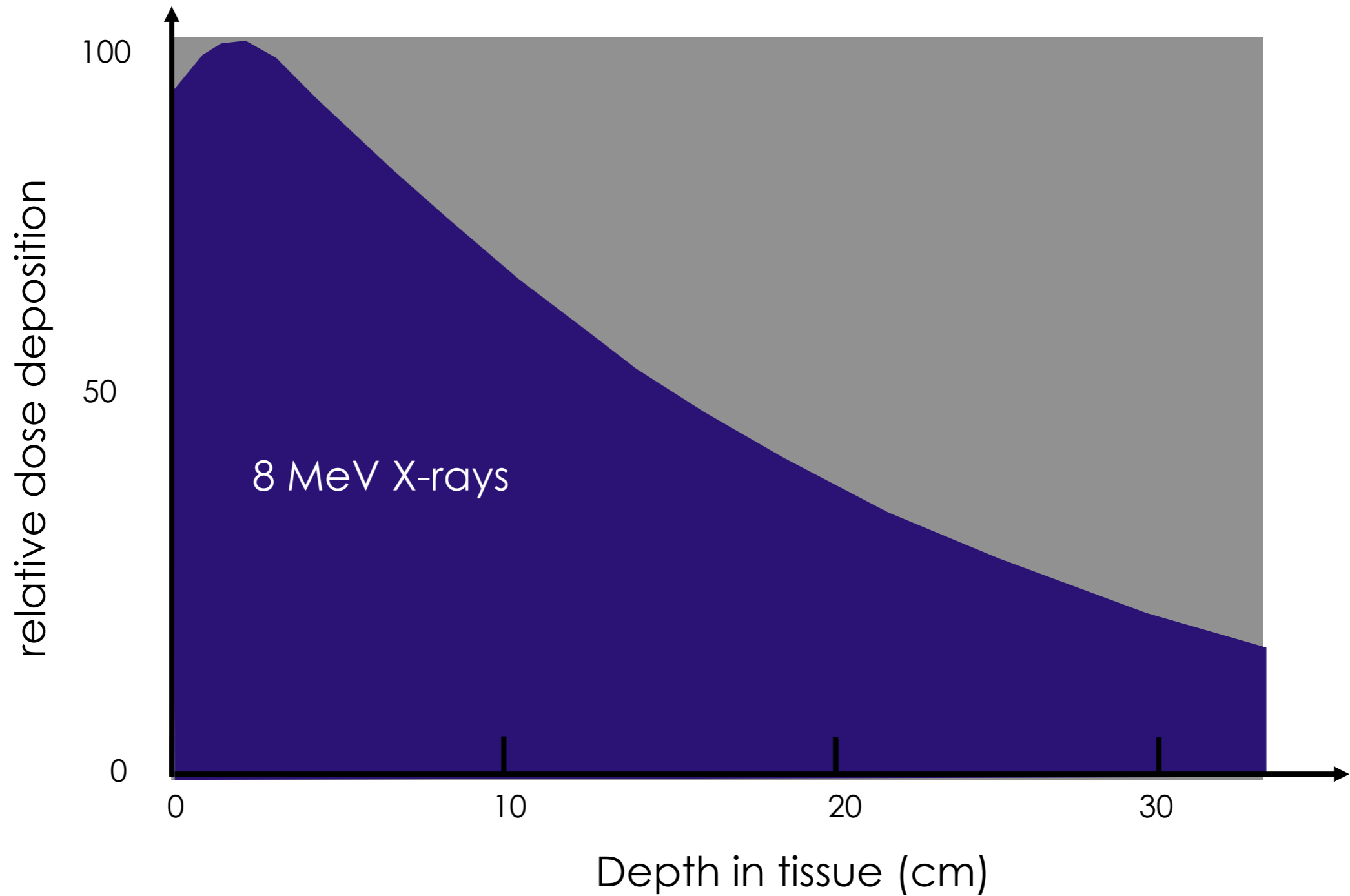
Particles @ radiation for therapy



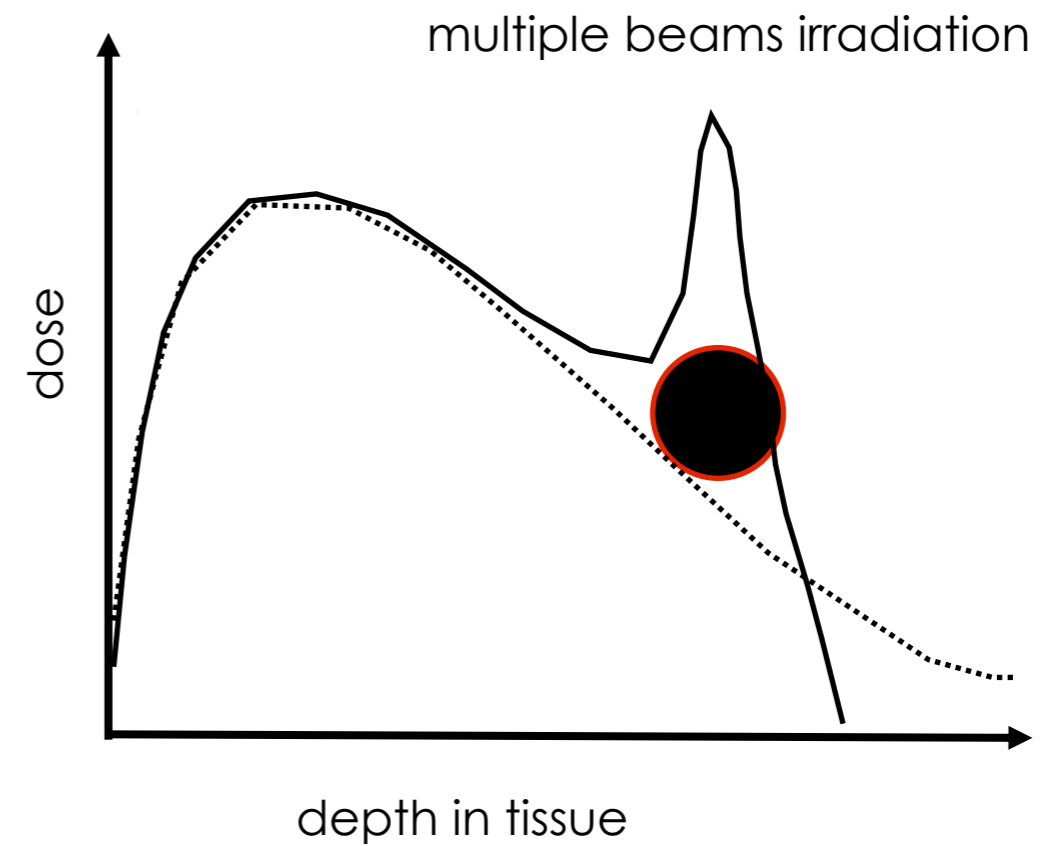
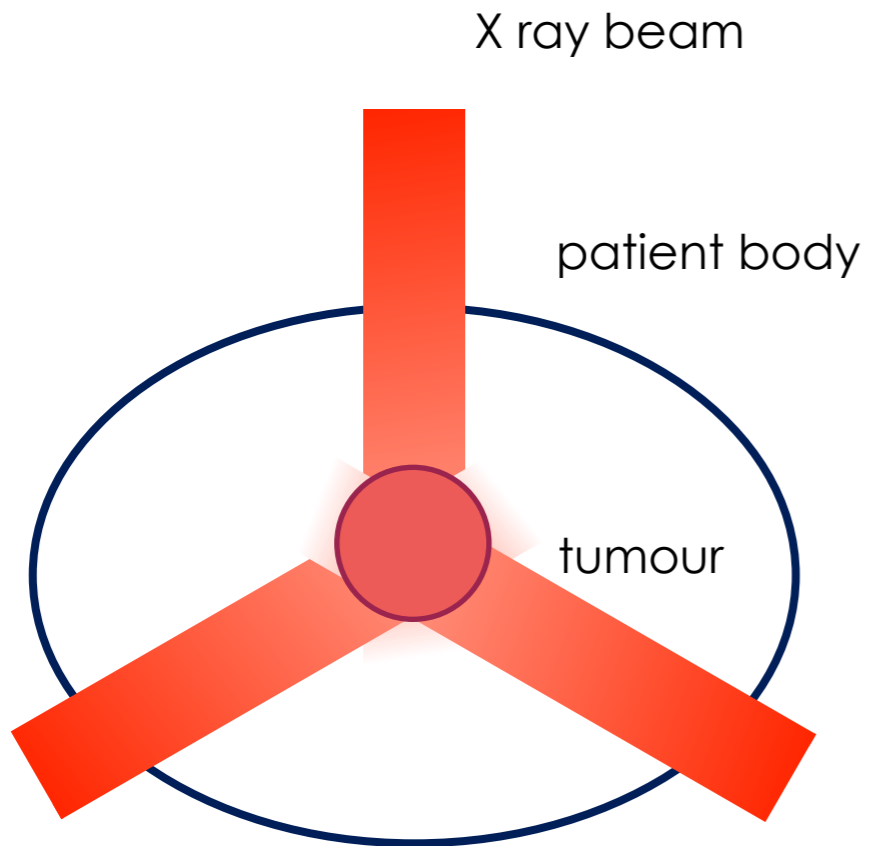
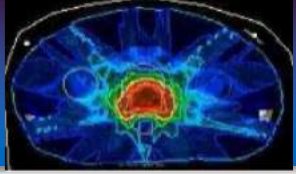




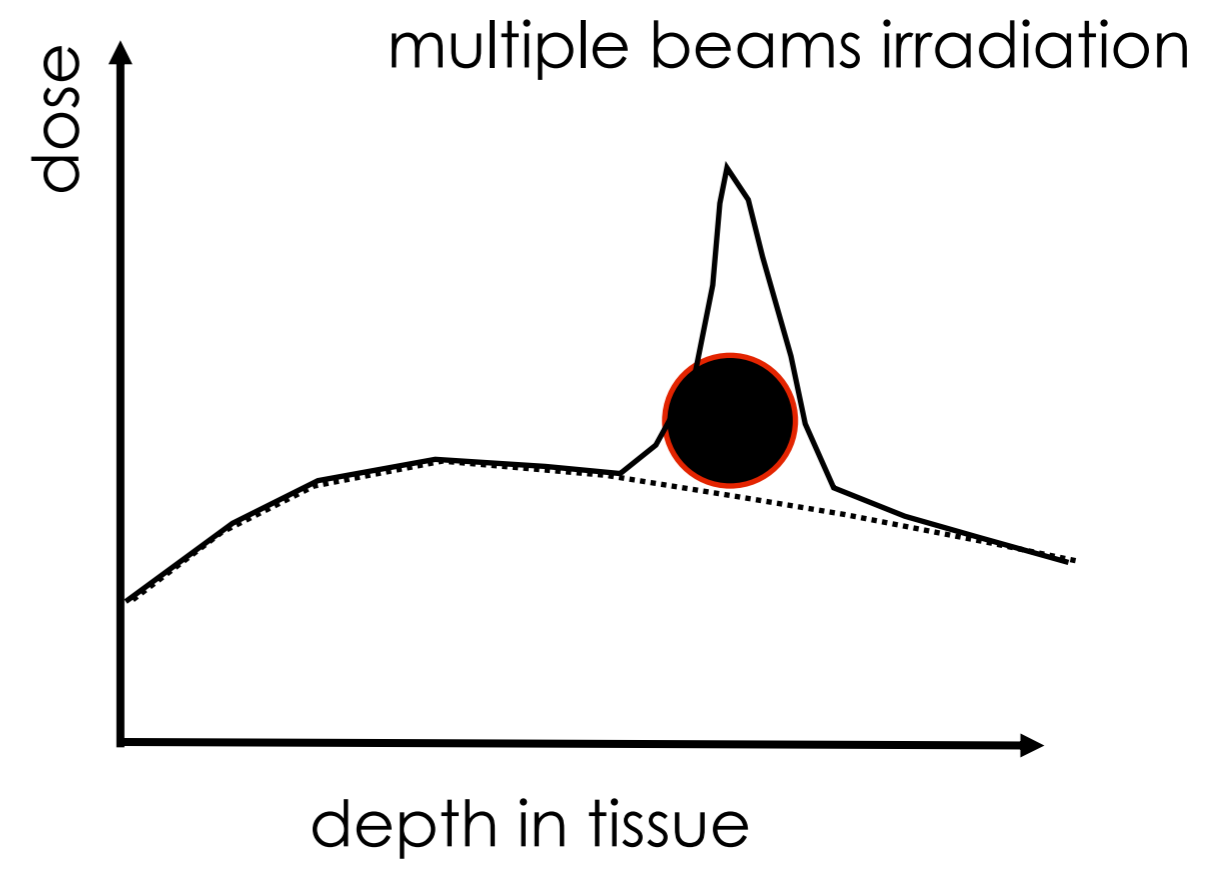
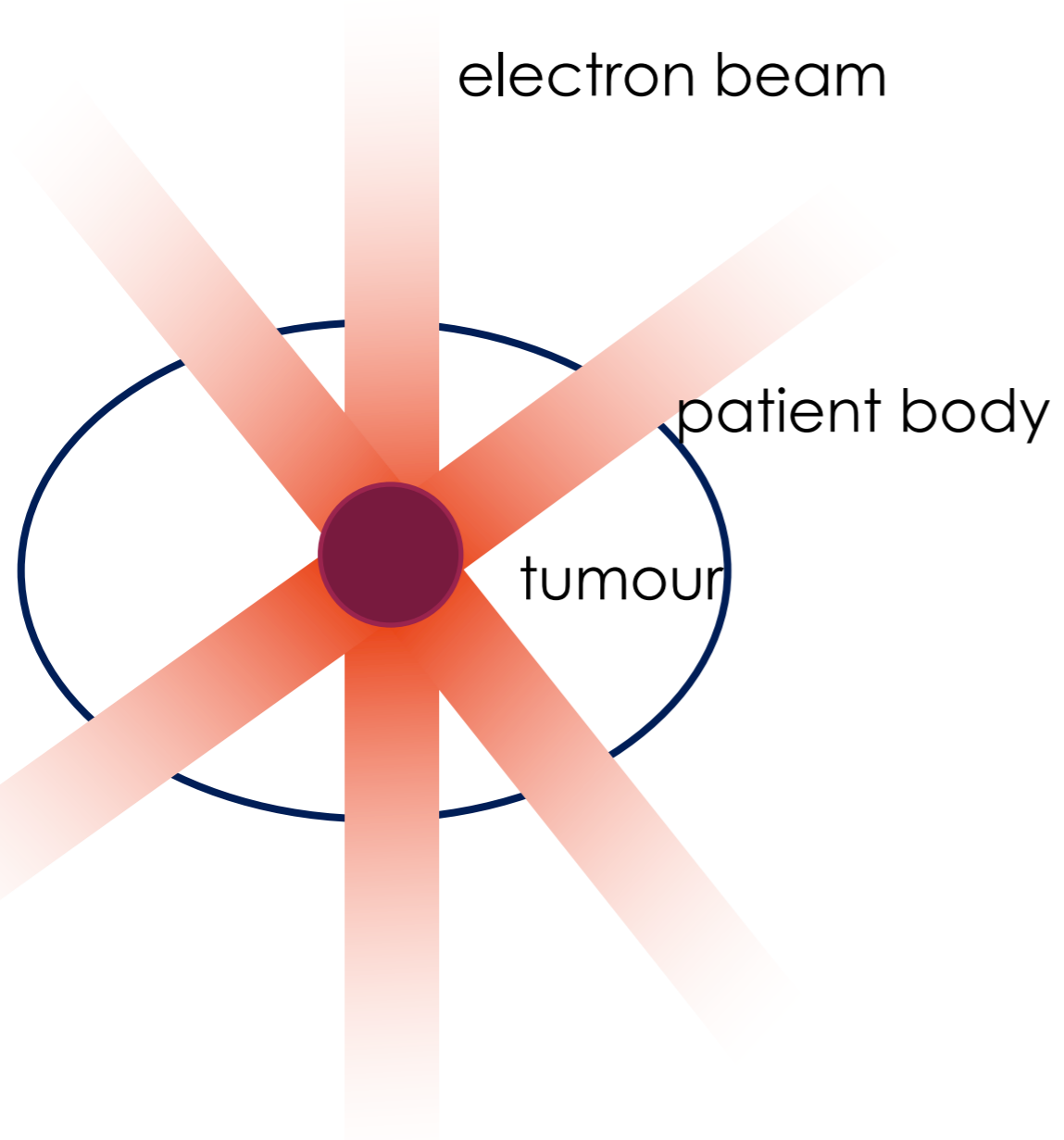
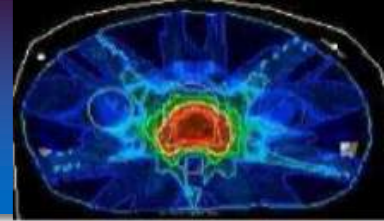
Multi-beams irradiation: a request



X-rays radiotherapy

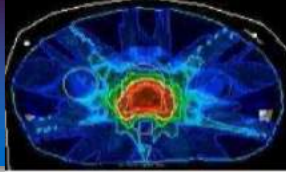


RT requires multi-fields irradiation : VHEE case

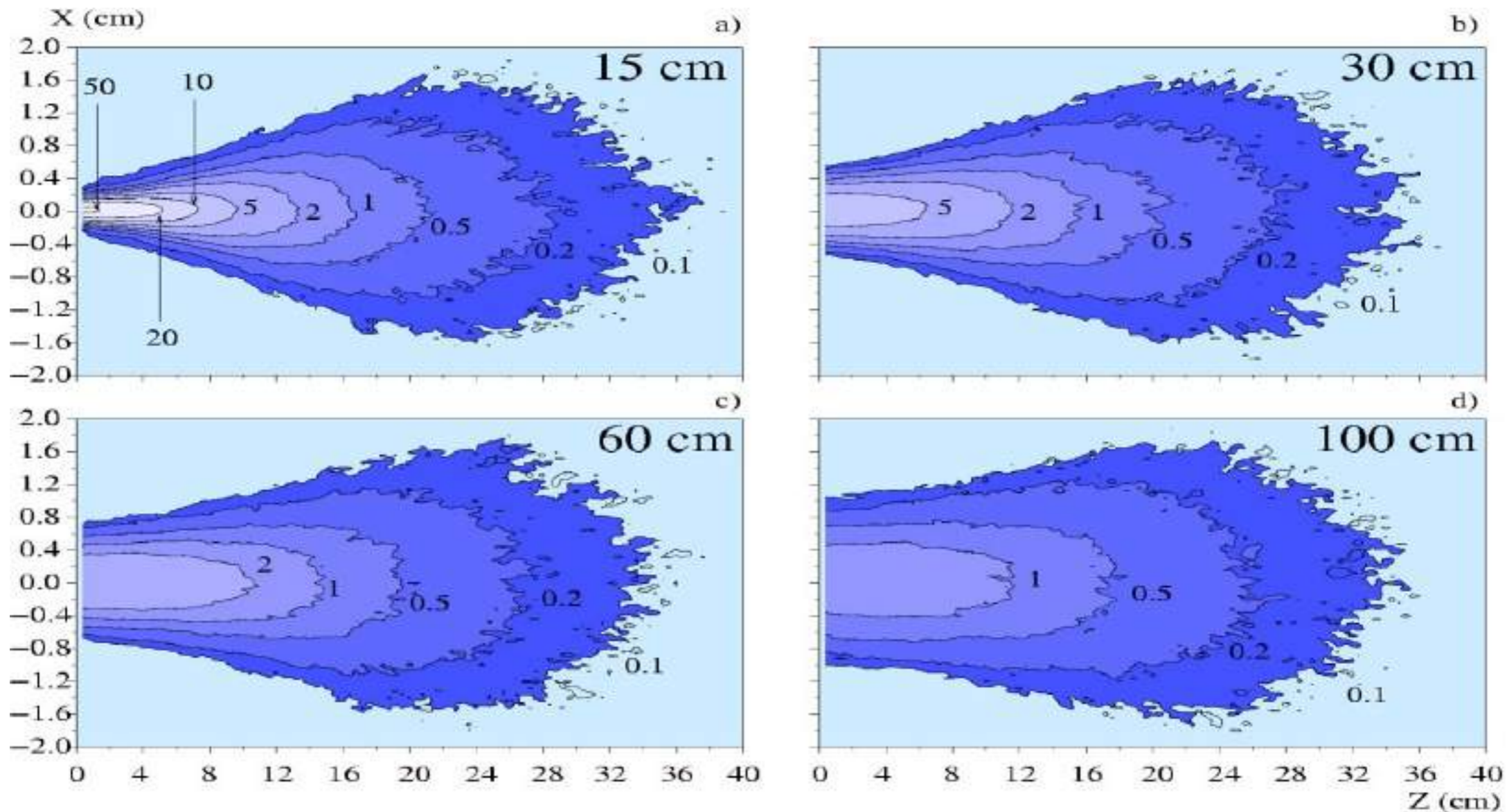


X rays machine for radiotherapy





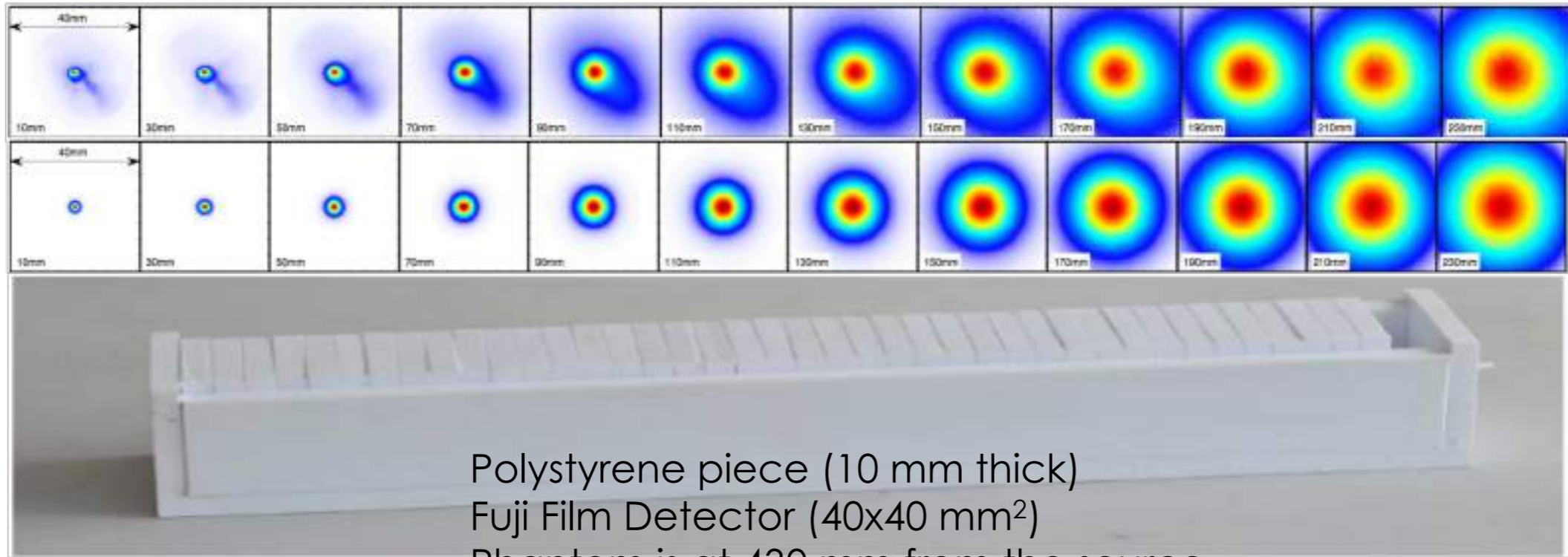
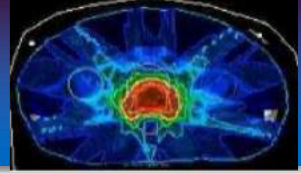
dose pencil



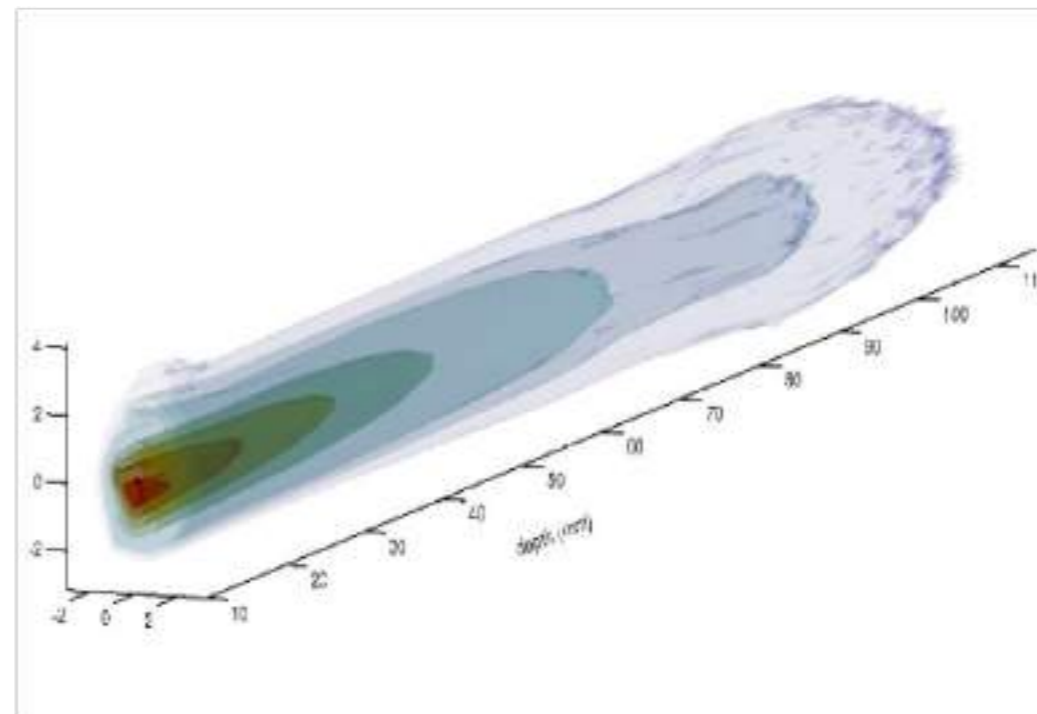
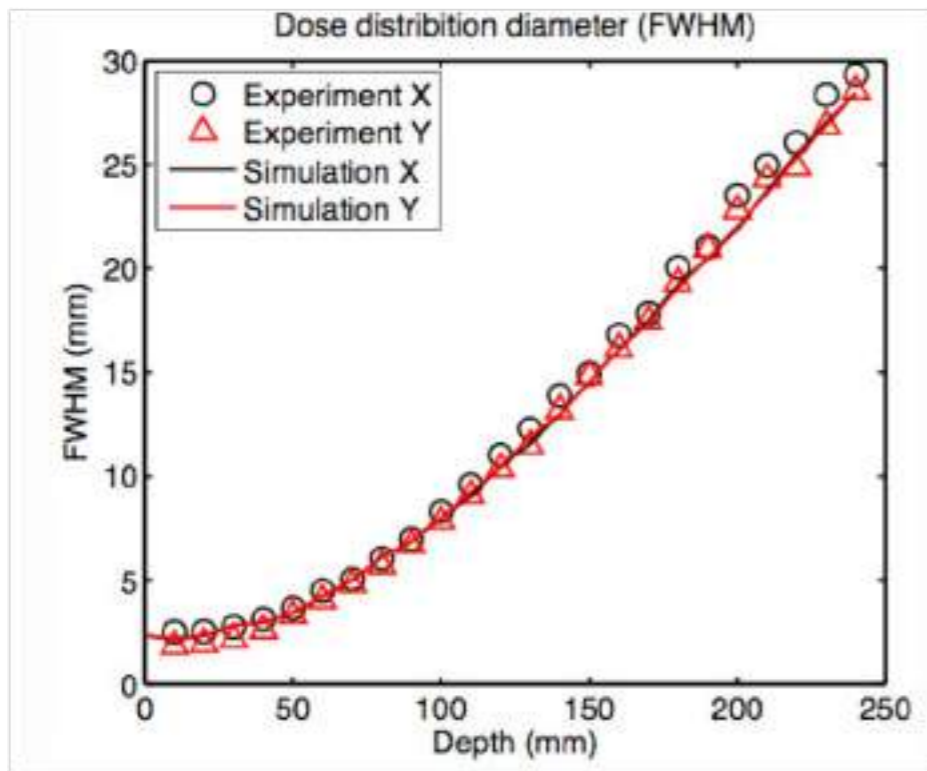
Isodose curves for different levels, 0.1, 0.2, 0.5, 1, 2, 5, 10, 20, 50 Gy/nC. The source to surface distance is a 15 cm, b 30 cm, c 60 cm, d 100 cm

Y. Glinec *et al.* *Med. Phys.* **33**, 1, 155-162 (2006), in coll. with DKFZ

Some examples of applications : radiotherapy

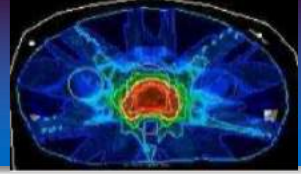


$E_{pic} = 120 \text{ MeV}$
 $\Delta E = 20 \text{ MeV}$
 $Q_{pic} = 30 \text{ pC}$
 $\Theta = 4.5 \text{ mrad}$
 $D_{max} = 1 \text{ Gy/tir}$

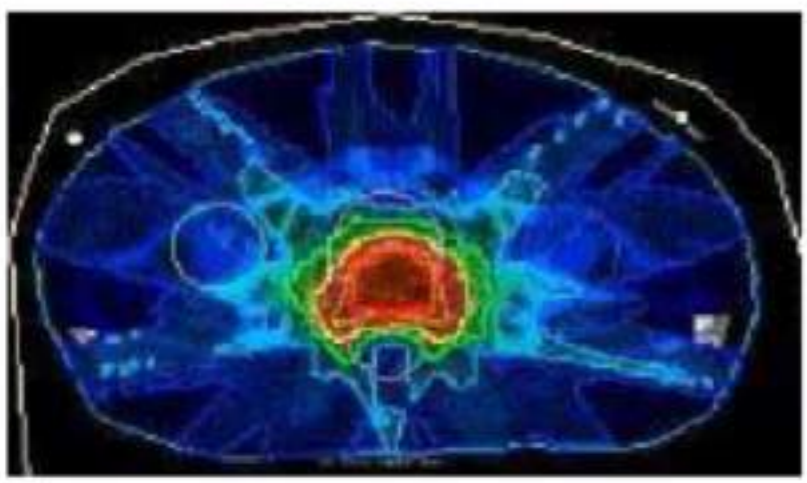
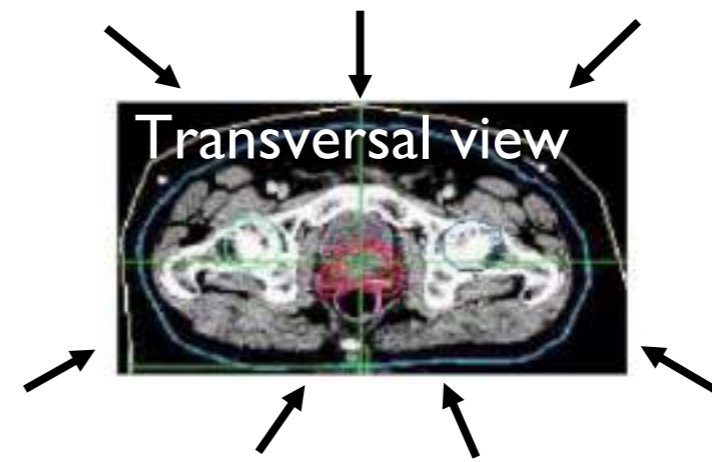


O. Lundh *et al.*, to be submitted

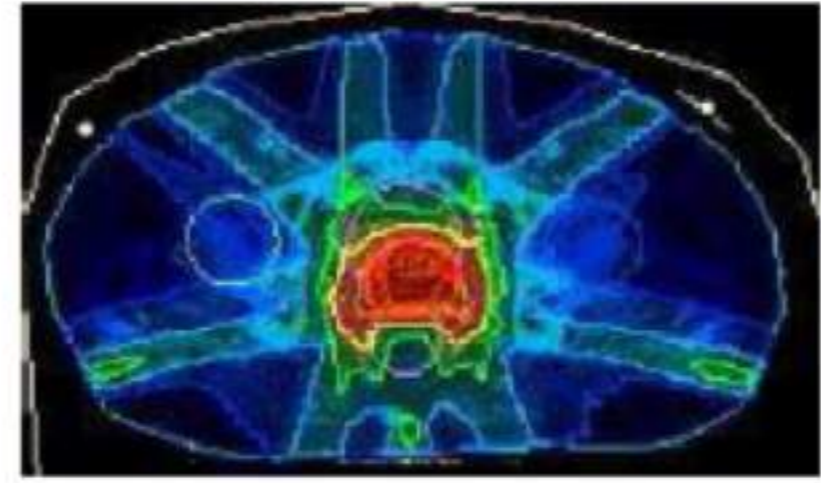
Some examples of applications : radiotherapy



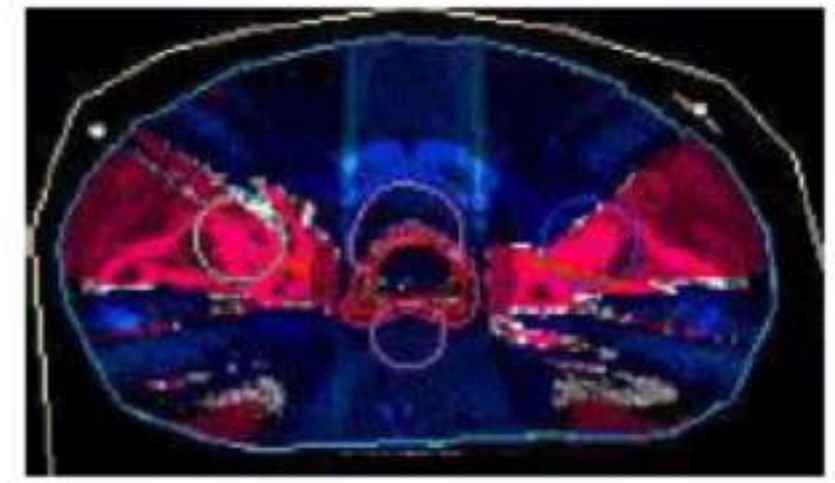
simulations of prostate cancer with 7 irradiation beams



250 MeV electrons



X rays IMRT

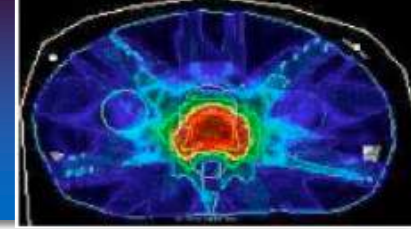


Difference

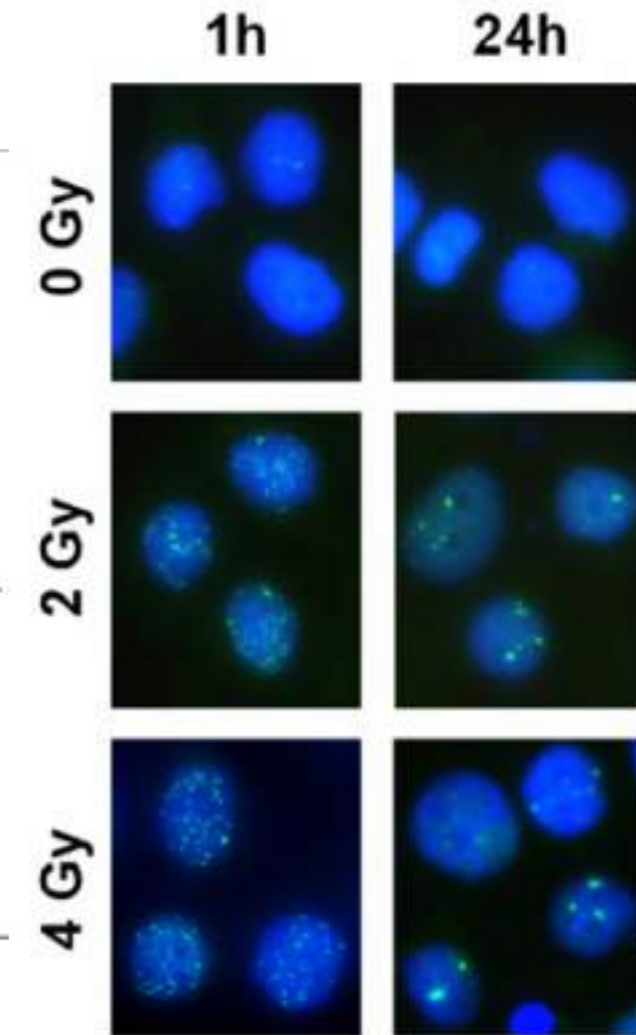
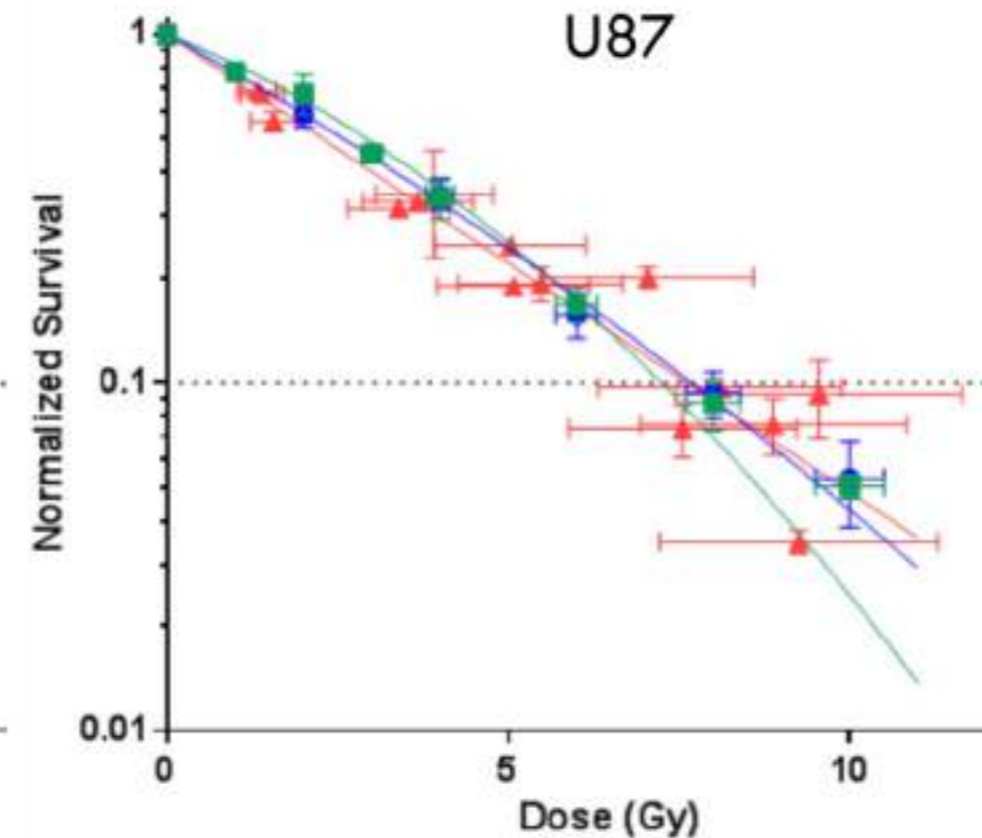
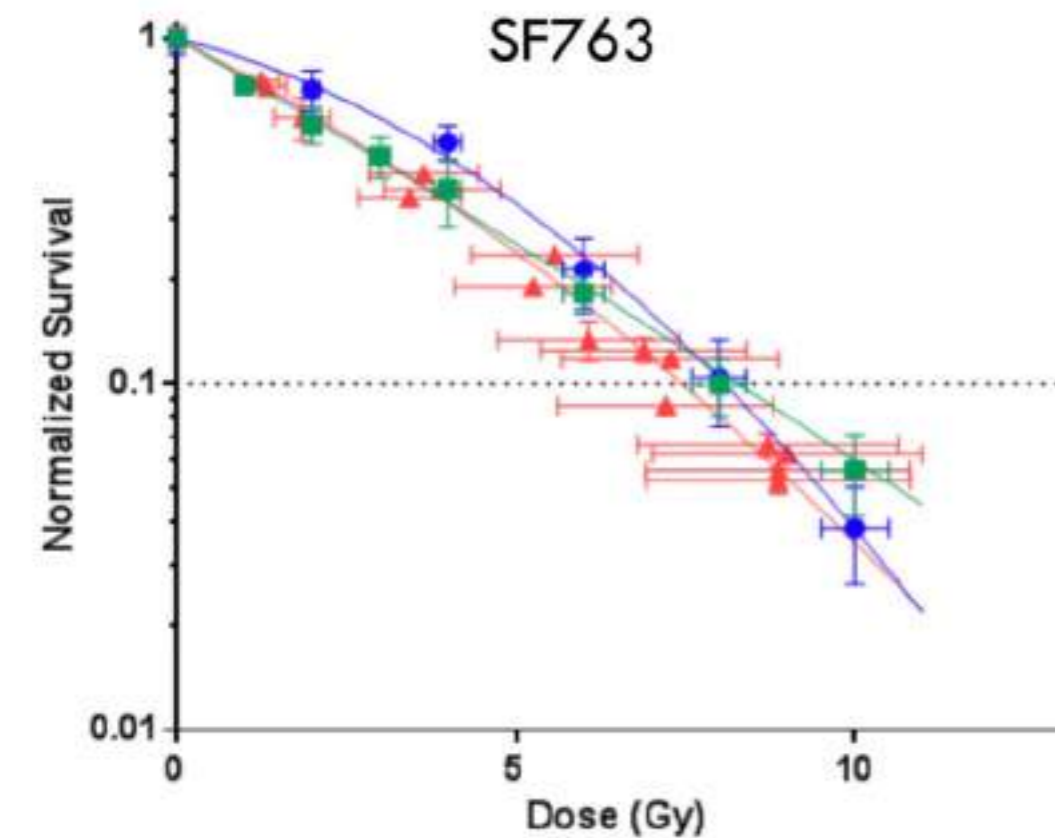
A comparison of dose deposition with 6 MeV X ray an improvement of the quality of a clinically approved prostate treatment plan. While the target coverage is the same or even slightly better for 250 MeV electrons compared to photons the dose sparing of sensitive structures is improved (up to 19%).

T. Fuchs *et al.* Phys. Med. Biol. **54**, 3315-3328 (2009)

No difference in DNA damage foci irradiated by p-Laser, p-Conv, and X rays

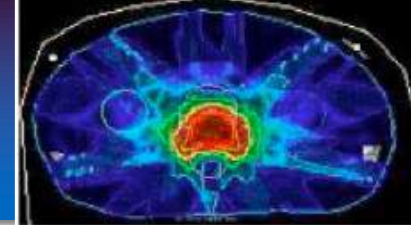


Average dose rate : 2.1 Gy/min ($\Delta t = 20$ s)

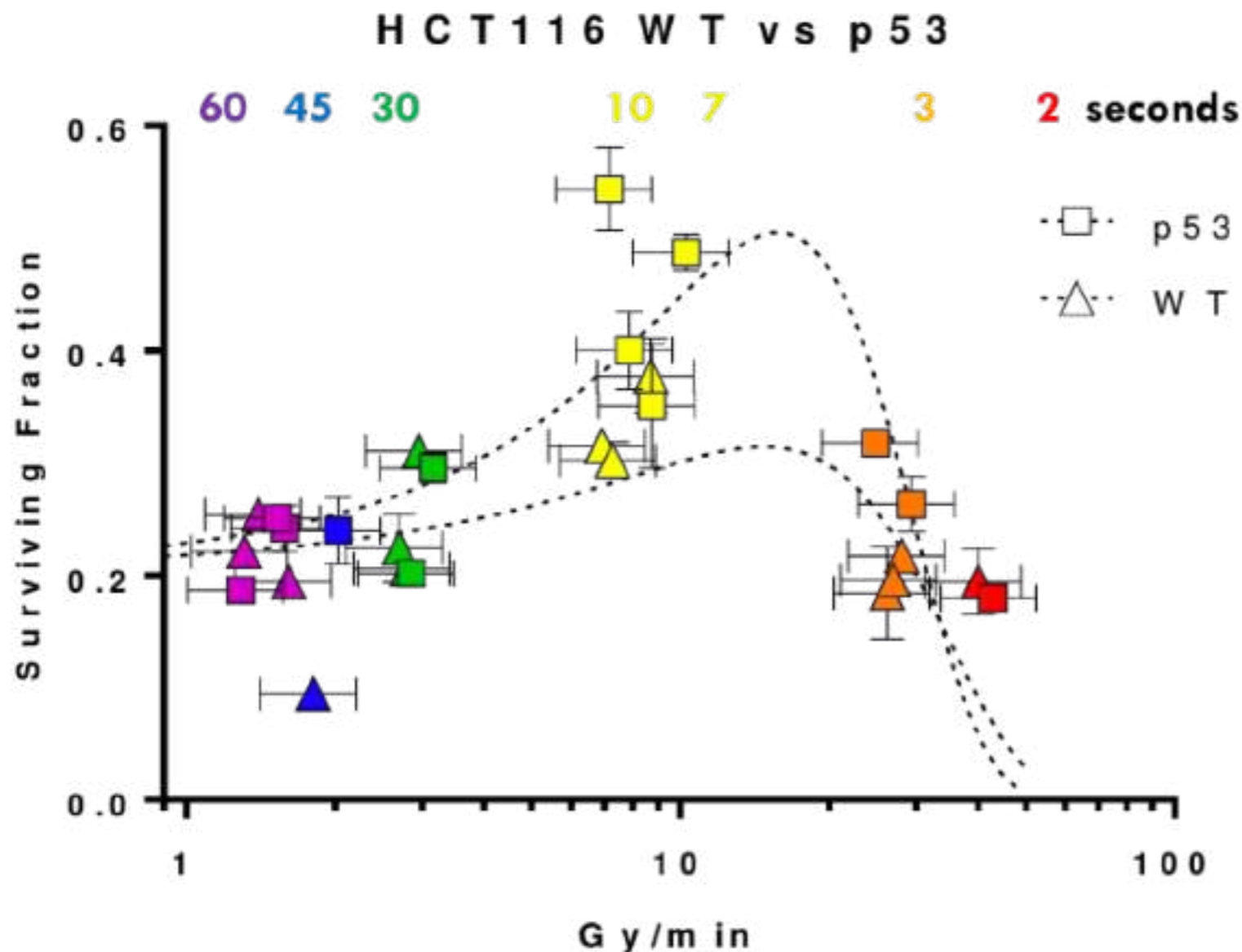


Dose responses of DNA damage foci formation and of cell survival. (A) Representative immune-fluorescent images of cells obtained 1h and 24h after exposure to the indicated doses of laser driven protons (LDP, dotted square), conventional accelerated protons (CAP, triangles) and X-rays (x cross). The negative controls (0 Gy) were sham-irradiated

Fast Fractionation effects



radiosensitive colorectal cancer cells HCT116WT and
Its radioresistant counterpart HCT116 p53^{-/-}p53

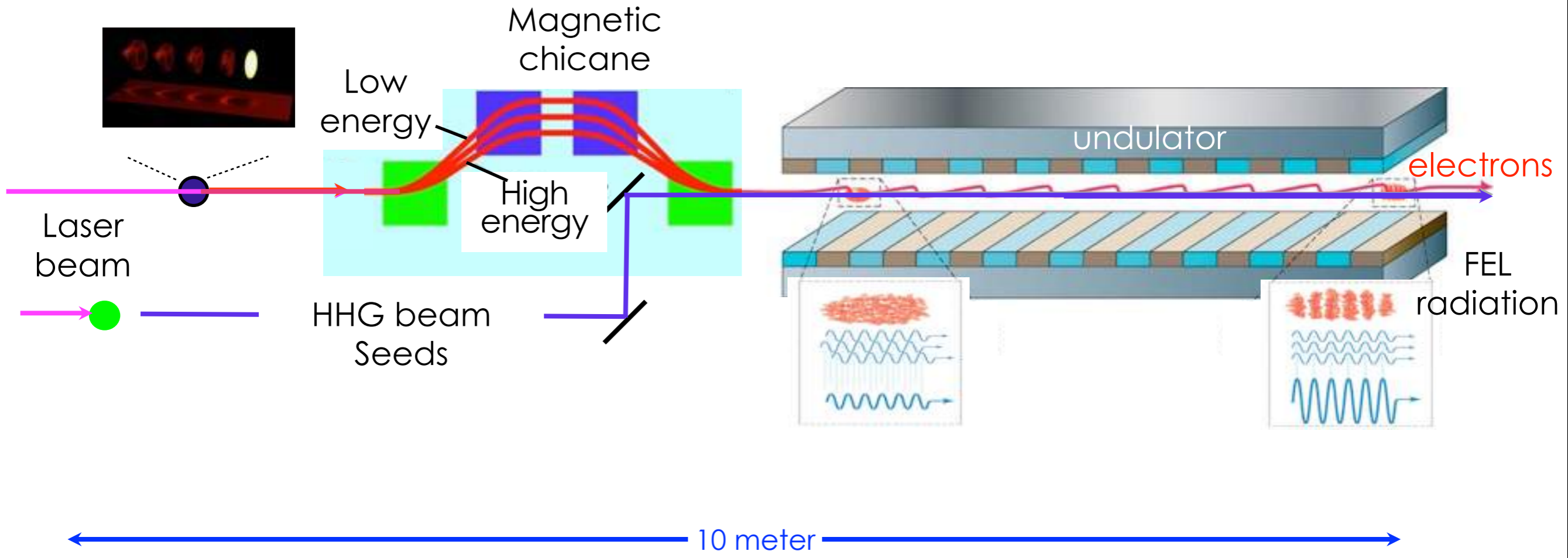
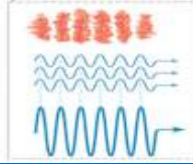


*Cell lines were exposed to a fixed number of LDP bunches with a variable delay between shots, from 60 to 2 seconds.

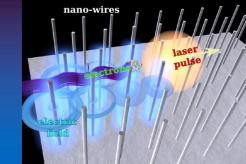
*Hence the total irradiation time varied from 15 to 540 seconds, which changes the overall "average" dose rate.

E. Bayart et al., Scientific Reports, s41598 (2019)

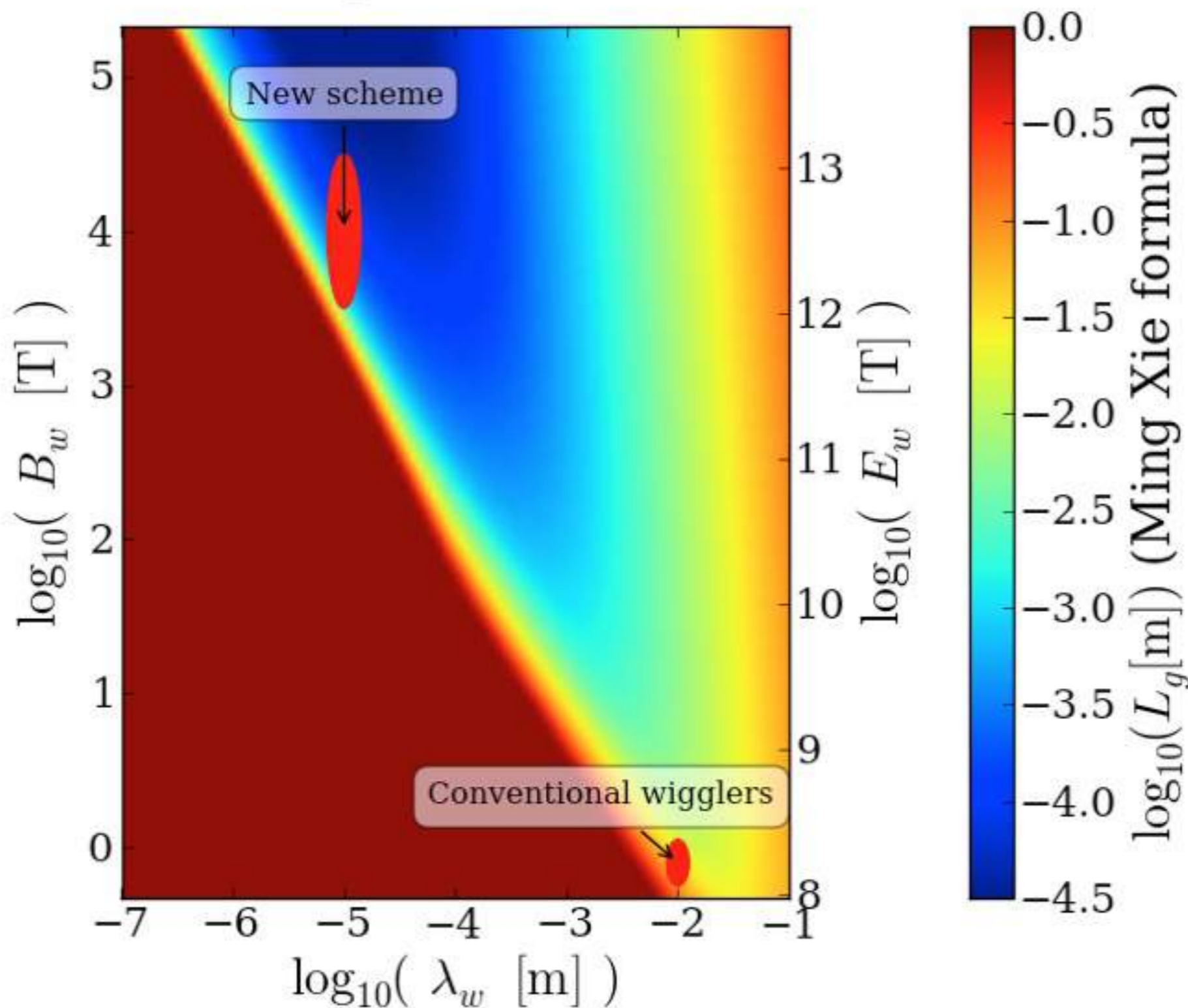
FEL experiment on Seeding mode with LPA



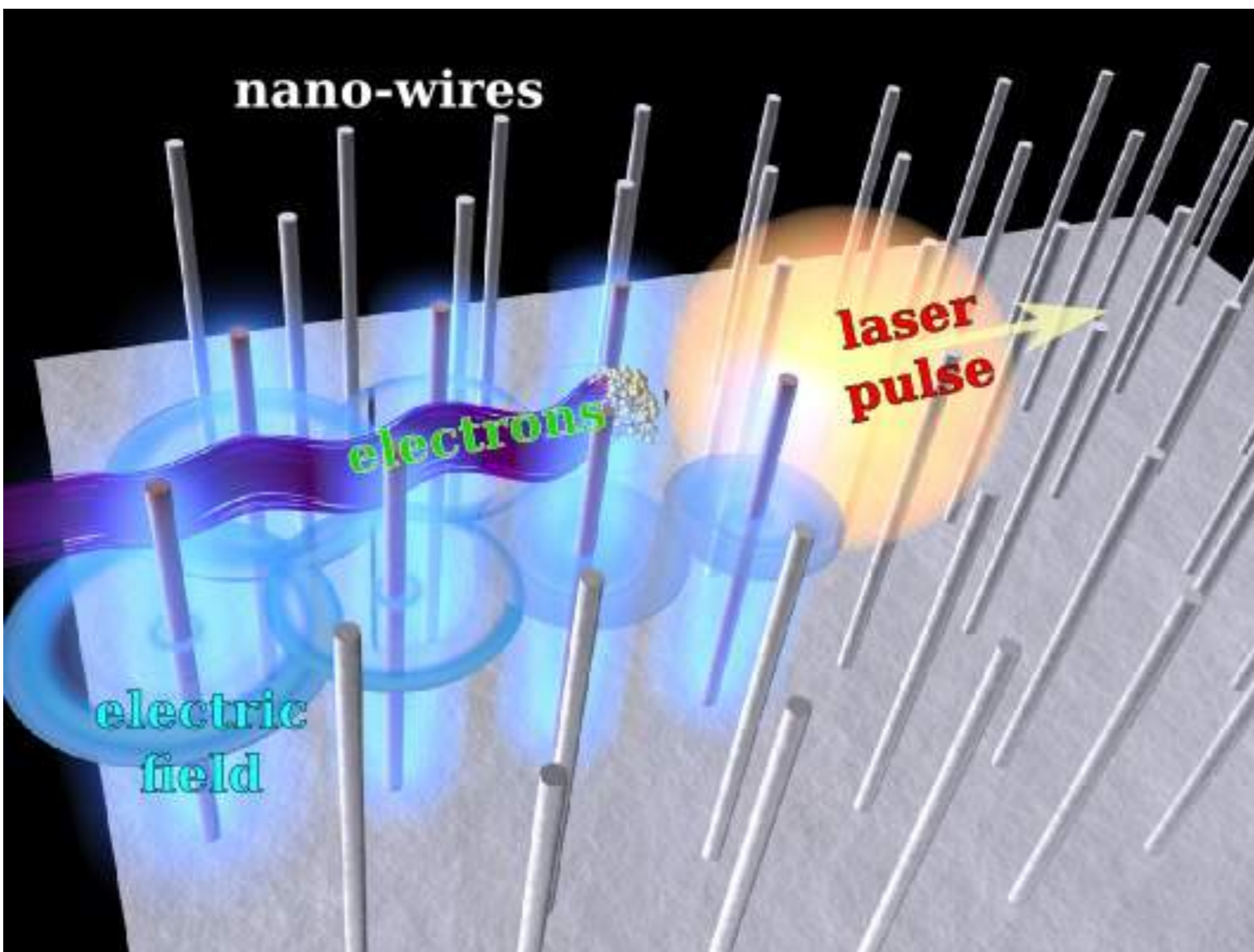
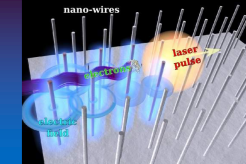
in collaboration with Marie Emmanuelle



Gain length of the FEL at 200 MeV



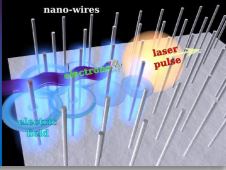
Concept for ultra compact X rays beam



I. Andriyash *et al.*, Nat. Communications, 5736 (2014)



Undulating with plasma fields



Varying electron energy

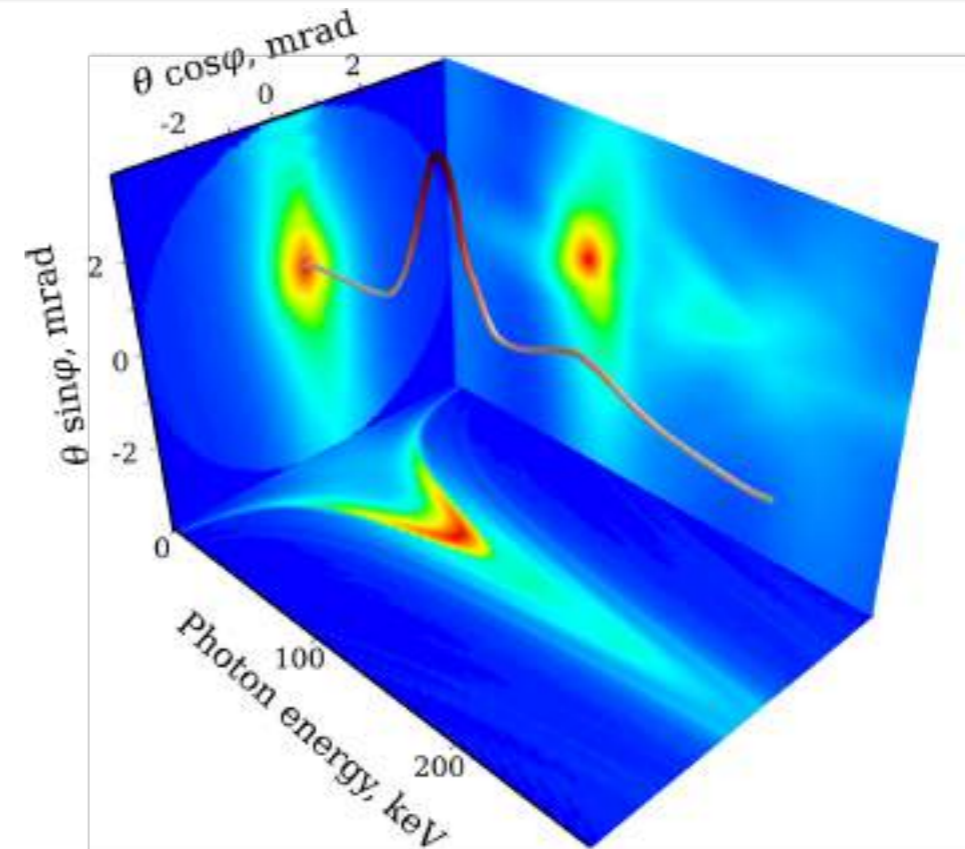
Energy 200 / 400 / 600 MeV

Undulator emission

Photon energy 12 / 47 / 106 keV

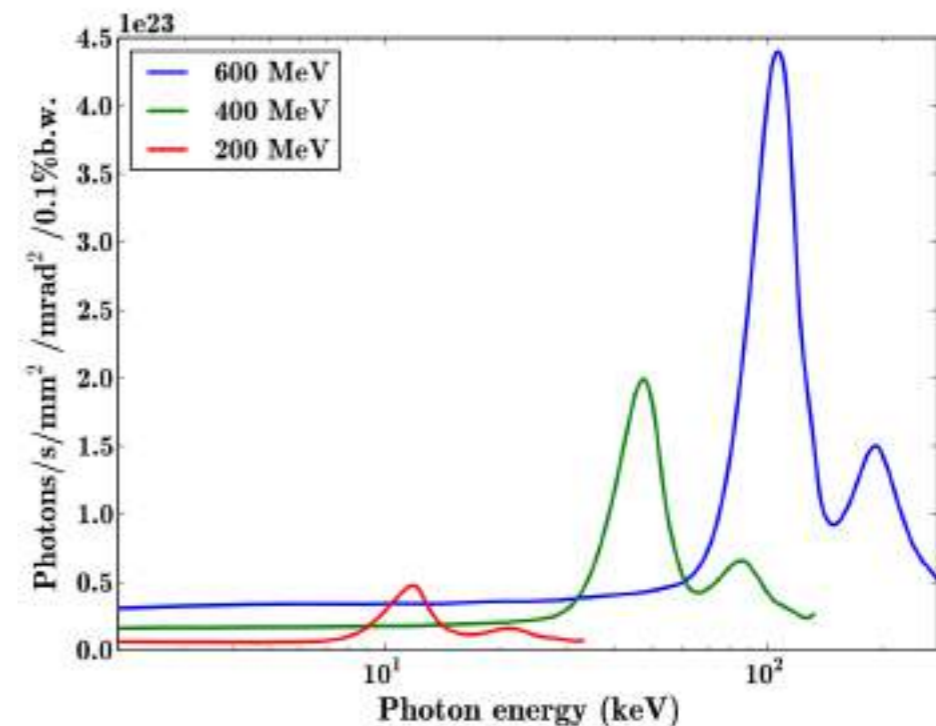
Brightness 0.5 / 2 / 4.5×10^{23} s.u.

Angular sizes 0.85×1.7 mrad

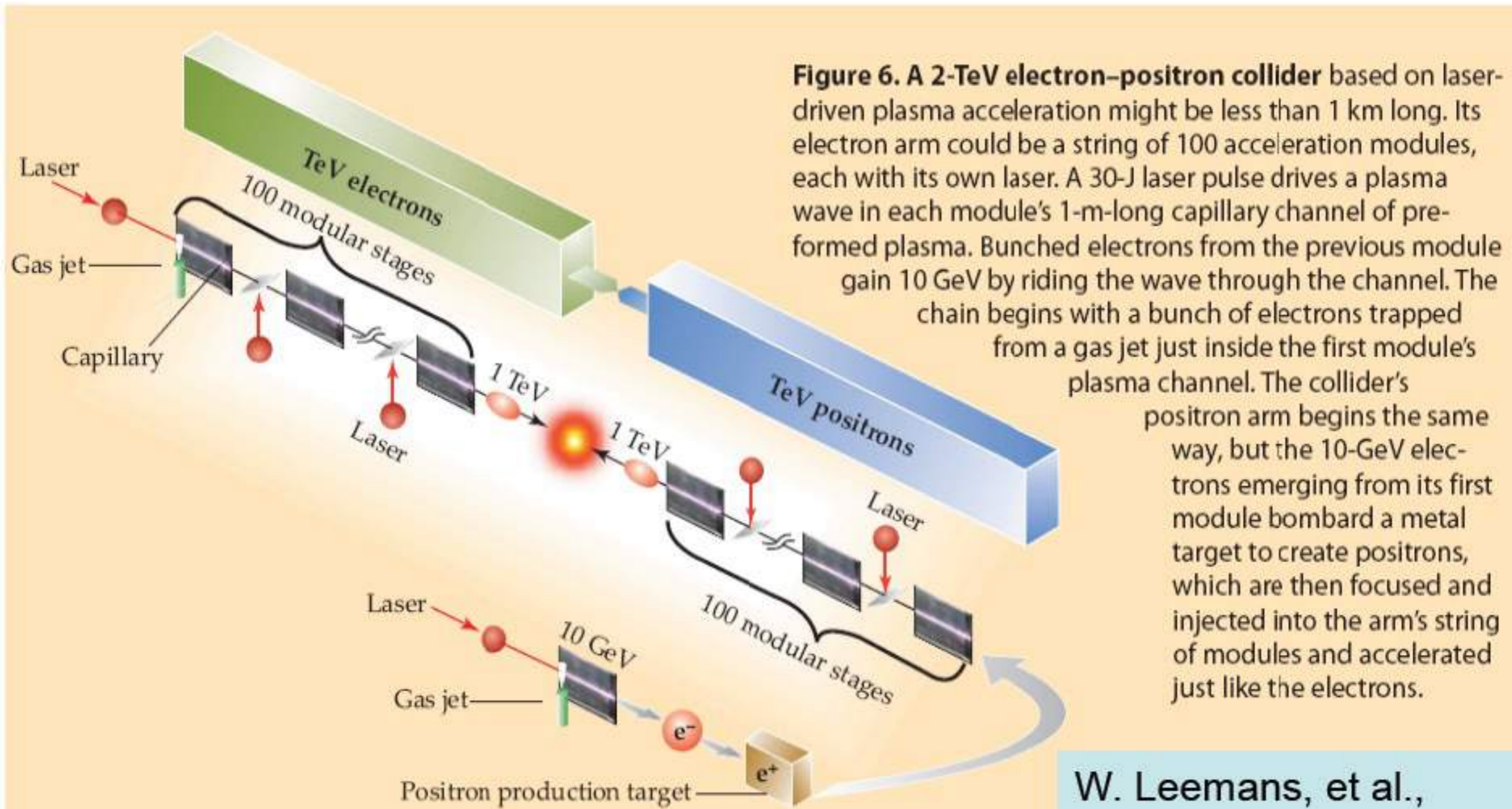


Laser plasma nanostructured SR source

- Quasi-monoenergetic collimated spectrum
- Tunability λ_u, ϵ_e
- Brightness $\sim \gamma_b^2$
- Source brightness level 10^{23} s.u.
- Interaction length $\lesssim 1$ mm

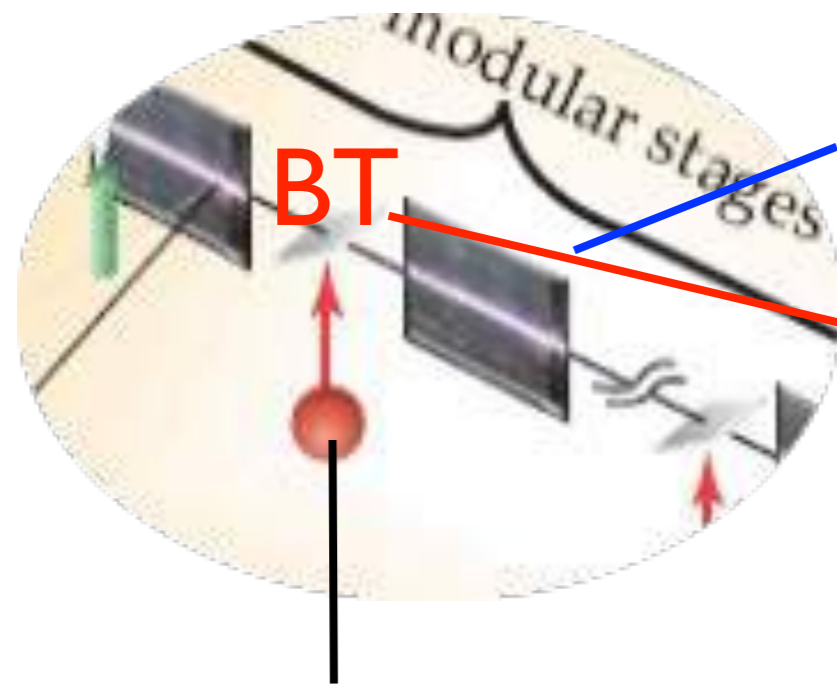


Laser-Driven Plasma Linac: «Artistic view»



W. Leemans et al., Phys. Today, March 2009

Concept of Laser-Driven Plasma Linac: Challenge



plasma accelerator
stage 0.1 to 1m, $\eta = 1\%$

Beam transport :
1, 10 m to up to few
km in the last stages
 $\eta = ? \%$

laser : 10x50 m + focal of 5-10 m, $\eta = \text{few } \%$

overall wall-plug efficiency: $10^{-3}, 10^{-4}$, i.e. for a 1 MW e, e⁺
beam, required power of 1-10 GW

100 of kHz-PW Laser reliability, plasma discharge, reliability, etc..

V. Malka Phys. of Plasma 19, 055501 (2012)



1 PW laser at high rep rate ($>100\text{Hz}$): today in the best 1 Hz

Plasma and vacuum chambers

Transport between stages

Thermal effects on the guiding structure wall

External guiding/self-guiding

Collimation and beam filtering

Accelerating plasma structure: linear ($<1\text{GV/m}$) or non-linear ($>\text{few GV/m}$ to 100s GV/m)

High efficiency laser driver : today in the best 1%

Laser Plasma Accelerators : Outline

- Introduction : context and motivations
- Colliding laser pulses scheme
- Injection in a density gradient
- Manipulating the longitudinal momentum
- Manipulating the transverse momentum
- Applications
- Conclusion and perspectives



Accelerators point of view :

- Good beam quality & Monoenergetic dE/E down to 1 % ✓
- Beam is very stable ✓
- Energy is tunable: up to 400 MeV ✓
- Charge is tunable: 1 to tens of pC ✓
- Energy spread is tunable: 1 to 10 % ✓
- Ultra short e-bunch : 1,5 fs rms ✓
- Low divergence : 2 mrad ✓
- Low emittance¹⁻³ : $< \pi$.mm.mrad ✓
- With PW class laser : peak energy at 4.5 GeV ✓

¹S. Fritzler *et al.*, Phys. Rev. Lett. **92**, 165006 (2004), ²C. M. S. Sears *et al.*, PRSTAB **13**, 092803 (2010), ³E. Brunetti *et al.*, Phys. Rev. Lett. **105**, 215007 (2010)

Results extremely important for :

Designing future accelerators

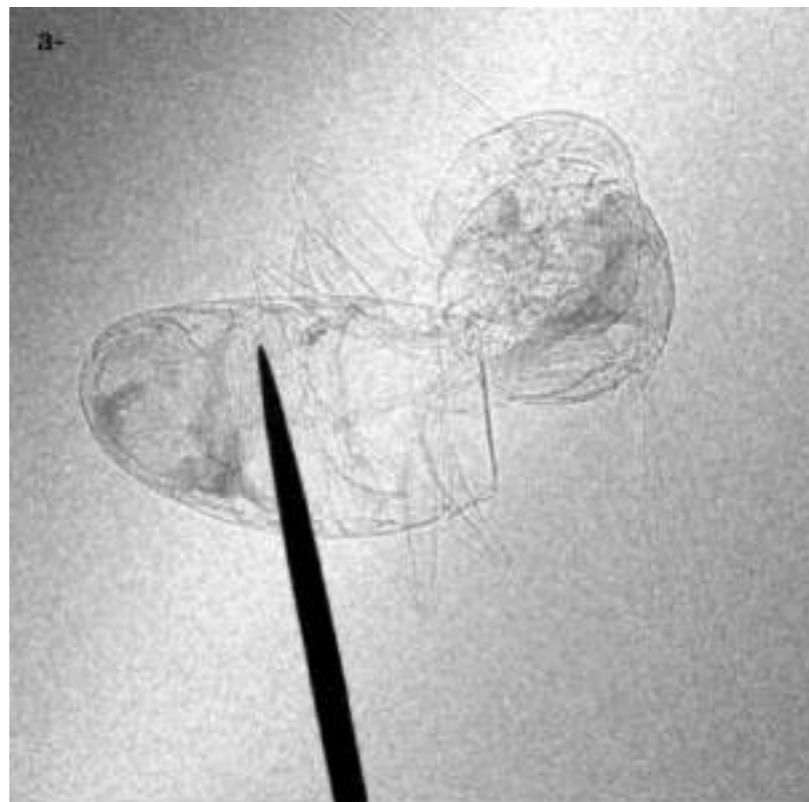
Compact X ray source (Thomson, Compton, Betatron, or FEL)

Applications (chemistry, radiotherapy, medicine, material science, ultrafast phenomena studies, etc..)

First X rays betatron contrast images

S. Fourmaux *et al.*,
Opt. Lett. **36**, 13 (2011)

S. Kneip *et al.*, APL **99**,
093701 (2011)



Courtesy of K. Krushelnick

V. Malka *et al.*, Nature Physics **4** (2008), E. Esarey *et al.*, Rev. Mod. Phys. **81**, 1229 (2009)



Short term perspective (< 10 years):

Relevant applications in medicine, radiobiology, material science

Compact FEL with moderate average power (10 Hz system)

Compact X ray source (Thomson, Compton, Betatron, or FEL)

Long term possible applications (>40-50 years):

High energy physics that will depend on the laser technology evolution, on laser to electron transfer efficiency, on progress of multistage design, acceleration of positron, etc...)

Conclusion & perspectives



By improving the control of the electron motion with intense lasers one can shape the electric field and manipulate the beam properties in the phase space.

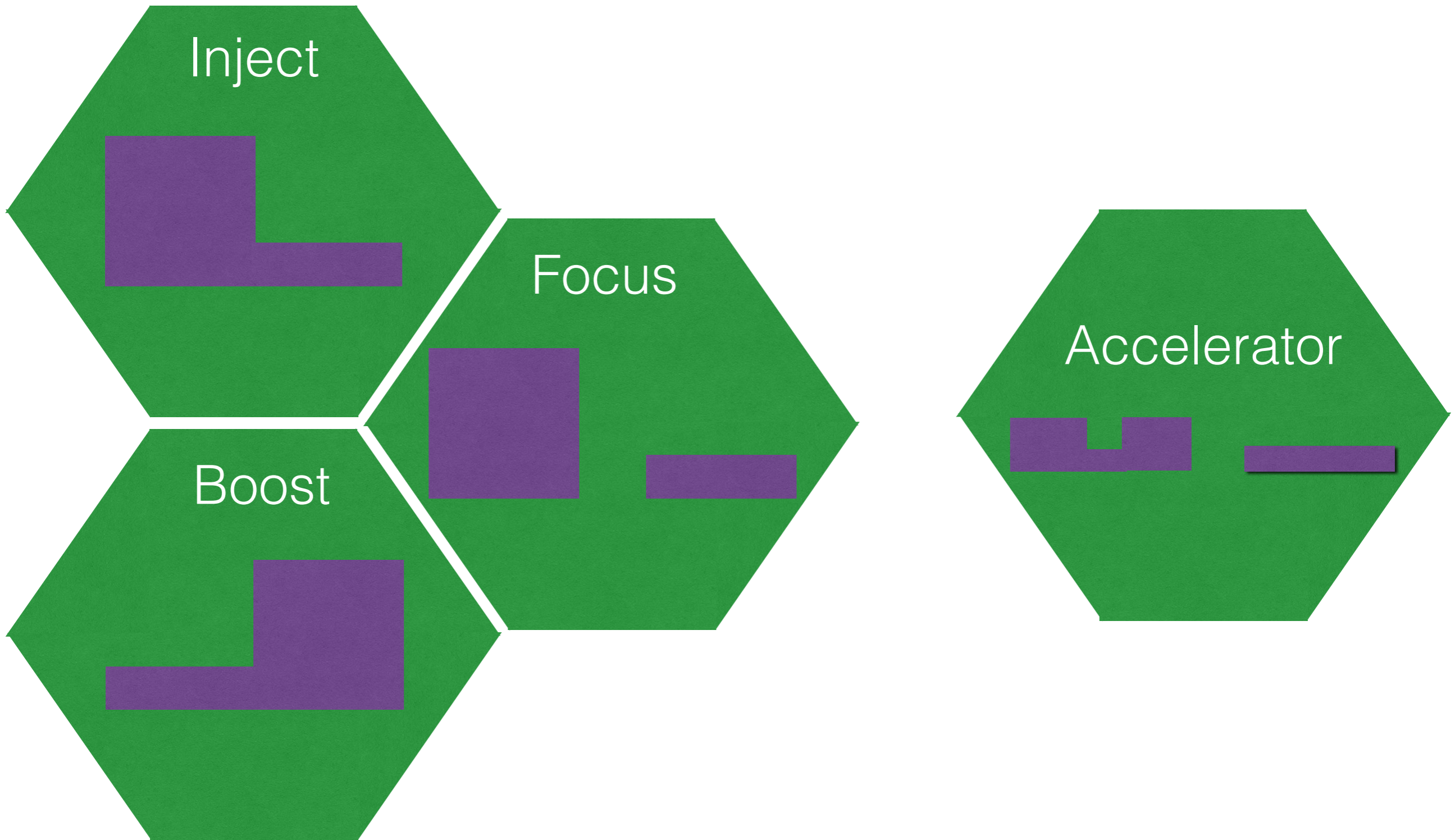
As a consequence, Laser Plasma Accelerators have made significant progresses delivering stable, reliable high quality and high current e-beams.

Applications in medicine (radiotherapy, cancer imaging, security) are almost here.

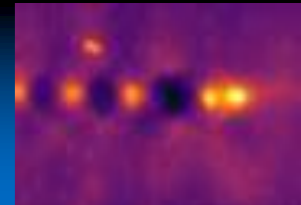
Compact FEL based on LWFA is one very important challenge that has been identified by the community.

V. Malka et al., Nature Physics **4** (2008), *V. Malka Phys. of Plasma* 19, 055501 (2012)
E. Esarey et al., Rev. Mod. Phys. **81** (2009), *S. Corde et al., Rev. Mod. Phys.* **85** (2013)

Simple plasma devices produced with a single laser pulse

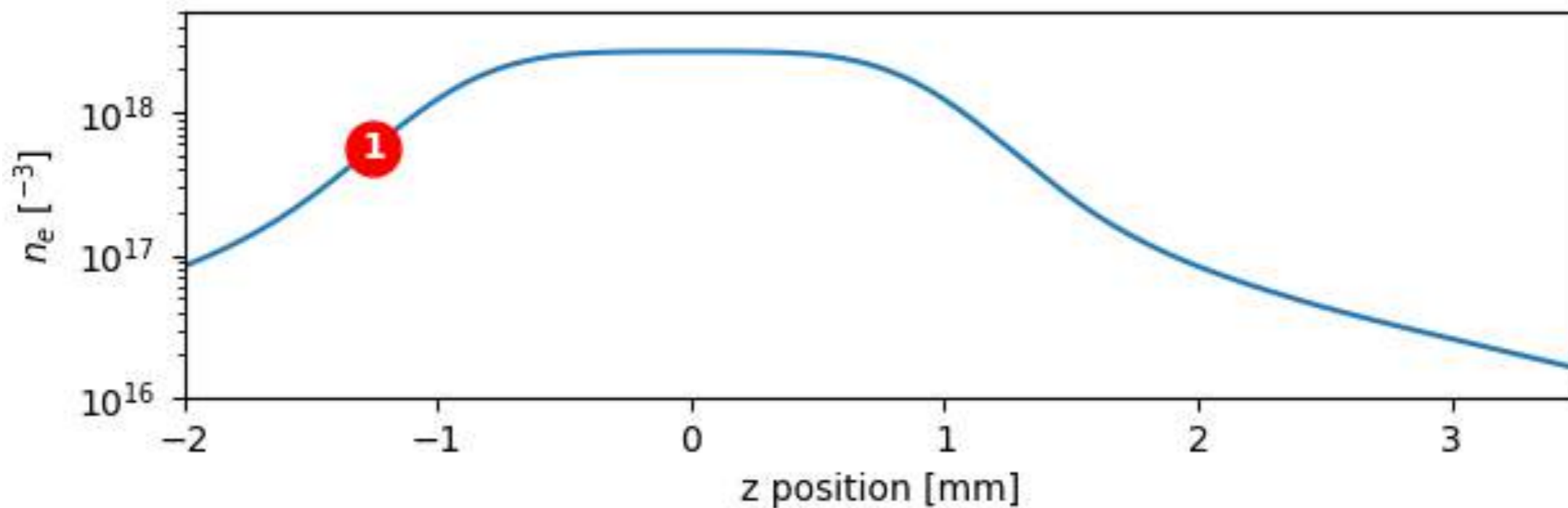
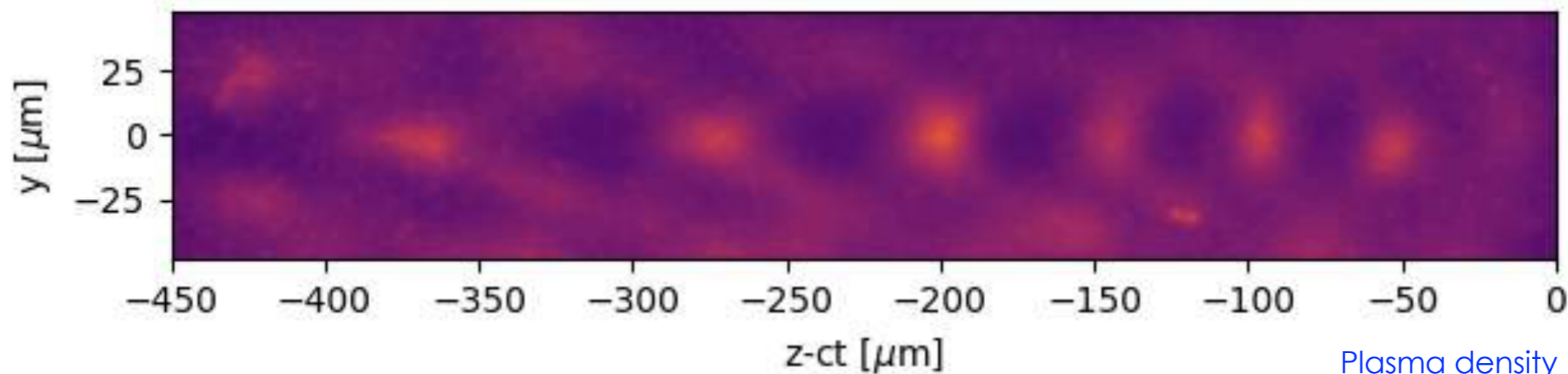


Visualization of the wakefield dynamics

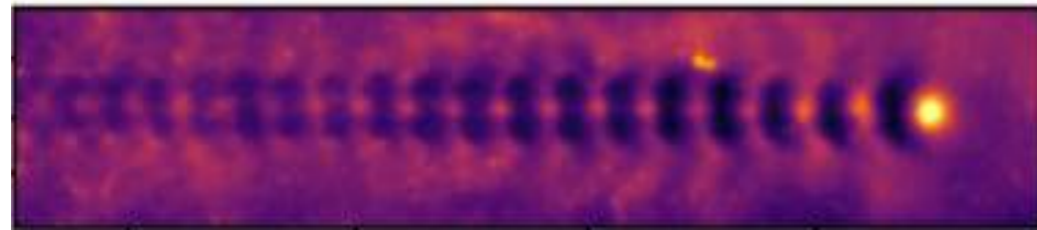
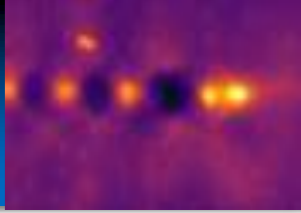


Jet 2: He (1% N₂), plasma density $2.8 \times 10^{18} \text{ cm}^{-3}$
Laser B: on-target energy $\sim 1 \text{ J}$, linearly polarized (horizontal)

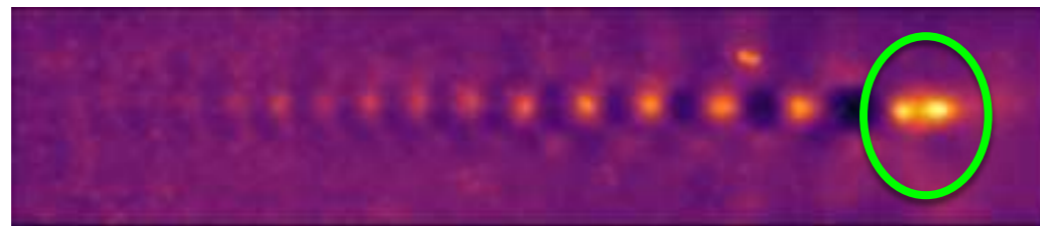
Exp. Probe image



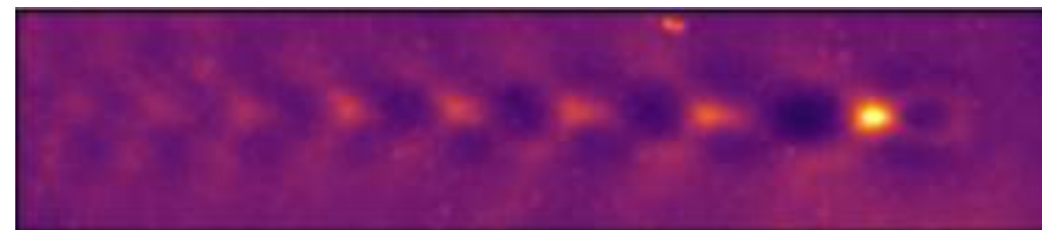
Transition from the laser to the plasma wakefield



Pure LWF



Electron injection in LWF

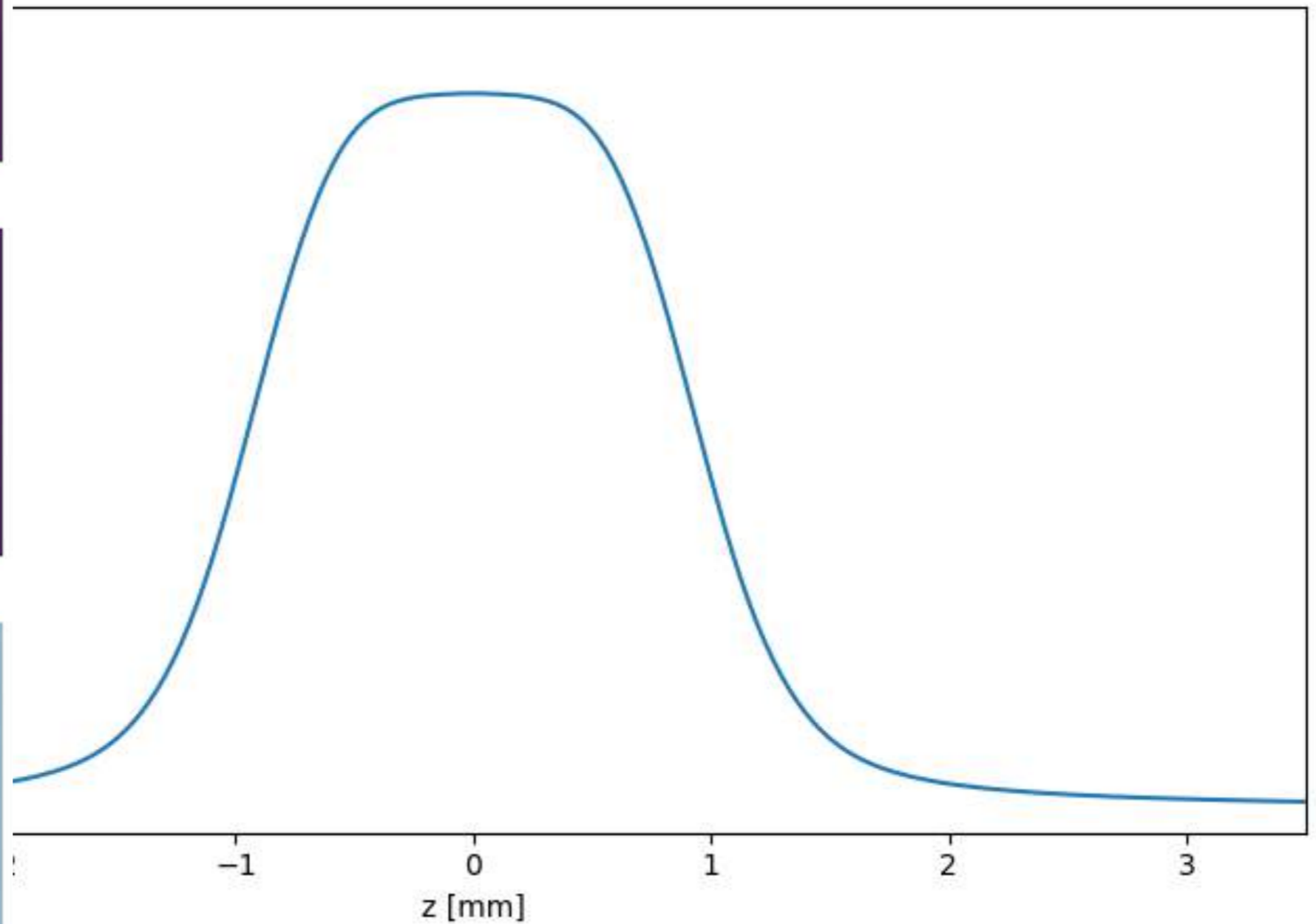
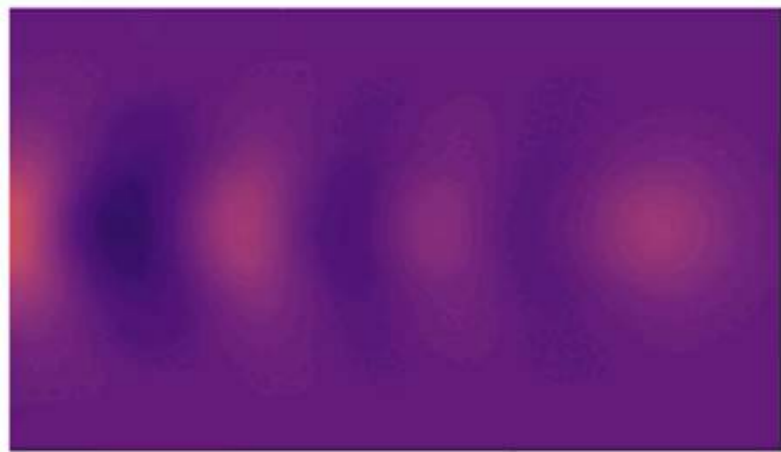
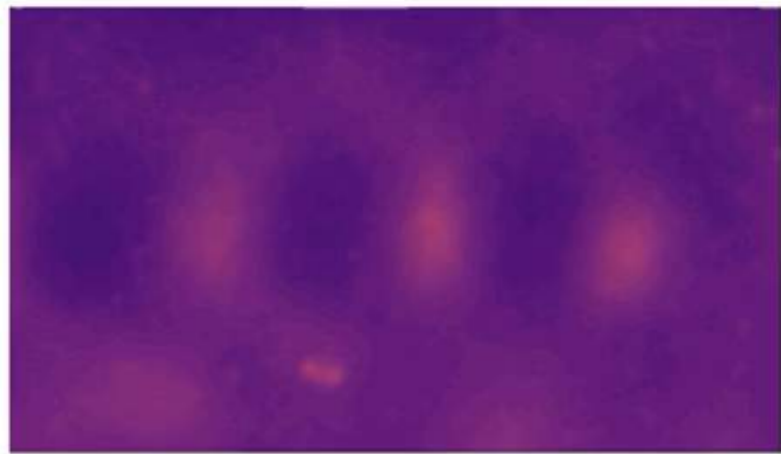
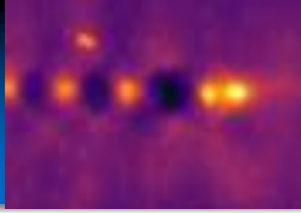


Mixed PWF and LWF

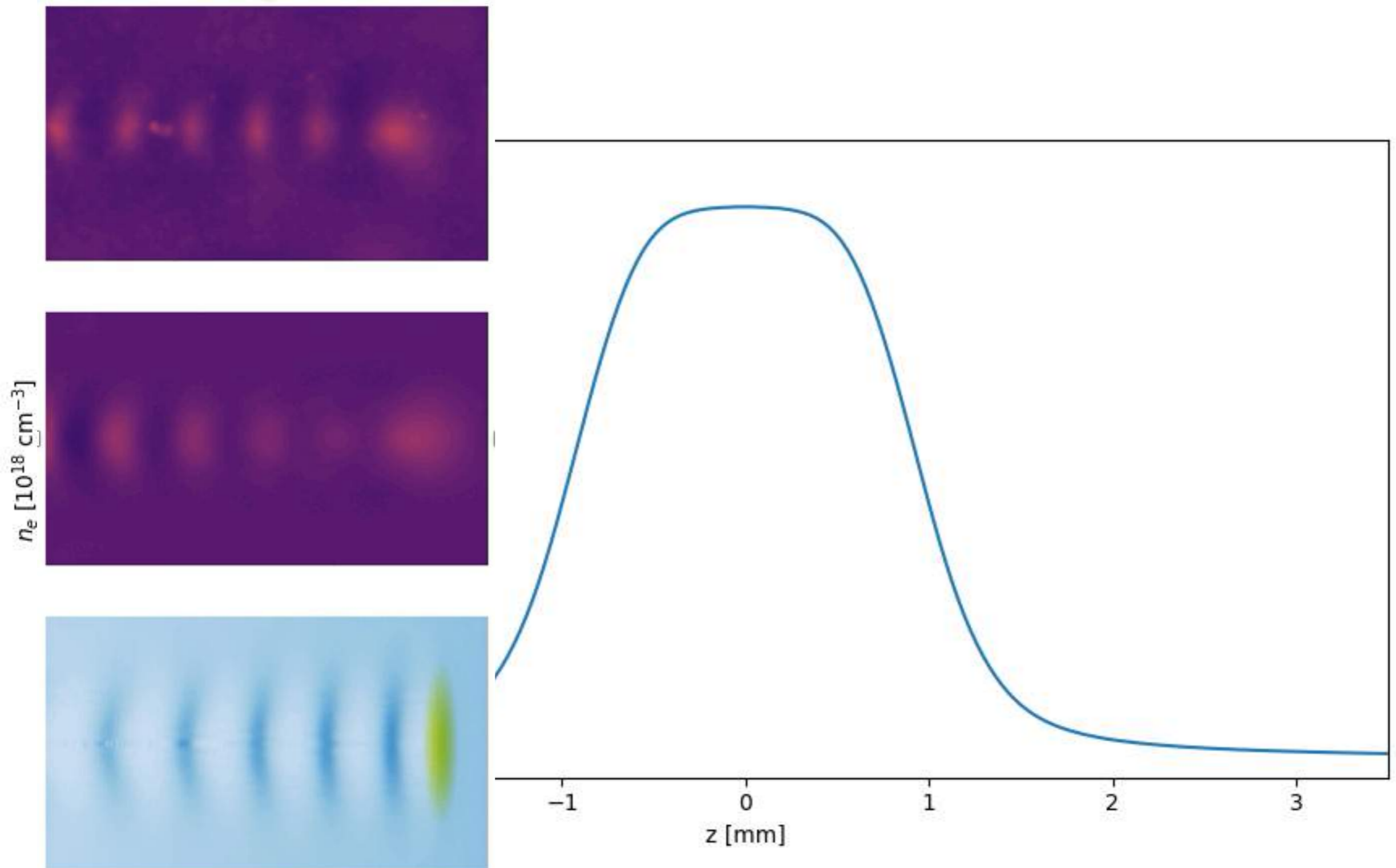
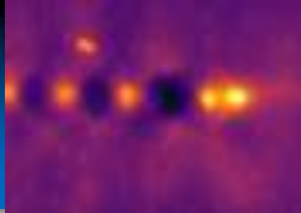


Pure PWF

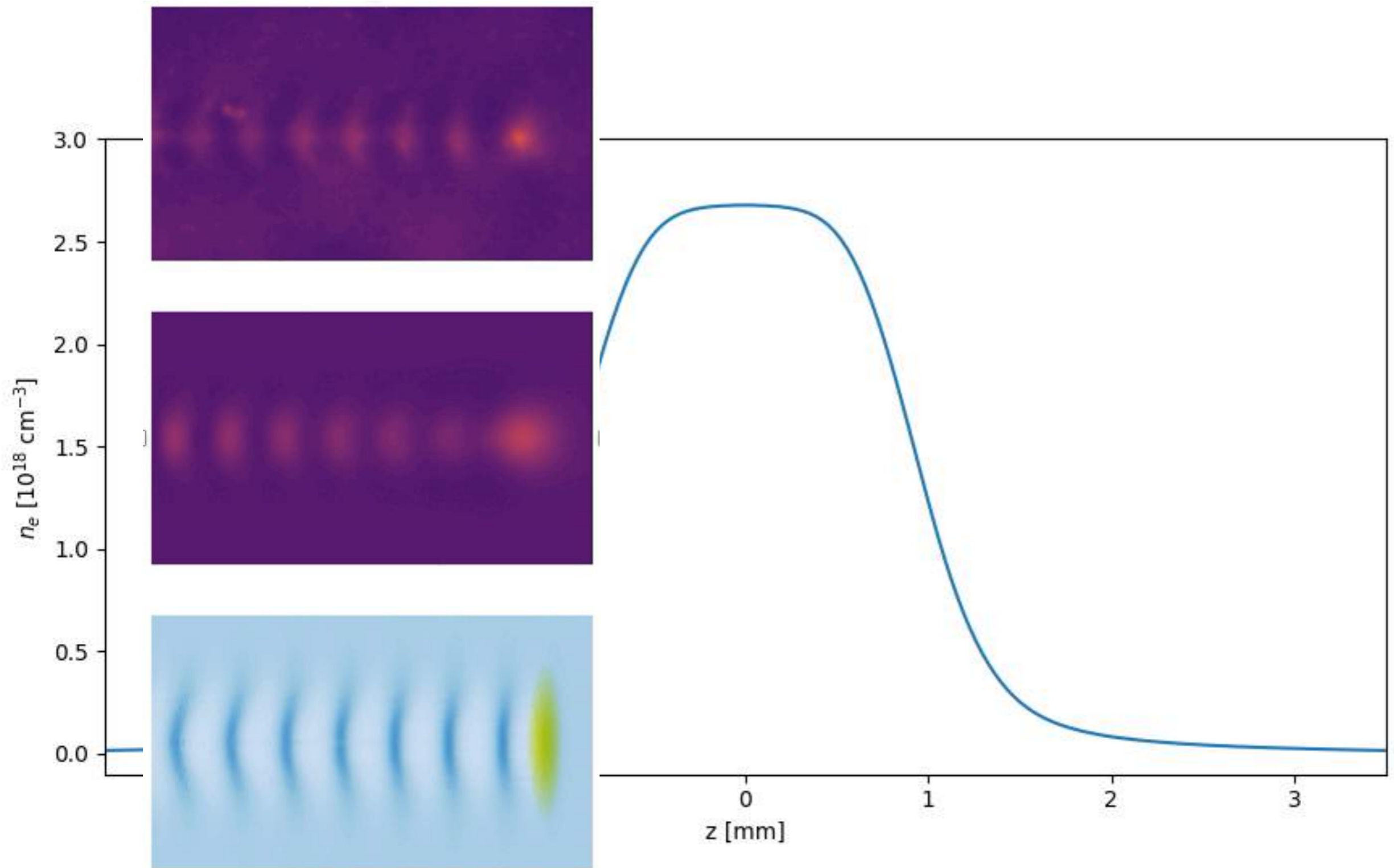
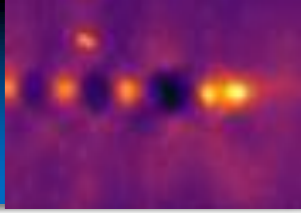
Transition from the laser to the plasma wakefield



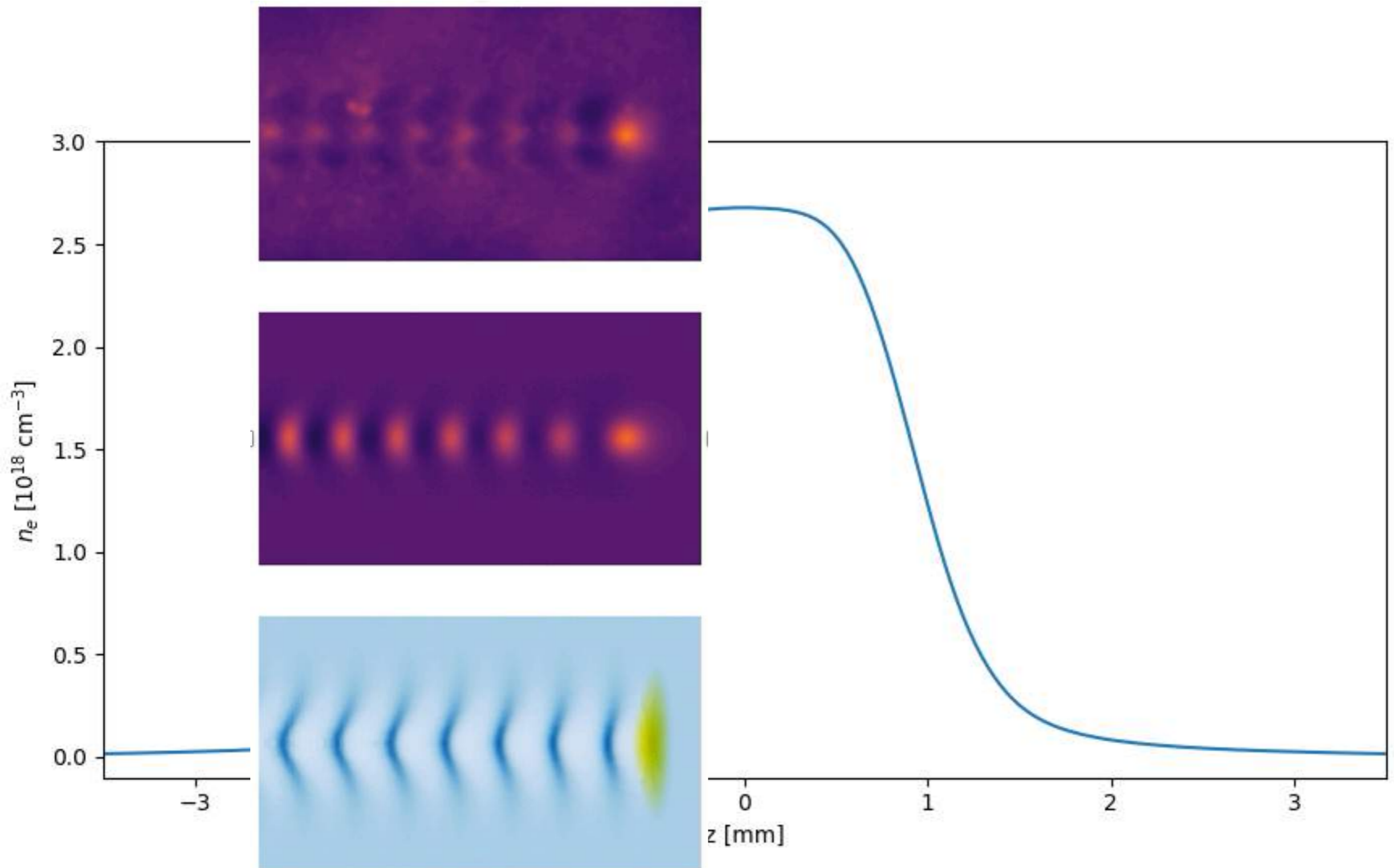
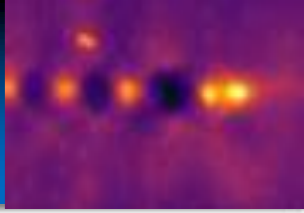
Transition from the laser to the plasma wakefield



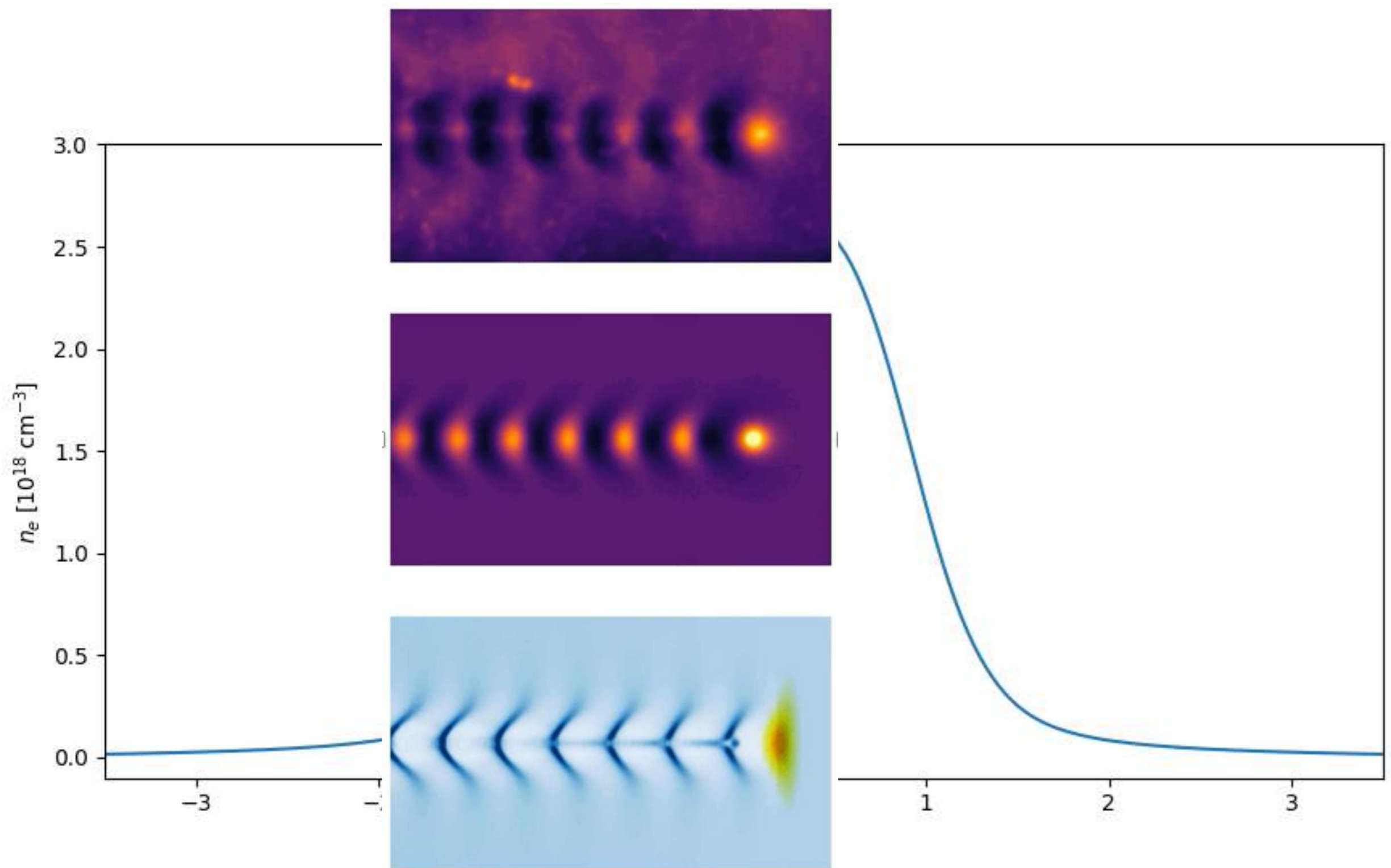
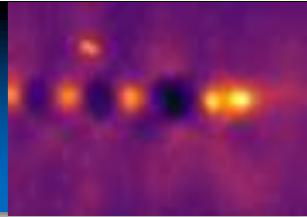
Transition from the laser to the plasma wakefield



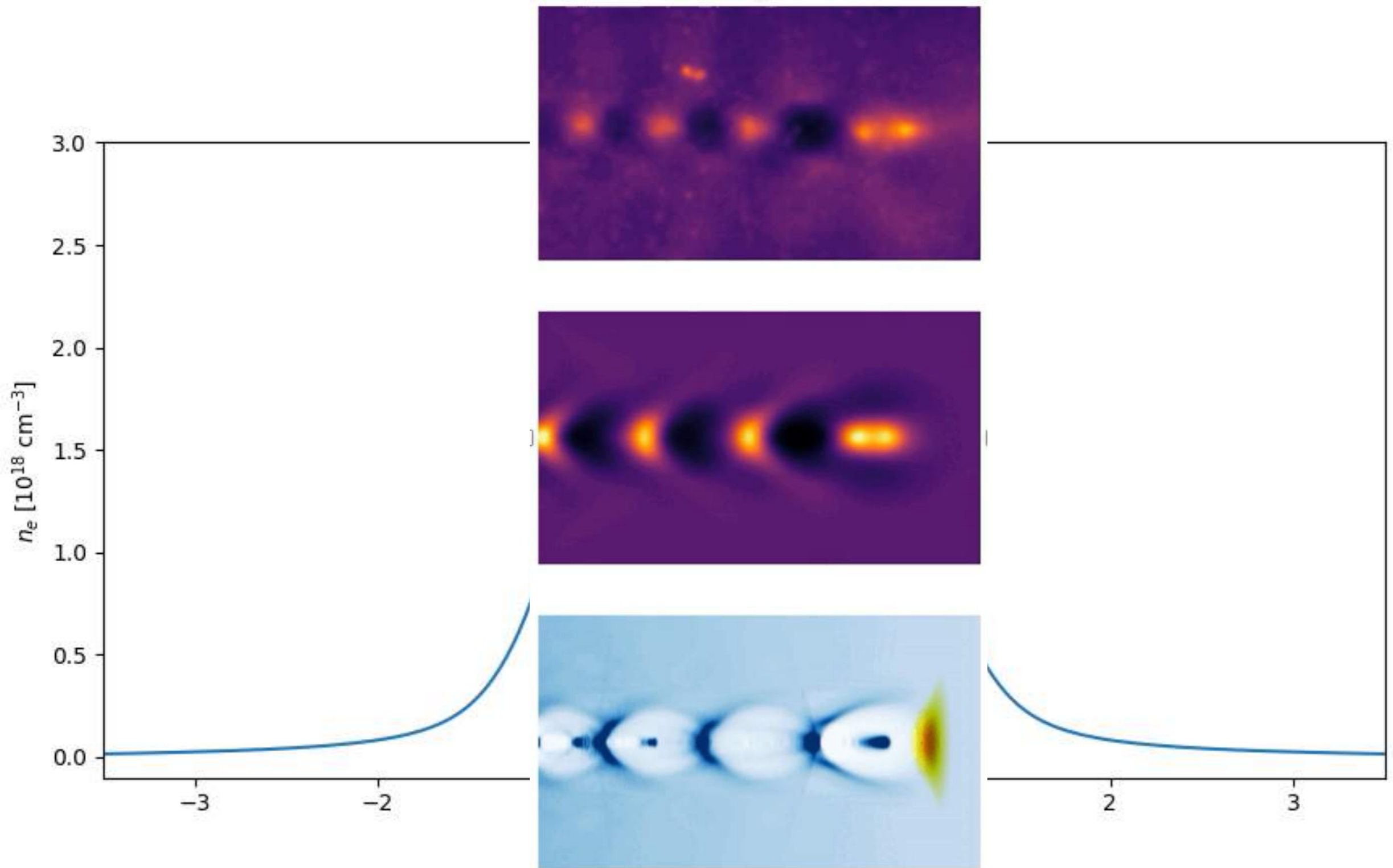
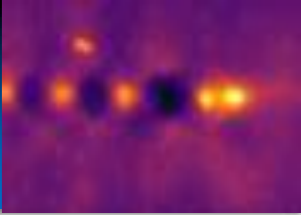
Transition from the laser to the plasma wakefield



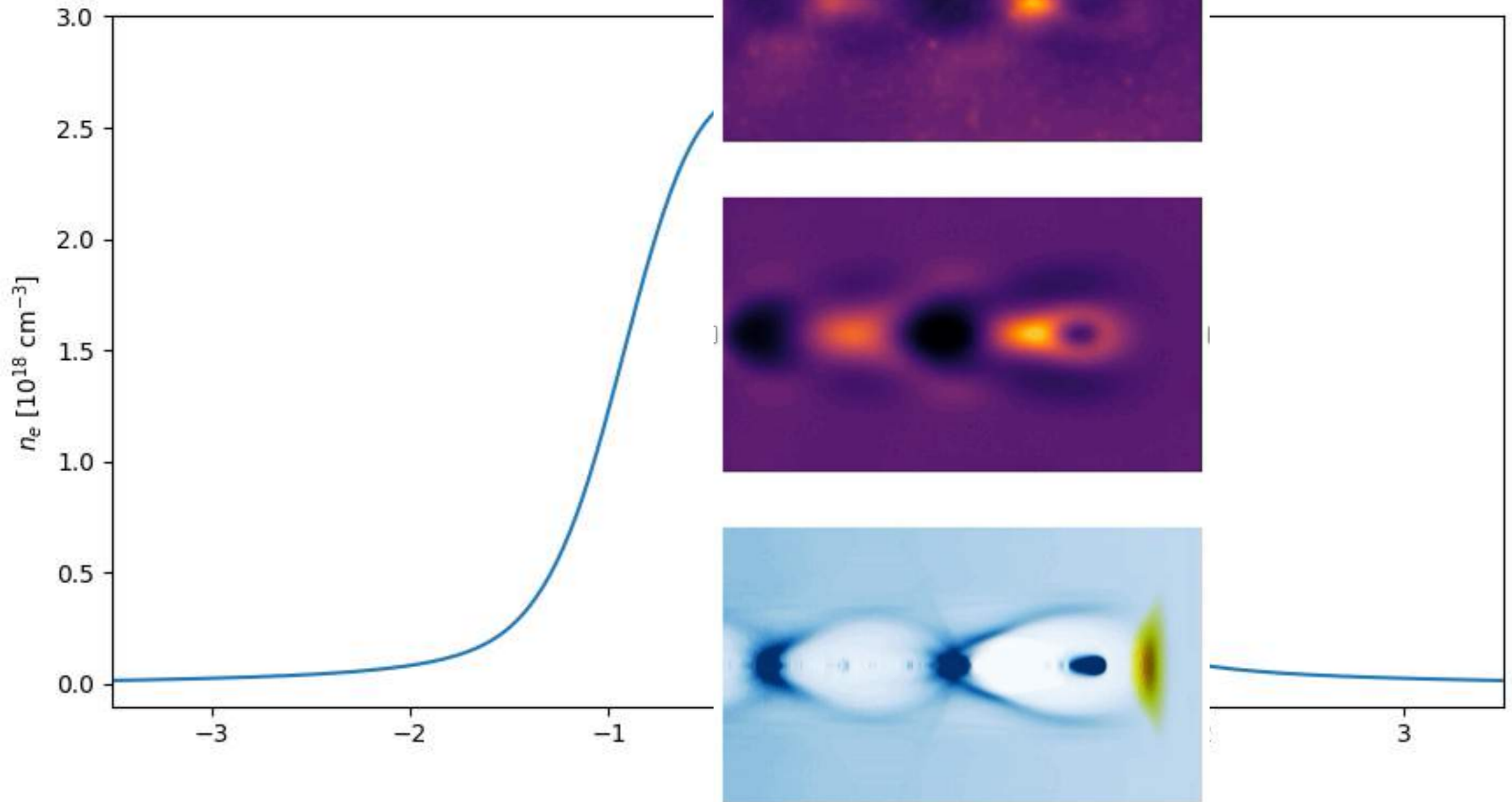
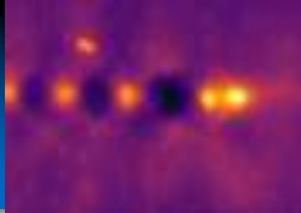
Transition from the laser to the plasma wakefield



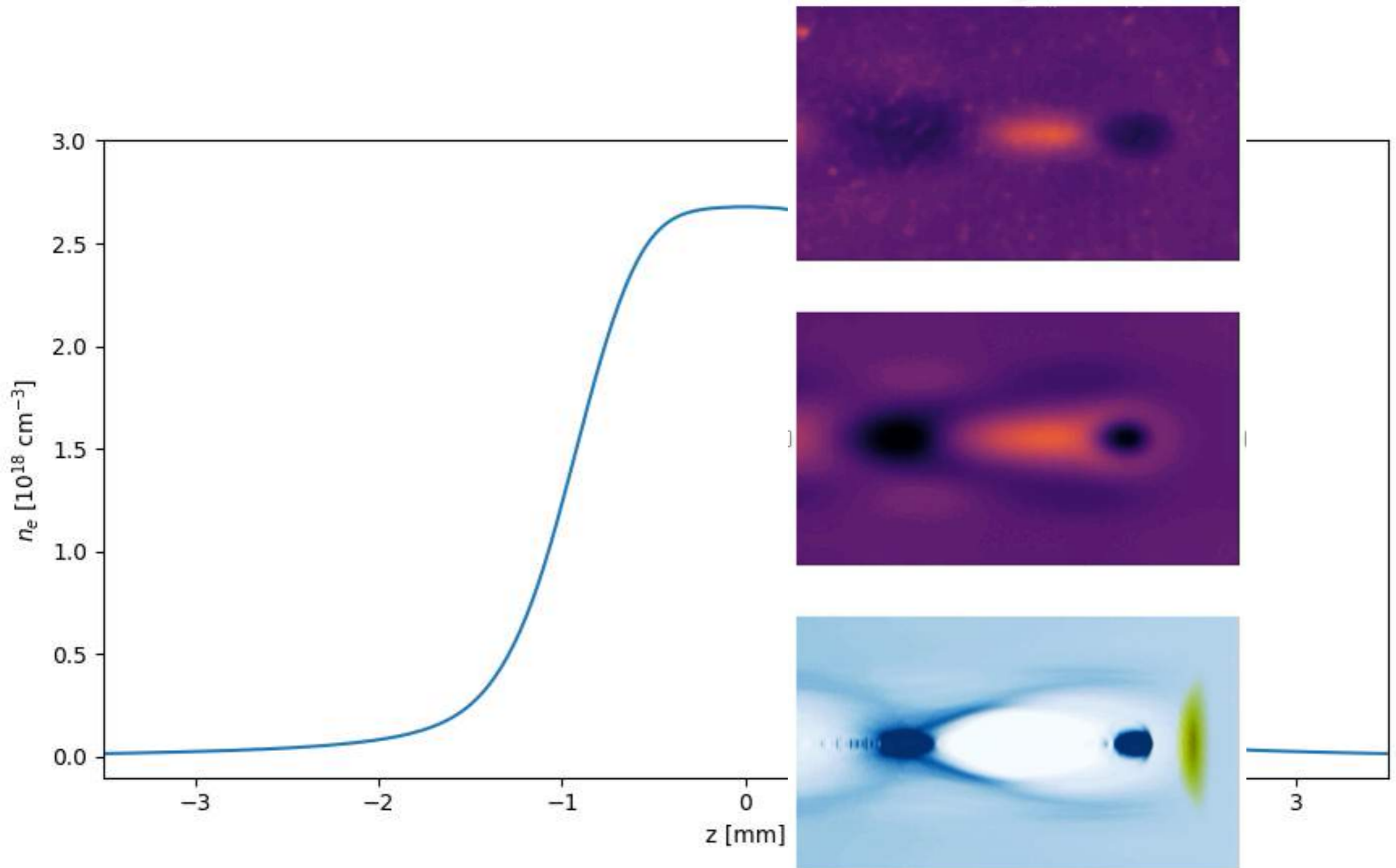
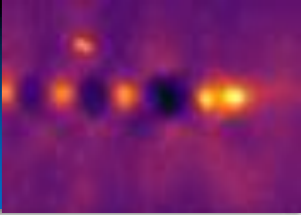
Transition from the laser to the plasma wakefield



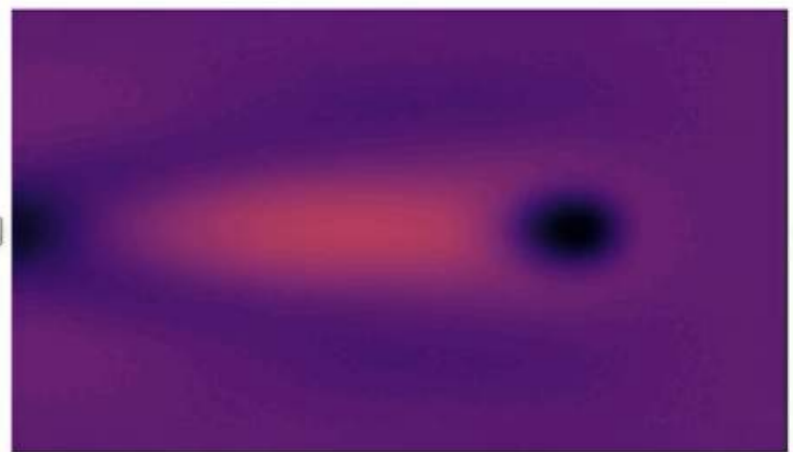
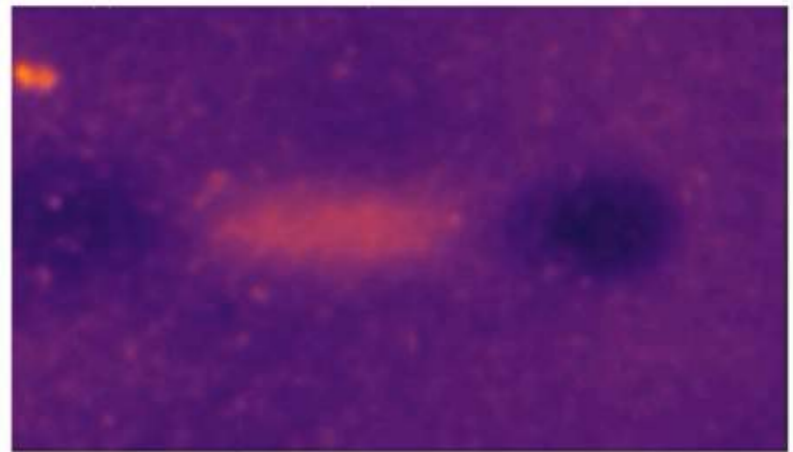
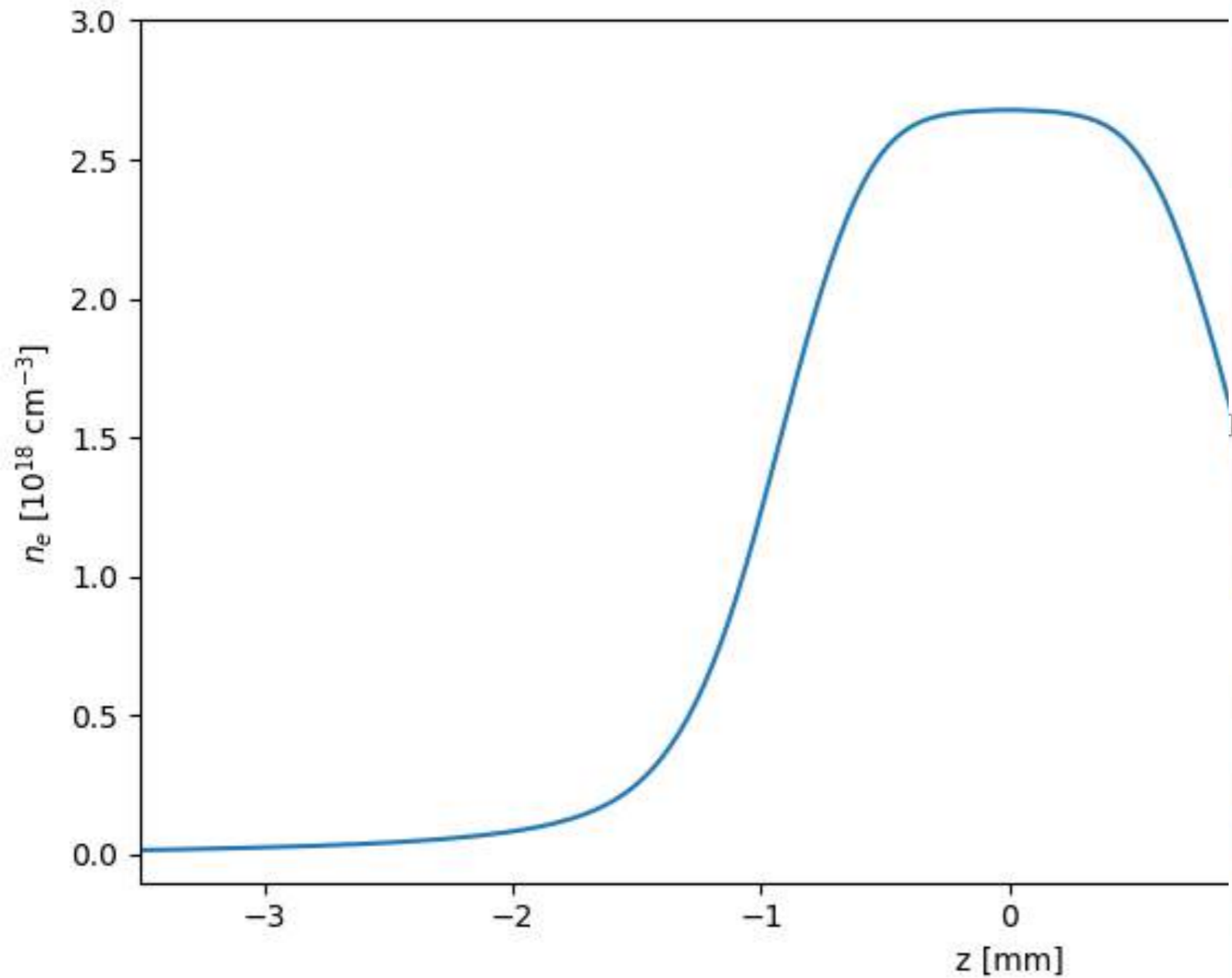
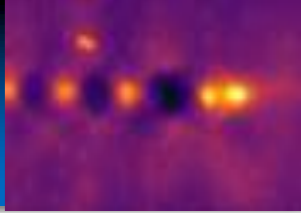
Transition from the laser to the plasma wakefield



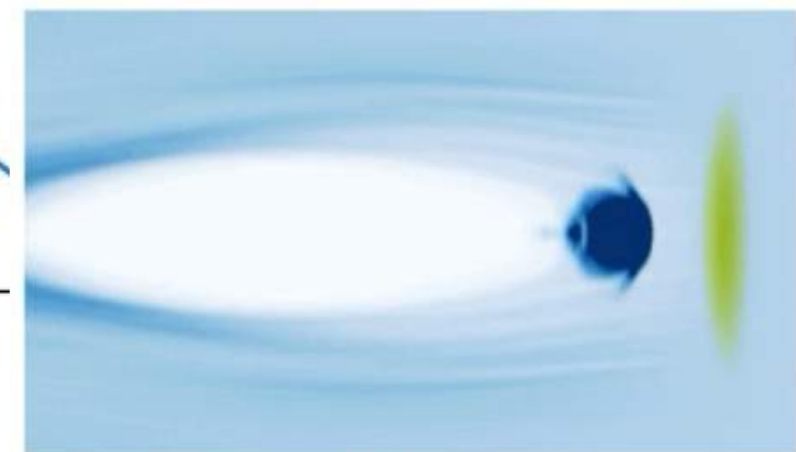
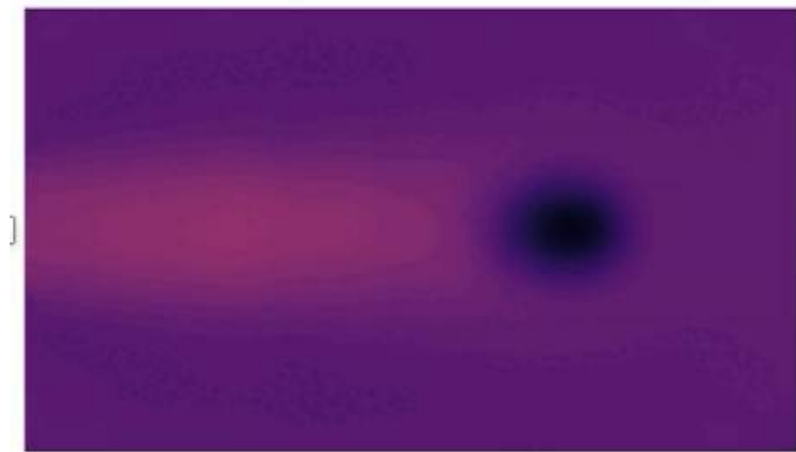
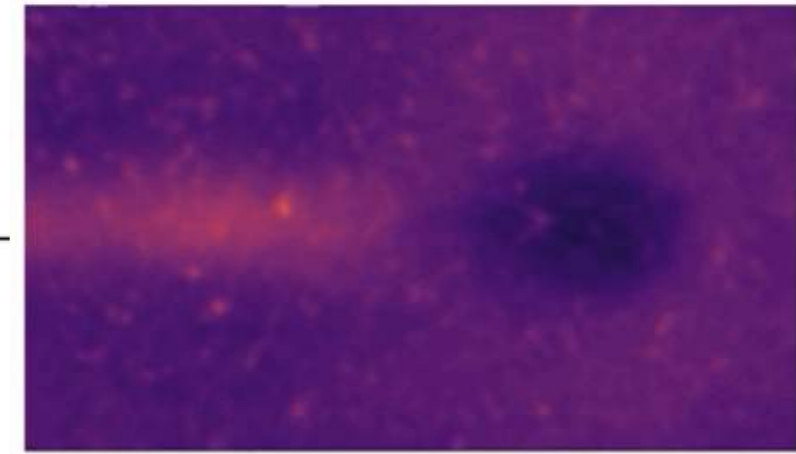
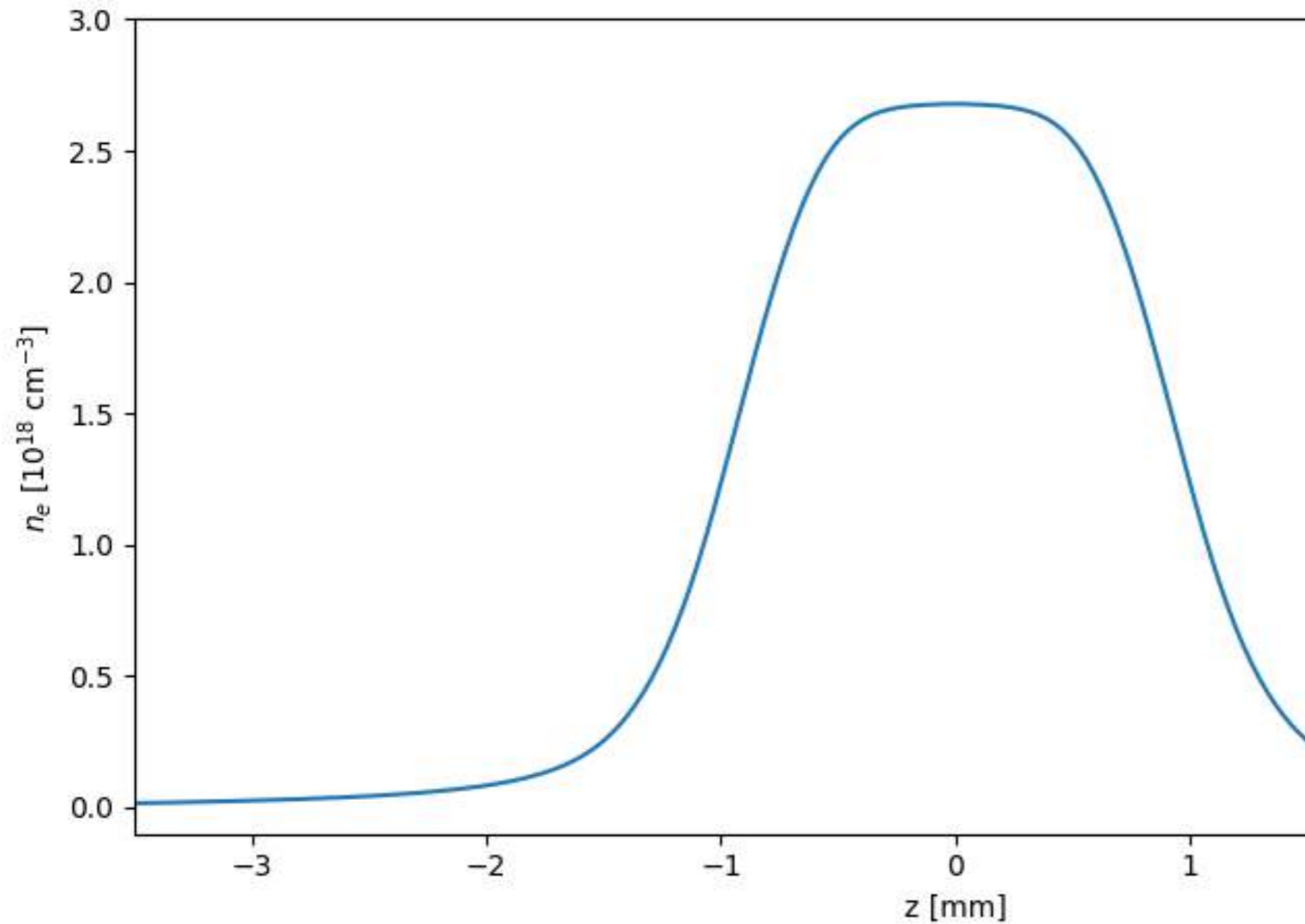
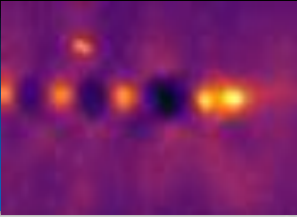
Transition from the laser to the plasma wakefield



Transition from the laser to the plasma wakefield



Transition from the laser to the plasma wakefield



A journey in the lab...



Acknowledgements

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Laserlab2&3&4, CARE/Eucard1 &2, EIC, etc..

